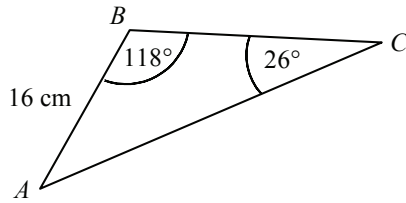
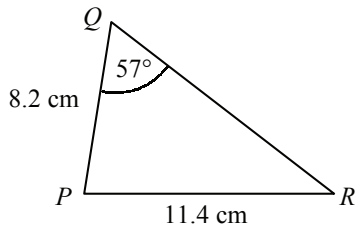


1



The diagram shows triangle ABC in which $AB = 16$ cm, $\angle ABC = 118^\circ$ and $\angle ACB = 26^\circ$.
Use the sine rule to find the length AC to 3 significant figures.

2

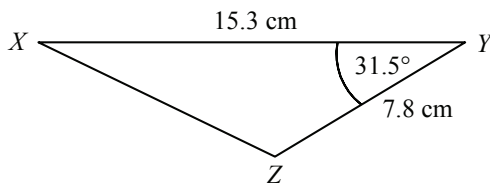


The diagram shows triangle PQR in which $PQ = 8.2$ cm, $PR = 11.4$ cm and $\angle PQR = 57^\circ$.
Use the sine rule to find the size of $\angle PRQ$ in degrees to 1 decimal place.

3 In triangle ABC , $AB = 16.2$ cm, $BC = 12.3$ cm and $\angle BAC = 37^\circ$.

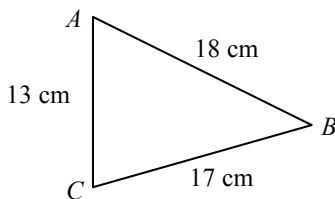
Find the two possible sizes of $\angle ACB$ and the corresponding lengths of AC .

4



The diagram shows triangle XYZ in which $XY = 15.3$ cm, $YZ = 7.8$ cm and $\angle XYZ = 31.5^\circ$.
Use the cosine rule to find the length XZ .

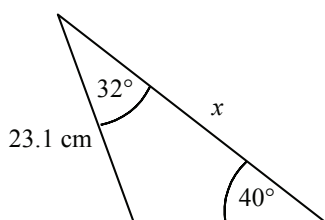
5



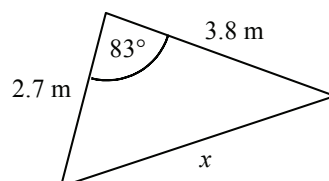
The diagram shows triangle ABC in which $AB = 18$ cm, $AC = 13$ cm and $BC = 17$ cm.
Use the cosine rule to find the size of $\angle ACB$.

6 Find the length x in each triangle.

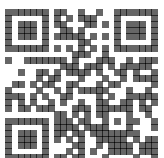
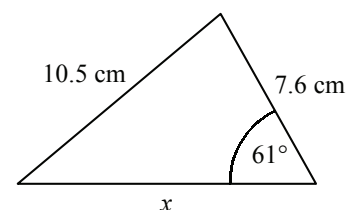
a



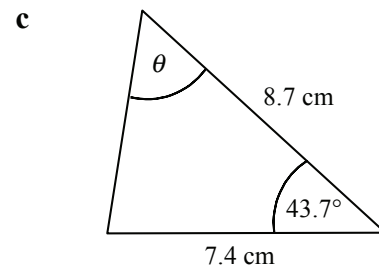
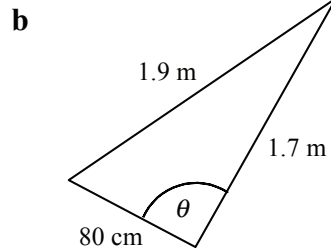
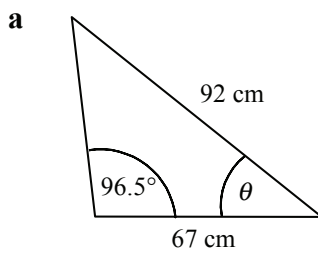
b



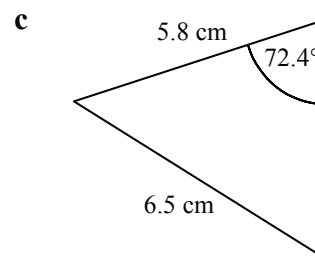
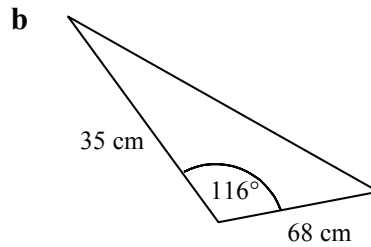
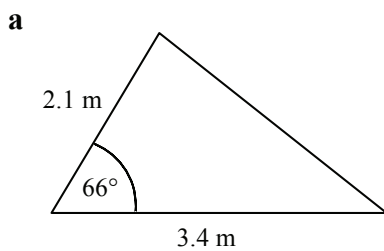
c



7 Find the angle θ in each triangle.



8 Find the area of each of the following triangles.

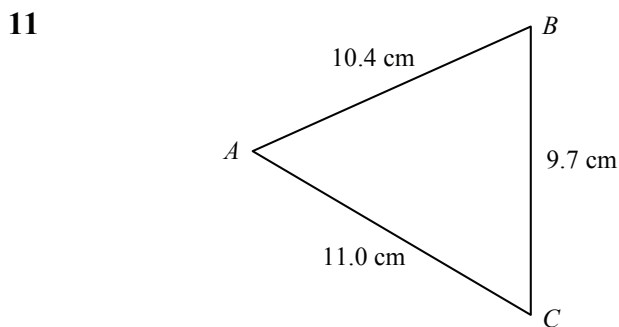


9 Joanne walks 4.2 miles on a bearing of 138° . She then walks 7.8 miles on a bearing of 251° .

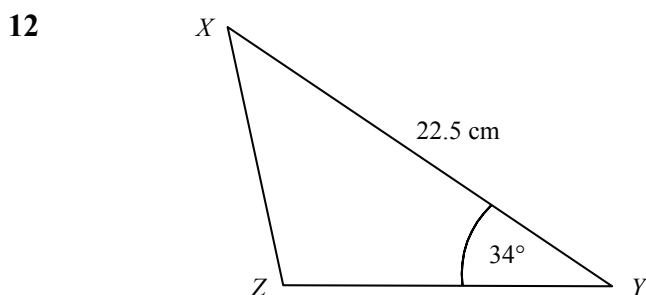
- Calculate how far Joanne is from the point where she started.
- Find, as a bearing, the direction in which Joanne would have to walk in order to return to the point where she started.

