Solomon Practice Paper

Core Mathematics 4B

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	7	
3	8	
4	9	
5	9	
6	11	
7	12	
8	13	
Total:	75	

How I can achieve better:

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- •



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1. Use integration by parts to find

$$\int x \sin(x) dx.$$

2. Given that y = -2 when x = 1, solve the differential equation

$$\frac{\mathrm{d}y}{\mathrm{d}x} = y^2 \sqrt{x},$$

 $\int a^2 \sin(a) da$ 

giving your answer in the form y = f(x).

3. A curve has the equation

Find an equation for the normal to the curve at the point with coordinates 
$$(-1, -3)$$
.

 $4x^2 - 2xy - y^2 + 11 = 0.$ 

4. (a) Expand

 $(1+ax)^{-3}, \qquad |ax| < 1,$ 

in ascending powers of x up to and including the term in  $x^3$ . Give each coefficient as simply as possible in terms of the constant a.

Given that the coefficient of  $x^2$  in the expansion of

$$\frac{6-x}{(1+ax)^3}, \qquad |ax| < 1,$$

is 3,

(b) find the two possible values of a.

Given also that a < 0,

(c) show that the coefficient of  $x^3$  in the expansion of  $\frac{6-x}{(1+ax)^3}$  is  $\frac{14}{9}$ . [2] Total: 9

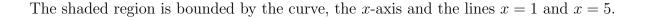
 $y = \frac{1}{\sqrt{3x+1}}$ 

5

5. Figure shows the curve with equation  $y = \frac{1}{\sqrt{3x+1}}$ .

0

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[6]

[7]

[3]

[8]

[4]

(a) Find the area of the shaded region.

The shaded region is rotated completely about the x-axis.

(b) Find the volume of the solid formed, giving your answer in the form  $k\pi \ln(2)$ , where k is a [5] simplified fraction.

6.

$$\mathbf{f}(x) = \frac{15 - 17x}{(2+x)(1-3x)^2}, \qquad x \neq -2, \ x \neq \frac{1}{3}$$

(a) Find the values of the constants A, B and C such that

$$\mathbf{f}(x) = \frac{A}{2+x} + \frac{B}{1-3x} + \frac{C}{(1-3x)^2}.$$

(b) Find the value of

$$\int_{-1}^{0} \mathbf{f}(x) \, \mathrm{d}x,$$

giving your answer in the form  $p + \ln(q)$ , where p and q are integers.

Total: 11

7. Figure shows the curve with parametric equations

$$x = -1 + 4\cos(\theta)$$
 and  $y = 2\sqrt{2}\sin(\theta)$ ,  $0 \le \theta < 2\pi$ .

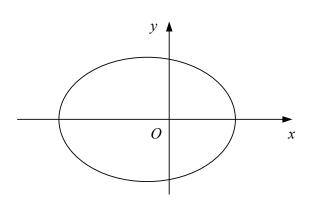


- (a) Find the value of θ at P.
  (b) Show that the normal to the curve at P passes through the origin.
  (c) Find a Cartesian equation for the curve.
  [3] Total: 12
- 8. The line  $l_1$  passes through the points A and B with position vectors  $(-3\mathbf{i}+3\mathbf{j}+2\mathbf{k})$  and  $(7\mathbf{i}-\mathbf{j}+12\mathbf{k})$  respectively, relative to a fixed origin.



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Total: 9

[4]

[7]

The line  $l_2$  has the equation

 $\mathbf{r} = (5\mathbf{j} - 7\mathbf{k}) + \mu(\mathbf{i} - 2\mathbf{j} + 7\mathbf{k}).$ 

The point C lies on  $l_2$  and is such that AC is perpendicular to BC.

(b) Show that one possible position vector for C is  $\mathbf{i} + 3\mathbf{j}$  and find the other.

Assuming that C has position vector  $(\mathbf{i} + 3\mathbf{j})$ ,

(c) find the area of triangle ABC, giving your answer in the form  $k\sqrt{5}$ .

Total: 13

[2]

[8]

[3]