Solomon Practice Paper

Core Mathematics 3K

Time allowed: 90 minutes

Question	Points	Score
1	8	
2	9	
3	9	
4	10	
5	12	
6	13	
7	14	
Total:	75	

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Name:

Teacher:

How I can achieve better:

- •
- •







1. (a) Find the exact value of x such that

 $3\arctan(x-2) + \pi = 0.$

(b) Solve, for $-\pi < \theta < \pi$, the equation

$$\cos(2\theta) - \sin(\theta) - 1 = 0,$$

giving your answers in terms of π .



[3]

[5]

Total: 8

2. (a) Express

$$\frac{4x}{x^2-9} - \frac{2}{x+3}$$

as a single fraction in its simplest form.

(b) Simplify

$$\frac{x^3 - 8}{3x^2 - 8x + 4}.$$
[5]

Total: 9

[4]

3. Differentiate each of the following with respect to x and simplify your answers.

(a) $\cot(x^2)$	[2]
(b) $x^2 e^{-x}$	[3]
(c) $\frac{\sin(x)}{3 + 2\cos(x)}$	[4]
	Total: 9



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4. (a) Find, as natural logarithms, the solutions of the equation

$$e^{2x} - 8e^x + 15 = 0.$$

(b) Use proof by contradiction to prove that $\log_2(3)$ is irrational.

Total: 10



[6]

5. The function f is defined by

	$f: x \to 3e^{x-1}, x \in \mathbb{R}$	$\mathbb{R}.$	
(a) State the range of f.			
(b) Find an expression for f^{-1}	$^{1}(x)$ and state its domain.		
The function g is defined by			
	g: $x \to 5x - 2, x \in \mathbb{R}$		
Find, in terms of e,			
(c) the value of $gf(\ln(2))$,			

(d) the solution of the equation $f^{-1}g(x) = 4$.

Total: 12

[1]

[4]

[3]

[4]



6.

$$f(x) = 2x^2 + 3\ln(2-x)$$
 $x \in \mathbb{R}, x < 2.$

(a) Show that the equation f(x) = 0 can be written in the form

$$x = 2 - e^{kx^2},$$

where k is a constant to be found.

The root, α , of the equation f(x) = 0 is 1.9 correct to 1 decimal place.

(b) Use the iteration formula

$$x_{n+1} = 2 - \mathrm{e}^{kx_n^2},$$

with $x_0 = 1.9$ and your value of k, to find α to 3 decimal places and justify the accuracy of your answer.

(c) Solve the equation f'(x) = 0.

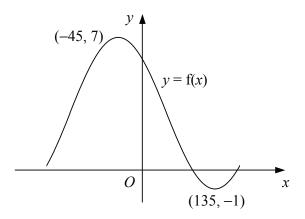
[5]

[5]

[3]

Total: 13

7. Figure shows the curve y = f(x) which has



a maximum point at (-45, 7) and a minimum point at (135, -1).

(a) Showing the coordinates of any stationary points, sketch on separate diagrams the graphs [6] of

i.
$$y = f(|x|)$$
,
ii. $y = 1 + 2f(x)$.

Given that

$$f(x) = A + 2\sqrt{2}\cos(x^{\circ}) - 2\sqrt{2}\sin(x^{\circ}), \quad x \in \mathbb{R}, -180 \le x \le 180,$$

where A is a constant,

(b) show that f(x) can be expressed in the form

$$f(x) = A + R\cos(x + \alpha)^{\circ},$$

where R > 0 and $0 < \alpha < 90$,

- (c) state the value of A,
- (d) find, to 1 decimal place, the x-coordinates of the points where the curve y = f(x) crosses [4] the x-axis.

[3]

[1]



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