10 A ferry and a cargo ship are both approaching the same port. The ferry is 3.2 km from the port on a bearing of 076° and the cargo ship is 6.9 km from the port on a bearing of 323° .

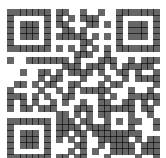
Find the distance between the two vessels and the bearing of the cargo ship from the ferry.



The diagram shows triangle ABC in which $AB = 10.4$ cm, $AC = 11.0$ cm and $BC = 9.7$ cm. Find the area of the triangle to 3 significant figures.



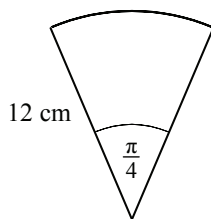
The diagram shows triangle XYZ in which $XY = 22.5$ cm and $\angle XYZ = 34^\circ$. Given that the area of the triangle is 100 cm², find the length XZ .



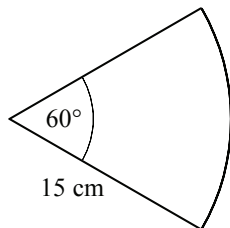
- 1 Convert each angle from degrees to radians, giving your answers in terms of π .
- a 180° b 30° c 45° d 720° e 18° f 120°
 g 15° h 40° i 270° j 7.5° k 144° l 220°
- 2 Convert each angle from degrees to radians, giving your answers to 2 decimal places.
- a 10° b 38° c 291° d 63.8° e 507° f 126.2°
- 3 Convert each angle from radians to degrees.
- a 2π b $\frac{\pi}{3}$ c $\frac{\pi}{2}$ d $\frac{3\pi}{4}$ e $\frac{\pi}{18}$ f $\frac{\pi}{30}$
 g $\frac{5\pi}{6}$ h $\frac{\pi}{8}$ i 3π j $\frac{2\pi}{15}$ k $\frac{7\pi}{3}$ l $\frac{9\pi}{20}$
- 4 Convert each angle from radians to degrees, giving your answers to 1 decimal place.
- a 2° b 0.5° c 3.1° d 1.43° e 8.7° f 0.742°

- 5 Find, in terms of π , the length of the arc in each of the following circular sectors.

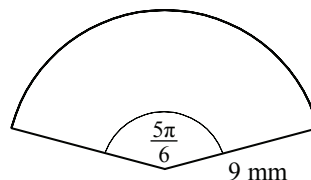
a



b

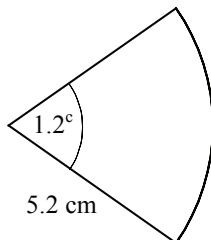


c

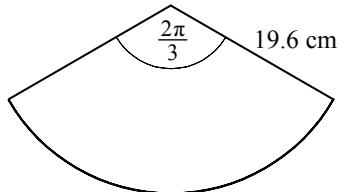


- 6 Find, to 3 significant figures, the perimeter of each of the following circular sectors.

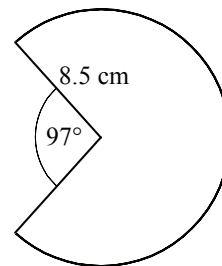
a



b

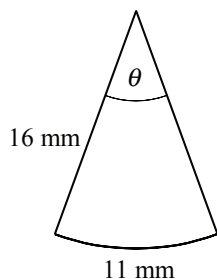


c

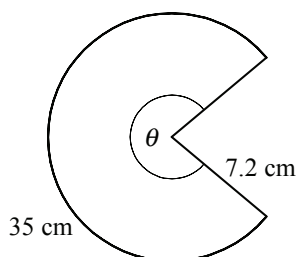


- 7 Find, in radians to 2 decimal places, the angle θ in each of the following circular sectors.

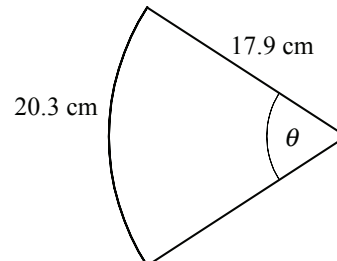
a



b



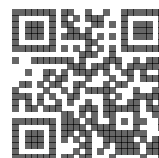
c



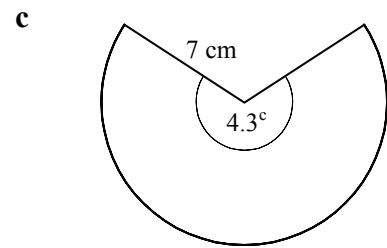
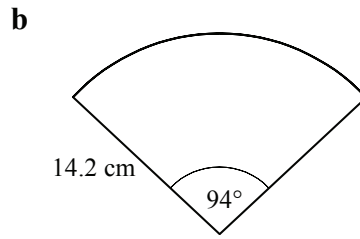
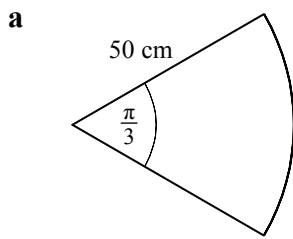
- 8 The minor arc AB of a circle, centre O , has length 46.2 cm.

