Solomon Practice Paper

Core Mathematics 3I

Time allowed: 90 minutes

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Name:

Teacher:

Question	Points	Score
1	5	
2	8	
3	8	
4	8	
5	9	
6	11	
7	12	
8	14	
Total:	75	

How I can achieve better:

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Last updated: May 5, 2023



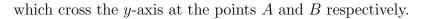
## Core Mathematics – Practice Paper 3I

1. Express

$$\frac{2x}{2x^2 + 3x - 5} \div \frac{x^3}{x^2 - x}$$

as a single fraction in its simplest form.

2. Figure shows the curves  $y = 3 + 2e^x$  and  $y = e^{x+2}$ 



(a) Find the exact length AB.

The two curves intersect at the point C.

(b) Find an expression for the x-coordinate of C and show that the y-coordinate of C is  $\frac{3e^2}{e^2-2}$ . [5]

Total: 8

3.

$$f(x) = \frac{x^2 + 3}{4x + 1}, x \in \mathbb{R}, x \neq -\frac{1}{4}.$$

(a) Find and simplify an expression for f'(x).

(b) Find the set of values of x for which f(x) is increasing.

4. The curve C has the equation  $y = x^2 - 5x + 2\ln\left(\frac{x}{3}\right), x > 0.$ 

(a) Show that the normal to C at the point where x = 3 has the equation

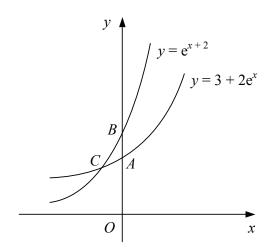
$$3x + 5y + 21 = 0$$

- (b) Find the x-coordinates of the stationary points of C.
- 5. The functions f and g are defined by

$$f(x) \equiv 6x - 1, \qquad x \in \mathbb{R}, g(x) \equiv \log_2(3x + 1), \quad x \in \mathbb{R}, x > -\frac{1}{2}$$

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[5]

[3]

[3]

[5]

 $\left[5\right]$ 

Total: 8

[3]

Total: 8

## Core Mathematics – Practice Paper 3I

- (a) Evaluate gf(1).
- (b) Find an expression for  $g^{-1}(x)$ .
- (c) Find, in terms of natural logarithms, the solution of the equation  $fg^{-1}(x) = 2$ .
- 6. (a) Use the identities for  $\cos(A+B)$  and  $\cos(A-B)$  to prove that

$$\cos(P) - \cos(Q) \equiv -2\sin\left(\frac{P+Q}{2}\right)\sin\left(\frac{P-Q}{2}\right)$$

(b) Hence find all solutions in the interval  $0 \le x < 180^{\circ}$  to the equation

$$\cos(5x^\circ) + \sin(3x^\circ) - \cos(x^\circ) = 0.$$

7. The function f is defined by

$$\mathbf{f}(x) \equiv x^2 - 2ax, \quad x \in \mathbb{R},$$

where a is a positive constant.

- (a) Showing the coordinates of any points where each graph meets the axes, sketch on separate [6] diagrams the graphs of
  - i. y = |f(x)|, ii. y = f(|x|).

The function g is defined by

$$g(x) \equiv 3ax, \quad x \in \mathbb{R}$$

- (b) Find fg(a) in terms of a.
- (c) Solve the equation  $gf(x) = 9a^3$ .
- 8.

$$f(x) = 2x + \sin(x) - 3\cos(x).$$

- (a) Show that the equation f(x) = 0 has a root in the interval [0.7, 0.8].
- (b) Find an equation for the tangent to the curve y = f(x) at the point where it crosses the [4] y-axis.
- (c) Find the values of the constants a, b and c, where b > 0 and  $0 < c < \frac{\pi}{2}$ , such that

$$f'(x) = a + b\cos(x - c).$$

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[4]

[2]

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Total: 9

Total: 11

[7]

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Total: 12

Total: 14