Solomon Practice Paper

Statistics S1 - L

90	minutes
•	90

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Name:

Teacher:

Question	Points	Score
1	7	
2	8	
3	10	
4	11	
5	12	
6	12	
7	15	
Total:	75	

How I can achieve better:

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July 14, 2025



1. A shop recorded the number of pairs of gloves, n, that it sold and the average daytime temperature, T° , for each month over a 12-month period. The data was then summarised as follows:

$$\sum T = 124$$
, $\sum n = 384$, $\sum T^2 = 1802$, $\sum n^2 = 18518$, $\sum Tn = 2583$.

- (a) Calculate the product moment correlation coefficient for these data.
- (b) Comment on what your value shows and suggest a reason for this.

[5]

[2]

Total: 7



2. Events A and B are independent. Given also that

$$\Pr(A) = \frac{3}{4}$$
 and $\Pr(A \cap B') = \frac{1}{4}$.

Find

(a) $\Pr(A \cap B)$,	[2]
(b) $\Pr(B)$,	[3]
(c) $\Pr(A' \cap B')$.	[3]
	Total: 8

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3. The random variable X is such that

$$E(X) = a$$
 and $Var(X) = b$

Find expressions in terms of a and b for

(a) E(2X + 3), [1] (b) Var(2X + 3), [2] (c) $E(X^2)$. [3] (d) Show that $E[(X + 1)^2] = (a + 1)^2 + b$. [4] Total: 10





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4. An engineer tested a new material under extreme conditions in a wind tunnel. He recorded the number of microfractures, n, that formed and the wind speed, v metres per second, for 8 different values of v with all other conditions remaining constant. He then coded the data using x = v - 700 and y = n - 20 and calculated the following summary statistics.

$$\sum x = 100, \quad \sum y = 23, \quad \sum x^2 = 215000, \quad \sum xy = 11600.$$

- (a) Find an equation of the regression line of y on x.
- (b) Hence, find an equation of the regression line of n on v.
- (c) Use your regression line to estimate the number of microfractures that would be formed if the material was tested in a wind speed of 900 metres per second with all other conditions remaining constant.

Total: 11

[7]

[2]

[2]



Value of goods stolen \pounds	(Number of weeks)
0 - 199	31
200-399	6
400-599	3
600-799	4
800-999	5
1000-1999	2
2000-2999	1

5. An antiques shop recorded the value of items stolen to the nearest pound during each week for a year giving the data in the table below.

Letting x represent the mid-point of each group and using the coding $y = \frac{x - 699.5}{200}$,

- (a) find $\sum fy$.
- (b) estimate to the nearest pound the mean and standard deviation of the value of the goods [6] stolen each week using your value for $\sum fy$ and $\sum fy^2 = 424$.

The median for these data is $\pounds 82$.

(c) Explain why the manager of the shop might be reluctant to use either the mean or the [3] median in summarising these data.

Total: 12

[3]

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- 6. At the start of a gameshow there are 10 contestants of which 6 are female. In each round of the game, one contestant is eliminated. All of the contestants have the same chance of progressing to the next round each time.
 - (a) Show that the probability that the first two contestants to be eliminated are both male is $\begin{bmatrix} 3 \\ \frac{2}{15} \end{bmatrix}$.
 - (b) Find the probability that more females than males are eliminated in the first three rounds[6] of the game.
 - (c) Given that the first contestant to be eliminated is male, find the probability that the next [3] two contestants to be eliminated are both female.

Total: 12



7. A cyber-cafe recorded how long each user stayed during one day giving the following results.

Length of stay (minutes)	0 -	30 -	60 -	90 -	120 -	240 -	360 -
Number of users	15	31	32	23	17	2	0

(a) Use linear interpolation to estimate the median and quartiles of these data.

The results of a previous study had led to the suggestion that the length of time each user stays can be modelled by a normal distribution with a mean of 72 minutes and a standard deviation of 48 minutes.

- (b) Find the median and quartiles that this model would predict.
- (c) Comment on the suitability of the suggested model in the light of the new results.

Total: 15

[6]

[7]

[2]