Given that $\angle AOB = 78.5^\circ$, find

- a the distance OA , b the perimeter of sector OAB .



9 Find, in cm^2 to 1 decimal place, the area of each of the following circular sectors.

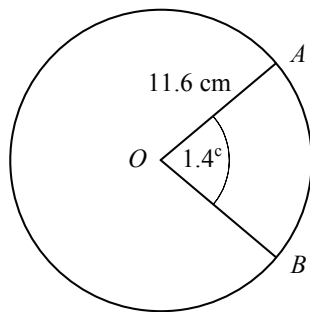


10 PQ is an arc of a circle of radius 8 cm, centre O .

Given that arc PQ has length 12 cm, find

- a the angle, in radians, subtended by PQ at O ,
b the area of sector OPQ .

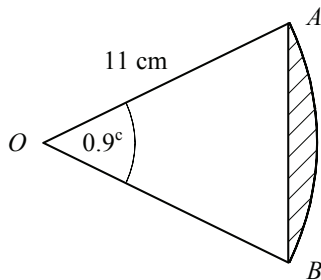
11



The diagram shows a circle of radius 11.6 cm, centre O . The arc of the circle AB subtends an angle of 1.4 radians at O . Find, to 3 significant figures,

- a the perimeter of the minor sector OAB , b the perimeter of the major sector OAB ,
c the area of the minor sector OAB , d the area of the major sector OAB .

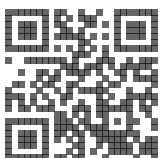
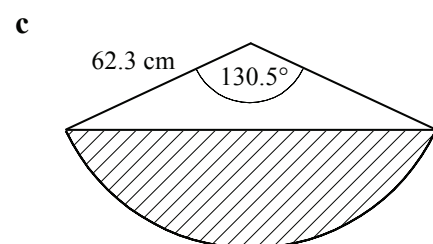
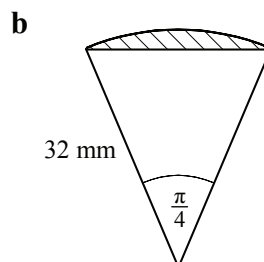
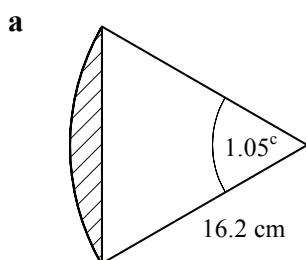
12



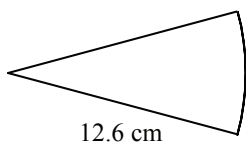
The diagram shows a circular sector OAB . Find the area of

- a the sector OAB , b the triangle OAB , c the shaded segment.

13 Find the area of the shaded segment in each of the following circular sectors.



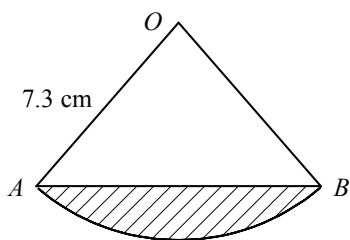
1



The diagram shows a sector of a circle of radius 12.6 cm.

Given that the perimeter of the sector is 31.7 cm, find its area.

2

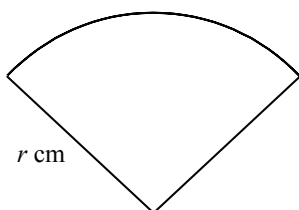


The diagram shows a sector OAB of a circle, centre O and radius 7.3 cm.

Given that the area of the sector is 38.4 cm^2 , find

- a the size of $\angle AOB$ in radians,
- b the perimeter of the shaded segment.

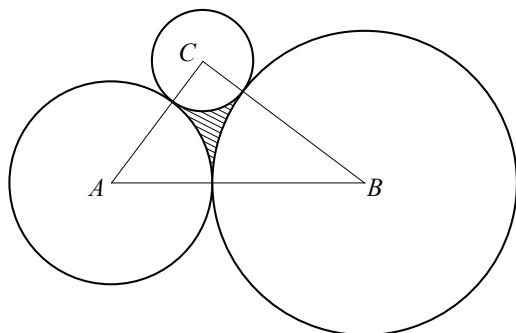
3



The diagram shows a sector of a circle of radius r cm. The area of the sector is 40 cm^2 .

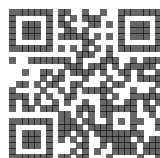
- a Show that the perimeter of the sector is $(2r + \frac{80}{r})$ cm.
- b Hence find the set of values of r for which the perimeter of the sector is less than 26 cm.

4

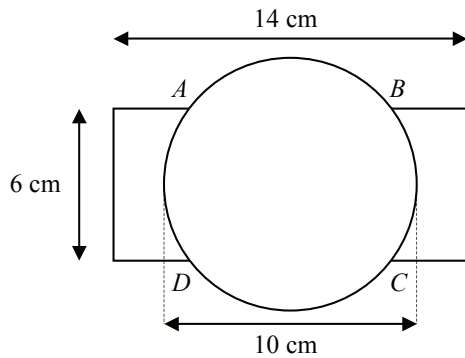


The diagram shows three circles with centres A , B and C , and radii 4 cm, 6 cm and 2 cm respectively. Each circle touches the other two circles.

- a Prove that triangle ABC is a right-angled triangle.
- b Find $\angle ABC$ in radians to 2 decimal places.
- c Show that the area of the shaded region enclosed by the three circles is 1.86 cm^2 to 3 significant figures.



