Solomon Practice Paper

Further Pure Mathematics 1E

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	7	
2	7	
3	9	
4	10	
5	12	
6	13	
7	17	
Total:	75	

How I can achieve better:

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July 14, 2025



Further Mathematics – Practice Paper 1E

- 1. The complex number w is given by $w = \frac{10 + 5\mathbf{i}}{2 \mathbf{i}}$.
 - (a) Express w in the form $a + \mathbf{i}b$ where a and b are real.
 - (b) Using your answer to part (a) find the complex number z such that

$$z + 2z^{\star} = w$$

Total: 7

[3]

[4]



2. Show that

$$\sum_{r=0}^{n} (r+1)(r+2) = \frac{1}{3}(n+1)(n+2)(n+3).$$



3. Find the equation of the curve which passes through the origin and for which

$$\frac{\mathrm{d}y}{\mathrm{d}x} = x + y,$$

giving your answer in the form y = f(x).

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4. The curve C has the polar equation

$$r = a(1 + \sin \theta), \quad 0 \le \theta \le \frac{\pi}{2}.$$

- (a) Sketch the curve C.
- (b) Find the polar coordinates of the point on the curve where the tangent to the curve is [8] perpendicular to the initial line $\theta = 0$.

Total: 10

[2]

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5. (a) Find, in terms of a and b, the equations of the asymptotes to the curve with equation

$$y = \frac{ax - 1}{x + b},$$

where a and b are positive constants.

(b) Sketch the curve

$$y = \frac{ax - 1}{x + b},\tag{3}$$

showing the coordinates of any points of intersection with the coordinate axes.

(c) Hence, or otherwise, find the set of values of x for which

$$\left|\frac{3x-1}{x+2}\right| < 2.$$

Total: 12

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[6]

[3]

- 6. (a) Show that the equation $e^x 4 \sin x = 0$ has a root, α , in the interval [0, 1] and a root, β , in [3] the interval [1, 1.5].
 - (b) Using the Newton–Raphson method with an initial value of x = 0.5, find α correct to 2 [5] decimal places.
 - (c) Use linear interpolation once between the values x = 1 and x = 1.5 to find an approximate [3] value for β , giving your answer correct to 1 decimal place.
 - (d) Determine whether or not your answer to part (c) gives the value of β correct to 1 decimal [2] place.

Total: 13

7. (a) Given that y is a function of t and that $x = t^{\frac{1}{2}}$, where x > 0, show that

i.
$$\frac{\mathrm{d}y}{\mathrm{d}x} = 2t^{\frac{1}{2}}\frac{\mathrm{d}y}{\mathrm{d}t},$$

ii.
$$\frac{\mathrm{d}^2y}{\mathrm{d}x^2} = \frac{\mathrm{d}y}{\mathrm{d}t} + 4t\frac{\mathrm{d}^2y}{\mathrm{d}t^2}.$$

(b) Use your answers to part (a) to show that the substitution $x = t^{\frac{1}{2}}$ transforms the differential [4] equation

$$\frac{1}{x^2}\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} + \left(\frac{4}{x} - \frac{1}{x^3}\right)\frac{\mathrm{d}y}{\mathrm{d}x} + 3y = 3x^2 + 5 \tag{(\star)}$$

into the differential equation

$$4\frac{\mathrm{d}^2 y}{\mathrm{d}t^2} + 8\frac{\mathrm{d}y}{\mathrm{d}t} + 3y = 3t + 5.$$

(c) Hence find the general solution of differential equation (\star) .

[7]

[6]

Total: 17

