## Solomon Practice Paper

Further Pure Mathematics 1H

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	8	
3	9	
4	9	
5	10	
6	15	
7	18	
Total:	75	

How I can achieve better:

- •



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1. (a) Given that

show that

(b) Hence find

$$f(r+1) - f(r) = r \times r!$$
$$\sum_{r=1}^{n} r \times r!.$$

 $\mathbf{f}(r) = r!,$ 

L'O1	ta	l:	6

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[2]

[4]

2. (a) Given that

$$y = \frac{2x}{x^2 + 9},$$

express x in terms of y.

(b) Hence prove that for all real values of x

$$-\frac{1}{a} \le \frac{2x}{x^2 + 9} \le \frac{1}{a},$$

where a is a positive integer which you should find.

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[3]

Total: 8

[5]

3. Find the general solution of the differential equation

$$x\frac{\mathrm{d}y}{\mathrm{d}x} + xy = 1 - y,$$

giving your answer in the form y = f(x).

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Figure above shows part of the curves  $y = x^2$  and  $y = \frac{3}{3x-2}$ . The curves meet at the point with x-coordinate  $\alpha$ .

(a) Find the integer N such that

$$\frac{N}{10} < \alpha < \frac{N+1}{10}.$$

(b) Use interval bisection on the interval found in part (a) to find the value of  $\alpha$  correct to 2 [5] decimal places.

Total: 9

[4]

5. Given that

 $f(z) \equiv z^4 - 4z^3 + kz^2 - 4z + 13,$ 

where k is a real constant, and that  $z = \mathbf{i}$  is a solution of the equation f(z) = 0,

- (a) show that k = 14,
- (b) find all solutions of the equation f(z) = 0.

Total: 10

[3]

[7]



6. The shape of a company logo is to be the region enclosed by the curve with polar equation



A sign in the shape of the logo is to be made by cutting the area enclosed by the curve from a square sheet of metal OPQR where O is the pole and R lies on the initial line,  $\theta = 0$ , as shown.

PQ and QR are tangents to the curve, parallel and perpendicular to the initial line respectively, at the points A and B on the curve.

- (a) Find the value of  $\theta$  at the point A.
- (b) Show that the area of OPQR is  $\frac{3\sqrt{3}}{8}a^2$ . [3]
- (c) Find the area of the metal sheet which is not used.

Total: 15

[7]

[5]

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7. Given that  $x = ke^{-t}$  satisfies the differential equation

$$\frac{\mathrm{d}^2 x}{\mathrm{d}t^2} + 5\frac{\mathrm{d}x}{\mathrm{d}t} + 6x = 8\mathrm{e}^{-t},$$

- (a) find the value of k.
- (b) Hence find the solution of the differential equation for which x = 1 and  $\frac{\mathrm{d}x}{\mathrm{d}t} = 3$  at t = 0. [8]
- The maximum value of x occurs when t = T.
- (c) Show that the maximum value of x is  $\frac{40}{27}$  and find the value of T.

[7] Total: 18

[3]

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