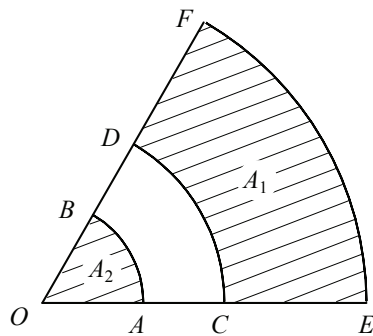
5



The diagram shows a company logo which consists of a circle of diameter 10 cm drawn on top of a rectangle measuring 6 cm by 14 cm. The centres of the circle and rectangle are coincident and the two shapes intersect at A , B , C and D .

- Find the length of the chord of the circle AB .
- Show that the perimeter of the logo is 42.5 cm to 3 significant figures.
- Find the area of the logo.

6



AB , CD and EF are arcs of concentric circles, centre O , such that $OACE$ and $OBDF$ are straight lines as shown in the diagram. The area of the shaded region $CEFD$ is denoted by A_1 and the area of the shaded sector OAB by A_2 .

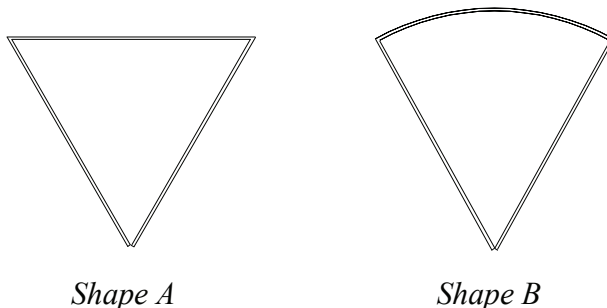
Given that $OA = r$ cm, $AC = 2$ cm, $OE = 8$ cm and $\angle AOB = \theta$ radians,

- find an expression for A_1 in terms of r and θ .

Given also that $A_1 = 7A_2$,

- show that $r = 2.5$

7

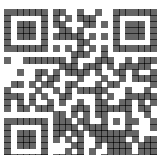


Shape A

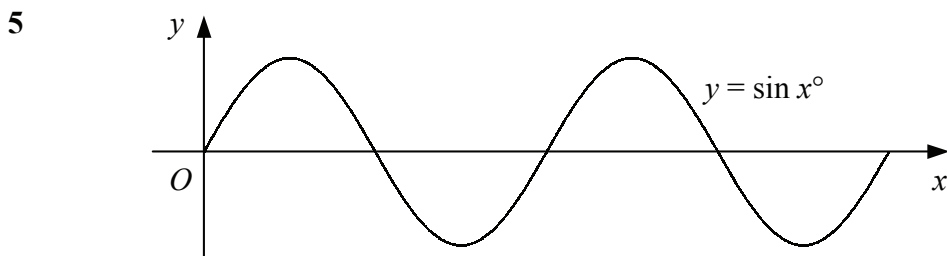
Shape B

A girl is playing with a paper clip. She straightens the wire and then bends it to form an equilateral triangle, *Shape A* above. She then curves one side of the triangle to form a sector of a circle, *Shape B* above.

Find, to 1 decimal place, the percentage change in the area enclosed by the paper clip when it is changed from *Shape A* to *Shape B*, indicating whether this is an increase or decrease.

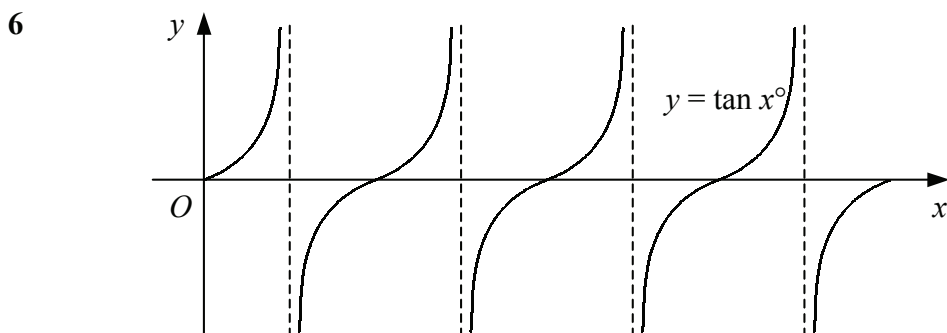


- 1 Find to 3 decimal places the value of
- | | | | |
|--------------------|----------------------|--------------------|------------------------|
| a $\sin 131^\circ$ | b $\tan 340.5^\circ$ | c $\cos 418^\circ$ | d $\sin(-165.2^\circ)$ |
|--------------------|----------------------|--------------------|------------------------|
- 2 Give the exact value of
- | | | | |
|---------------------|----------------------|---------------------|----------------------|
| a $\cos 60^\circ$ | b $\sin 45^\circ$ | c $\tan 45^\circ$ | d $\cos 30^\circ$ |
| e $\sin 90^\circ$ | f $\tan 30^\circ$ | g $\cos 120^\circ$ | h $\sin 135^\circ$ |
| i $\tan 210^\circ$ | j $\cos 225^\circ$ | k $\sin 300^\circ$ | l $\tan 120^\circ$ |
| m $\cos 330^\circ$ | n $\tan 150^\circ$ | o $\cos(-60^\circ)$ | p $\sin 405^\circ$ |
| q $\tan(-45^\circ)$ | r $\sin(-240^\circ)$ | s $\tan 570^\circ$ | t $\cos(-150^\circ)$ |
- 3 Find to 3 decimal places the value of
- | | | | |
|---------------------|---------------------|----------------------|----------------------|
| a $\cos 0.42^\circ$ | b $\sin 4.16^\circ$ | c $\tan(-3.1^\circ)$ | d $\cos 11.25^\circ$ |
|---------------------|---------------------|----------------------|----------------------|
- 4 Give the exact value of
- | | | | |
|-------------------------|---------------------------|--------------------------|---------------------------|
| a $\sin \frac{\pi}{6}$ | b $\cos \frac{\pi}{2}$ | c $\sin \frac{\pi}{4}$ | d $\tan \frac{\pi}{3}$ |
| e $\cos \frac{\pi}{3}$ | f $\sin \frac{2\pi}{3}$ | g $\tan \frac{3\pi}{4}$ | h $\cos \frac{5\pi}{6}$ |
| i $\tan \frac{5\pi}{3}$ | j $\cos \frac{5\pi}{4}$ | k $\sin(-\frac{\pi}{6})$ | l $\tan(-\frac{5\pi}{6})$ |
| m $\sin 3\pi$ | n $\tan(-\frac{5\pi}{4})$ | o $\cos \frac{8\pi}{3}$ | p $\sin(-\frac{7\pi}{3})$ |



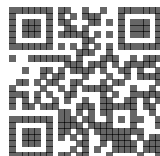
The graph shows the curve $y = \sin x^\circ$ in the interval $0 \leq x \leq 720$.

