

# Solomon Practice Paper

## Further Pure Mathematics 1F

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	4	
2	7	
3	7	
4	7	
5	10	
6	10	
7	14	
8	16	
Total:	75	

How I can achieve better:

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- 



Last updated: July 14, 2025



1.

[4]

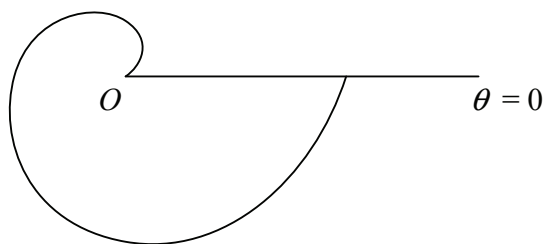
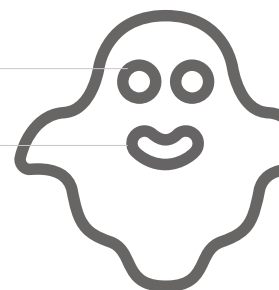


Figure above shows the curve with polar equation

$$r = a\theta, \quad 0 \leq \theta < 2\pi, \quad a > 0.$$

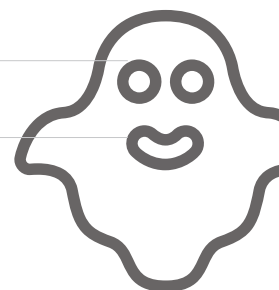
Find the area of the finite region bounded by the curve and the initial line  $\theta = 0$ .



2. Find the set of values of  $x$  for which

[7]

$$\frac{(x-1)(x+2)}{x+4} > 4.$$



3.

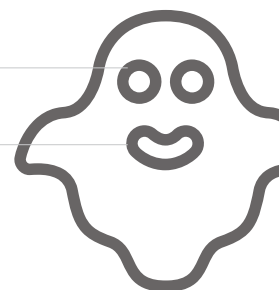
$$f(x) = 3x^5 - 7x^2 + 3.$$

- (a) Show that there is a root,  $\alpha$ , of the equation  $f(x) = 0$  in the interval  $[0, 1]$ . [2]
- (b) Use linear interpolation once on the interval  $[0, 1]$  to estimate the value of  $\alpha$ . [2]

There is another root,  $\beta$ , of the equation  $f(x) = 0$  close to  $-0.62$ .

- (c) Use the Newton–Raphson method once to obtain a second approximation to  $\beta$ , giving your answer correct to 3 decimal places. [3]

Total: 7



4. The Cartesian equation of the curve  $C$  is

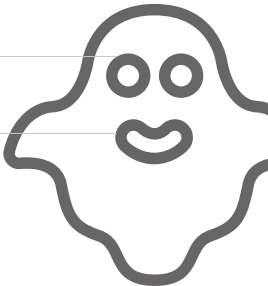
$$(x^2 + y^2)^2 = a^2 (x^2 - y^2).$$

(a) Show that, in polar coordinates, the equation of curve  $C$  can be written as [4]

$$r^2 = a^2 \cos(2\theta).$$

(b) Sketch the curve  $C$  for  $0 \leq \theta < 2\pi$ . [3]

Total: 7



5. (a) Show that the substitution  $y = \frac{1}{u}$  transforms the differential equation [3]

$$\frac{dy}{dx} + \frac{y}{x} - xy^2 = 0$$

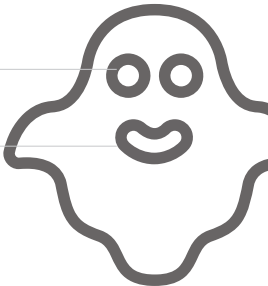
(★)

into the differential equation

$$\frac{du}{dx} - \frac{u}{x} + x = 0.$$

(b) Hence find the solution of differential equation (★) such that  $y = 1$  when  $x = 1$ , giving your [7]  
answer in the form  $y = f(x)$ .

Total: 10



6. (a) Find  $\sum_{r=n+1}^{2n} r^2$  in terms of  $n$ . [4]

(b) Hence, or otherwise, show that [6]

$$4 \leq \frac{\sum_{r=n+1}^{2n} r^2}{\sum_{r=1}^n r^2} < 7$$

for all positive integer values of  $n$ .

Total: 10

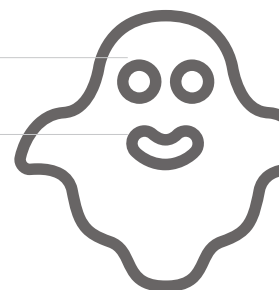


$$2\frac{d^2x}{dt^2} - 5\frac{dx}{dt} - 3x = 20\sin(t).$$

Initially the particle is at  $x = 5$ .

(b) find an expression for  $x$  in terms of  $t$ . [4]

Total: 14





8. The complex numbers  $z_1$  and  $z_2$  are given by

$$z_1 = \frac{1 + \mathbf{i}}{1 - \mathbf{i}} \quad \text{and} \quad z_2 = \frac{\sqrt{2}}{1 - \mathbf{i}}$$

- (a) Find  $z_1$  in the form  $a + \mathbf{i}b$  where  $a$  and  $b$  are real. [2]
- (b) Write down the modulus and argument of  $z_1$ . [2]
- (c) Find the modulus and argument of  $z_2$ . [4]
- (d) Show the points representing  $z_1$ ,  $z_2$  and  $z_1 + z_2$  on the same Argand diagram, and hence find [8]  
the exact value of  $\tan \frac{3\pi}{8}$ .

Total: 16