- Write down the coordinates of any points where the curve intersects the coordinate axes.
- Write down the coordinates of the turning points of the curve.



The graph shows the curve $y = \tan x^\circ$ in the interval $0 \leq x \leq 720$.

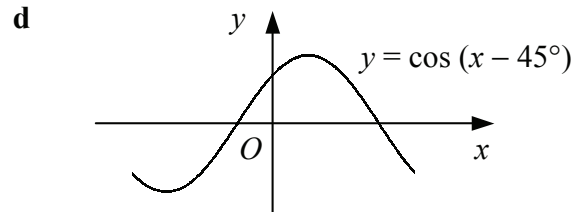
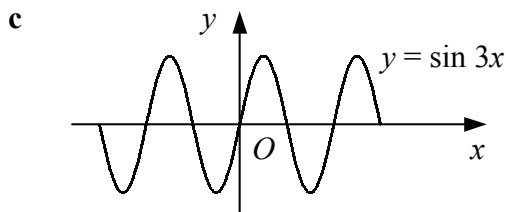
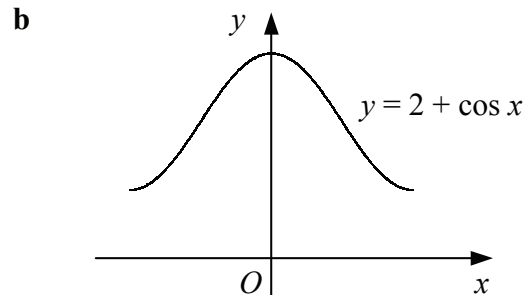
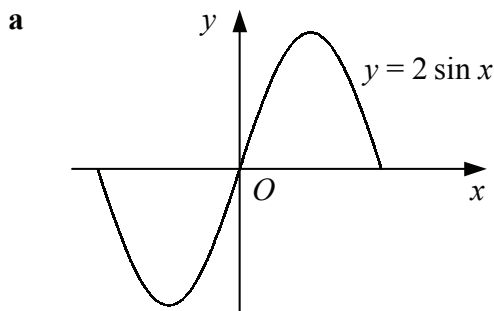
- Write down the coordinates of any points where the curve intersects the coordinate axes.
- Write down the equations of the asymptotes.



- 7 Describe the transformation that maps the graph of $y = \sin x^\circ$ onto the graph of
- a** $y = 3 \sin x^\circ$ **b** $y = \sin 4x^\circ$ **c** $y = \sin (x + 60)^\circ$ **d** $y = \sin (-x^\circ)$
- 8 Sketch each of the following pairs of curves on the same set of axes in the interval $0 \leq x \leq 360^\circ$.
- a** $y = \cos x$ and $y = 3 \cos x$ **b** $y = \sin x$ and $y = \sin (x - 30^\circ)$
c $y = \cos x$ and $y = \cos 2x$ **d** $y = \tan x$ and $y = 2 + \tan x$
e $y = \sin x$ and $y = -\sin x$ **f** $y = \cos x$ and $y = \cos (x + 60^\circ)$
g $y = \tan x$ and $y = \tan \frac{1}{2}x$ **h** $y = \sin x$ and $y = 1 + \sin x$

- 9 Each curve is shown for the interval $-180^\circ \leq x \leq 180^\circ$.

Write down the coordinates of the turning points of each curve in this interval.



- 10 Write down the period of each of the following graphs.

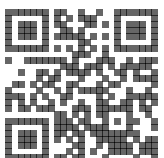
a $y = \sin x^\circ$ **b** $y = \tan x^\circ$ **c** $y = 2 \cos x^\circ$
d $y = \sin 2x^\circ$ **e** $y = \tan (x + 30)^\circ$ **f** $y = \cos \frac{1}{3}x^\circ$

- 11 Sketch each of the following curves for x in the interval $0 \leq x \leq 360$. Show the coordinates of any points of intersection with the coordinate axes and the equations of any asymptotes.

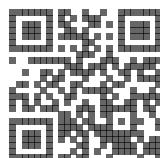
a $y = \tan x^\circ$ **b** $y = \cos (x + 30)^\circ$ **c** $y = \sin 2x^\circ$
d $y = 1 + \cos x^\circ$ **e** $y = \sin \frac{1}{2}x^\circ$ **f** $y = \tan (x + 90)^\circ$
g $y = \sin (x - 45)^\circ$ **h** $y = -\tan x^\circ$ **i** $y = \cos (x - 120)^\circ$

- 12 Sketch each of the following curves for x in the interval $0 \leq x \leq 2\pi$. Show the coordinates of any turning points and the equations of any asymptotes.

a $y = \cos x$ **b** $y = 3 \sin x$ **c** $y = \tan 2x$
d $y = \sin (x - \frac{\pi}{3})$ **e** $y = \cos \frac{1}{3}x$ **f** $y = \sin x - 2$
g $y = \tan (x + \frac{\pi}{4})$ **h** $y = \sin \frac{3}{4}x$ **i** $y = \cos (x - \frac{\pi}{6})$



- 1 Find all values of x in the interval $0 \leq x \leq 360^\circ$ such that
- | | | | |
|----------------------------------|---------------------------------|----------------------------------|---------------------------|
| a $\sin x = \frac{1}{2}$ | b $\tan x = \sqrt{3}$ | c $\cos x = 0$ | d $\sin x = -1$ |
| e $\cos x = \frac{\sqrt{3}}{2}$ | f $\sin x = \frac{1}{\sqrt{2}}$ | g $\tan x = -1$ | h $\cos x = -\frac{1}{2}$ |
| i $\sin x = -\frac{\sqrt{3}}{2}$ | j $\tan x = \frac{1}{\sqrt{3}}$ | k $\cos x = -\frac{1}{\sqrt{2}}$ | l $\tan x = -\sqrt{3}$ |
- 2 Solve each equation for θ in the interval $0 \leq \theta \leq 360^\circ$ giving your answers to 1 decimal place.
- | | | | |
|-------------------------|-------------------------|--------------------------|--------------------------|
| a $\cos \theta = 0.4$ | b $\sin \theta = 0.27$ | c $\tan \theta = 1.6$ | d $\sin \theta = 0.813$ |
| e $\tan \theta = 0.1$ | f $\cos \theta = 0.185$ | g $\sin \theta = -0.6$ | h $\tan \theta = -0.7$ |
| i $\cos \theta = -0.39$ | j $\tan \theta = -3.4$ | k $\cos \theta = -0.636$ | l $\sin \theta = -0.203$ |
- 3 Solve each equation for x in the interval $0 \leq x \leq 360$.
Give your answers to 1 decimal place where appropriate.
- | | | |
|-------------------------------------|--------------------------------|--------------------------------|
| a $\sin(x - 60)^\circ = 0.5$ | b $\tan(x + 30)^\circ = 1$ | c $\cos(x - 45)^\circ = 0.2$ |
| d $\tan(x + 30)^\circ = 0.78$ | e $\cos(x + 45)^\circ = -0.5$ | f $\sin(x - 60)^\circ = -0.89$ |
| g $\cos(x + 45)^\circ = 0.9$ | h $\sin(x + 30)^\circ = 0.14$ | i $\cos(x - 60)^\circ = 0.6$ |
| j $\sin(x - 30)^\circ = -0.3$ | k $\tan(x - 60)^\circ = -1.26$ | l $\sin 2x^\circ = 0.5$ |
| m $\cos 2x^\circ = 0.64$ | n $\sin 2x^\circ = -0.18$ | o $\tan 2x^\circ = -2.74$ |
| p $\sin \frac{1}{2}x^\circ = 0.703$ | q $\tan 3x^\circ = 0.591$ | r $\cos 2x^\circ = -0.415$ |
- 4 Solve each equation for x in the interval $0 \leq x \leq 2\pi$ giving your answers in terms of π .
- | | | |
|--|---|---|
| a $\sin x = 0$ | b $\cos x = \frac{1}{2}$ | c $\tan x = 1$ |
| d $\cos x = -1$ | e $\tan x = -\frac{1}{\sqrt{3}}$ | f $\sin x = -\frac{1}{\sqrt{2}}$ |
| g $\tan(x + \frac{\pi}{6}) = \sqrt{3}$ | h $\sin(x - \frac{\pi}{4}) = \frac{1}{2}$ | i $\cos(x + \frac{\pi}{3}) = -\frac{\sqrt{3}}{2}$ |
| j $\sin(x + \frac{\pi}{3}) = \frac{1}{\sqrt{2}}$ | k $\cos 2x = -\frac{1}{\sqrt{2}}$ | l $\tan 3x = \frac{1}{\sqrt{3}}$ |
- 5 Solve each equation for θ in the interval $-180^\circ \leq \theta \leq 180^\circ$.
Give your answers to 1 decimal place where appropriate.
- | | | |
|--------------------------------------|---------------------------------------|--------------------------------------|
| a $\cos \theta = 0$ | b $\tan 2\theta + 1 = 0$ | c $\sin(\theta + 60^\circ) = 0.291$ |
| d $2 \tan(\theta - 15^\circ) = 3.7$ | e $\sin 2\theta - 0.3 = 0$ | f $4 \cos 3\theta = 2$ |
| g $1 + \sin(\theta + 110^\circ) = 0$ | h $5 \cos(\theta - 27^\circ) = 3$ | i $7 - 3 \tan \theta = 0$ |
| j $3 + 8 \cos 2\theta = 0$ | k $2 + 6 \tan(\theta + 92^\circ) = 0$ | l $1 - 4 \sin \frac{1}{3}\theta = 0$ |



- 6 Solve each equation for x in the interval $0 \leq x \leq 180^\circ$.
Give your answers to 1 decimal place where appropriate.
- a $\tan(2x + 30^\circ) = 1$ b $\sin(2x - 15^\circ) = 0$ c $\cos(2x + 70^\circ) = 0.5$
d $\sin(2x + 210^\circ) = 0.26$ e $\cos(2x - 38^\circ) = -0.64$ f $\tan(2x - 56^\circ) = -0.32$
g $\cos(3x - 24^\circ) = 0.733$ h $\tan(3x + 60^\circ) = -1.9$ i $\sin(\frac{1}{2}x + 18^\circ) = 0.572$
- 7 Solve each equation for x in the interval $0 \leq x \leq 2\pi$, giving your answers to 2 decimal places.
- a $\tan x = 0.52$ b $\cos 2x = 0.315$ c $\sin(x + \frac{\pi}{4}) = 0.7$
d $3 \cos x + 1 = 0$ e $\sin \frac{1}{2}x = 0.09$ f $\tan 2x = -0.225$
g $3 - 4 \sin(x - \frac{\pi}{3}) = 0$ h $\tan(2x + \frac{\pi}{6}) = 2$ i $\cos 3x = -0.81$
j $5 + 3 \tan x = 0$ k $\cos(2x - \frac{\pi}{2}) = -0.34$ l $1 + 6 \sin 2x = 0$
- 8 a Solve the equation

$$2y^2 - 3y + 1 = 0.$$
- b Hence, find the values of x in the interval $0 \leq x \leq 360^\circ$ for which

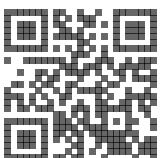
$$2 \sin^2 x - 3 \sin x + 1 = 0.$$
- 9 Solve each equation for θ in the interval $0 \leq \theta \leq 360$.
Give your answers to 1 decimal place where appropriate.
- a $\sin^2 \theta^\circ = 0.75$ b $1 - \tan^2 \theta^\circ = 0$
c $2 \cos^2 \theta^\circ + \cos \theta^\circ = 0$ d $\sin \theta^\circ(4 \cos \theta^\circ - 1) = 0$
e $4 \sin \theta^\circ = \sin \theta^\circ \tan \theta^\circ$ f $(2 \cos \theta^\circ - 1)(\cos \theta^\circ + 1) = 0$
g $\tan^2 \theta^\circ - 3 \tan \theta^\circ + 2 = 0$ h $3 \sin^2 \theta^\circ - 7 \sin \theta^\circ + 2 = 0$
i $\tan^2 \theta^\circ - \tan \theta^\circ = 6$ j $6 \cos^2 \theta^\circ - \cos \theta^\circ - 2 = 0$
k $4 \sin^2 \theta^\circ + 3 = 8 \sin \theta^\circ$ l $\cos^2 \theta^\circ + 2 \cos \theta^\circ - 1 = 0$
m $\tan^2 \theta^\circ + 3 \tan \theta^\circ - 1 = 0$ n $3 \sin^2 \theta^\circ + \sin \theta^\circ = 1$
- 10 a Sketch the curve $y = \cos x^\circ$ for x in the interval $0 \leq x \leq 360$.
b Sketch on the same diagram the curve $y = \cos(x + 90)^\circ$ for x in the interval $0 \leq x \leq 360$.
c Using your diagram, find all values of x in the interval $0 \leq x \leq 360$ for which

$$\cos x^\circ = \cos(x + 90)^\circ.$$
- 11 a Sketch the curves $y = \cos x^\circ$ and $y = \cos 3x^\circ$ on the same set of axes for x in the interval $0 \leq x \leq 360$.
b Solve, for x in the interval $0 \leq x \leq 360$, the equation

$$\cos x^\circ = \cos 3x^\circ.$$

c Hence solve, for x in the interval $0 \leq x \leq 180$, the equation

$$\cos 2x^\circ = \cos 6x^\circ.$$



1 a Given that $4 \sin x + \cos x = 0$, show that $\tan x = -\frac{1}{4}$.

b Hence, find the values of x in the interval $0 \leq x \leq 360^\circ$ for which
 $4 \sin x + \cos x = 0$,
 giving your answers to 1 decimal place.

2 a Show that

$$5 \sin^2 x + 5 \sin x + 4 \cos^2 x \equiv \sin^2 x + 5 \sin x + 4.$$

b Hence, find the values of x in the interval $0 \leq x \leq 360^\circ$ for which
 $5 \sin^2 x + 5 \sin x + 4 \cos^2 x = 0$

3 Solve each equation for x in the interval $0 \leq x \leq 360^\circ$.

Give your answers to 1 decimal place where appropriate.

a $2 \sin x - \cos x = 0$

b $3 \sin x = 4 \cos x$

c $\cos^2 x + 3 \sin x - 3 = 0$

d $3 \cos^2 x - \sin^2 x = 2$

e $2 \sin^2 x + 3 \cos x = 3$

f $3 \cos^2 x = 5(1 - \sin x)$

g $3 \sin x \tan x = 8$

h $\cos x = 3 \tan x$

i $3 \sin^2 x - 5 \cos x + 2 \cos^2 x = 0$

j $2 \sin^2 x + 7 \sin x - 2 \cos^2 x = 0$

k $3 \sin x - 2 \tan x = 0$

l $\sin^2 x - 9 \cos x - \cos^2 x = 5$

4 Solve each equation for θ in the interval $-\pi \leq \theta \leq \pi$ giving your answers in terms of π .

a $4 \cos^2 \theta = 1$

b $4 \sin^2 \theta + 4 \sin \theta + 1 = 0$

c $\cos^2 \theta + 2 \cos \theta - 3 = 0$

d $3 \sin^2 \theta - \cos^2 \theta = 0$

e $4 \sin^2 \theta - 5 \sin \theta + 2 \cos^2 \theta = 0$

f $\sin^2 \theta - 3 \cos \theta - \cos^2 \theta = 2$

5 Prove that

a $(\sin x + \cos x)^2 \equiv 1 + 2 \sin x \cos x$

b $\frac{1}{\cos x} - \cos x \equiv \sin x \tan x, \cos x \neq 0$

c $\frac{\cos^2 x}{1 - \sin x} \equiv 1 + \sin x, \sin x \neq 1$

d $\frac{1 + \sin x}{\cos x} \equiv \frac{\cos x}{1 - \sin x}, \cos x \neq 0$

6 a Prove the identity

$$(\cos x - \tan x)^2 + (\sin x + 1)^2 \equiv 2 + \tan^2 x.$$

b Hence find, in terms of π , the values of x in the interval $0 \leq x \leq 2\pi$ such that

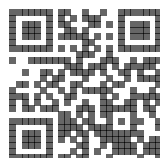
$$(\cos x - \tan x)^2 + (\sin x + 1)^2 = 3.$$

7 $f(x) \equiv \cos^2 x + 2 \sin x, 0 \leq x \leq 2\pi.$

a Prove that $f(x)$ can be expressed in the form

$$f(x) = 2 - (\sin x - 1)^2.$$

b Hence deduce the maximum value of $f(x)$ and the value of x for which this occurs.



1 Find, in terms of π , the values of x in the interval $0 \leq x \leq 2\pi$ for which

a $3 \tan x - \sqrt{3} = 0$,

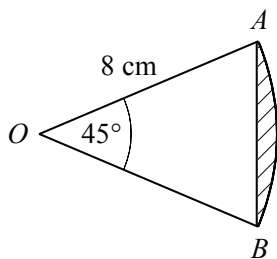
b $2 \cos(x + \frac{\pi}{3}) + \sqrt{3} = 0$.

2 Given that $\cos A = \sqrt{3} - 1$,

a find the value of $\sin^2 A$ in the form $p\sqrt{3} + q$ where p and q are integers,

b show that $\tan^2 A = \frac{\sqrt{3}}{2}$.

3



The diagram shows sector OAB of a circle, centre O , radius 8 cm, in which $\angle AOB = 45^\circ$.

a Find the perimeter of the sector in centimetres to 1 decimal place.

b Show that the area of the shaded segment is $8(\pi - 2\sqrt{2}) \text{ cm}^2$.

4 Find, to 1 decimal place, the values of θ in the interval $0 \leq \theta \leq 360^\circ$ for which

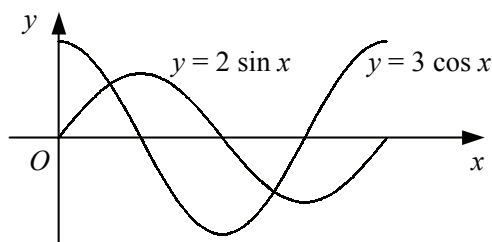
$$2 \sin^2 \theta + \sin \theta - \cos^2 \theta = 2.$$

5 Solve, for x in the interval $-\pi \leq x \leq \pi$, the equation

$$3 \sin^2 x = 4(1 - \sin x),$$

giving your answers to 2 decimal places.

6



The diagram shows the curves $y = 2 \sin x$ and $y = 3 \cos x$ for x in the interval $0 \leq x \leq 2\pi$.

Find, to 2 decimal places, the coordinates of the points where the curves intersect in this interval.

7 a Sketch the curve $y = \cos 2x^\circ$ for x in the interval $0 \leq x \leq 360$.

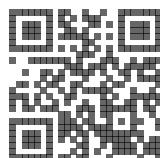
b Find the values of x in the interval $0 \leq x \leq 360$ for which

$$\cos 2x^\circ = -\frac{1}{2}.$$

8 Solve, for θ in the interval $0 \leq \theta \leq 360$, the equation

$$12 \cos \theta^\circ = 7 \tan \theta^\circ,$$

giving your answers to 1 decimal place.

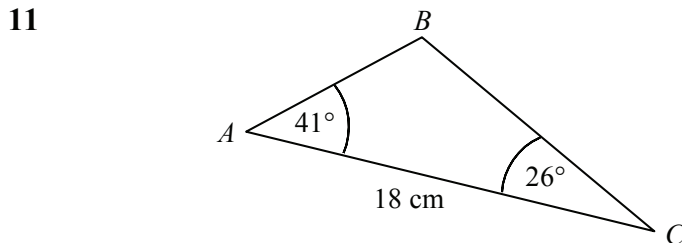


9 Given that $\tan 15^\circ = \frac{\tan 60^\circ - \tan 45^\circ}{1 + (\tan 60^\circ \times \tan 45^\circ)}$,

a show that $\tan 15^\circ = 2 - \sqrt{3}$,

b find the exact value of $\tan 345^\circ$.

10 Find, to an appropriate degree of accuracy, the values of x in the interval $0 \leq x \leq 360^\circ$ for which $\sin^2 x + 5 \cos x - 3 \cos^2 x = 2$.



The diagram shows triangle ABC in which $AC = 18$ cm, $\angle BAC = 41^\circ$ and $\angle ACB = 26^\circ$.

Find to 3 significant figures

a the length BC ,

b the area of triangle ABC .

12 Solve, for θ in the interval $0 \leq \theta \leq 360^\circ$, the equation

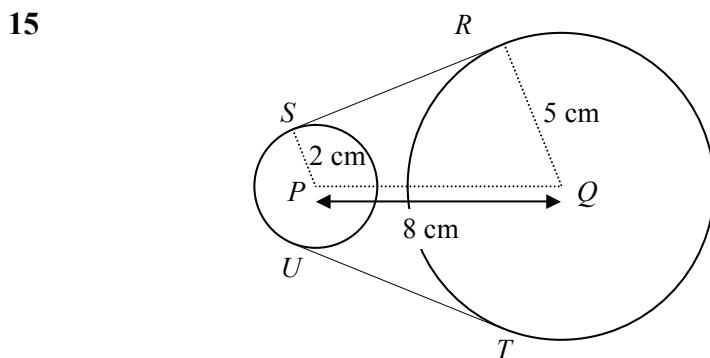
$$(6 \cos \theta - 1)(\cos \theta + 1) = 3.$$

13 Find, in degrees to 1 decimal place, the values of x in the interval $-180^\circ \leq x \leq 180^\circ$ for which $\sin^2 x + 5 \sin x = 2 \cos^2 x$.

14 Prove that

a $\sin^4 \theta - 2 \sin^2 \theta \equiv \cos^4 \theta - 1$,

b $\frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} \equiv \frac{2}{\sin \theta}$, for $\sin \theta \neq 0$.



The gears in a toy are shown in the diagram above.

A thin rubber band passes around two circular discs. The centres of the discs are at P and Q where $PQ = 8$ cm and their radii are 2 cm and 5 cm respectively. The sections of the rubber band not in contact with the discs, RS and TU , are assumed to be taut.

a Show that $\angle PQR = 1.186$ radians to 3 decimal places.

b Find the length RS .

c Find the length of the rubber band in this situation.

