

# Solomon Practice Paper

## Core Mathematics 4D

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	6	
2	8	
3	10	
4	12	
5	12	
6	13	
7	14	
Total:	75	

How I can achieve better:

- 
- 
- 



Last updated: July 14, 2025



1. (a) Find the binomial expansion of  $(2 - 3x)^{-3}$  in ascending powers of  $x$  up to and including the term in  $x^3$ , simplifying each coefficient. [5]
- (b) State the set of values of  $x$  for which your expansion is valid. [1]

Total: 6



2. A curve has the equation

$$x^2 + 3xy - 2y^2 + 17 = 0.$$

(a) Find an expression for  $\frac{dy}{dx}$  in terms of  $x$  and  $y$ . [5]

(b) Find an equation for the normal to the curve at the point  $(3, -2)$ . [3]

Total: 8



3. (a) Find the values of the constants  $A, B, C$  and  $D$  such that

[5]

$$\frac{2x^3 - 5x^2 + 6}{x^2 - 3x} \equiv Ax + B + \frac{C}{x} + \frac{D}{x - 3}.$$

- (b) Evaluate

[5]

$$\int_1^2 \frac{2x^3 - 5x^2 + 6}{x^2 - 3x} dx,$$

giving your answer in the form  $p + q \ln(2)$ , where  $p$  and  $q$  are integers.

Total: 10



- She uses the model

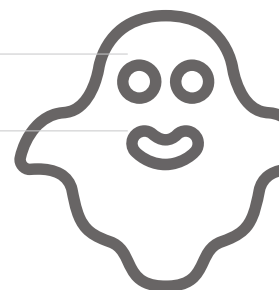
$$\frac{dx}{dt} = \frac{k(5-t)}{x},$$

Given that after two hours she has made sales of £96 in total,

- The mathematician believes that is it not worth staying at the sale once she is making sales at a rate of less than £10 per hour.

- (b) Verify that at 3 hours and 5 minutes after the start of the sale, she should have already left. [4]

Total: 12



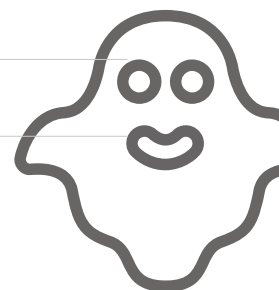
$$\mathbf{r} = \begin{pmatrix} 4 \\ 1 \\ 1 \end{pmatrix} + s \begin{pmatrix} 1 \\ 4 \\ 5 \end{pmatrix} \quad \text{and} \quad \mathbf{r} = \begin{pmatrix} -3 \\ 1 \\ -6 \end{pmatrix} + t \begin{pmatrix} 3 \\ a \\ b \end{pmatrix},$$

Given that the two lines are perpendicular,

- Given also that the two lines intersect,

- (c) find the coordinates of the point where they intersect. [2]

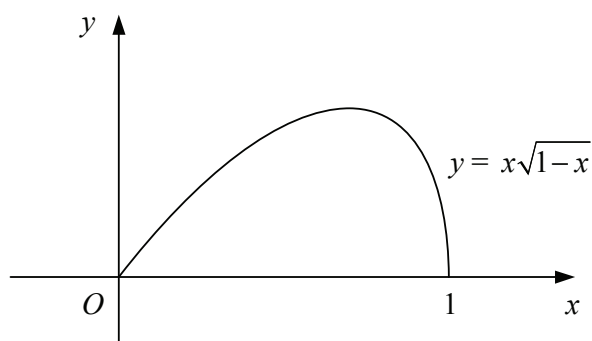
Total: 12





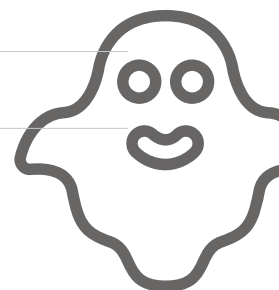
6. Figure shows the curve with equation

$$y = x\sqrt{1-x}, \quad 0 \leq x \leq 1.$$



- (a) Use the substitution  $u^2 = 1 - x$  to show that the area of the region bounded by the curve and the  $x$ -axis is  $\frac{4}{15}$ . [8]
- (b) Find, in terms of  $\pi$ , the volume of the solid formed when the region bounded by the curve and the  $x$ -axis is rotated through  $360^\circ$  about the  $x$ -axis. [5]

Total: 13







7. A curve has parametric equations

$$x = 3 \cos^2(t), \quad \text{and} \quad y = \sin(2t), \quad 0 \leq t < \pi.$$

(a) Show that [4]

$$\frac{dy}{dx} = -\frac{2}{3} \cot(2t).$$

(b) Find the coordinates of the points where the tangent to the curve is parallel to the  $x$ -axis. [3]

(c) Show that the tangent to the curve at the point where  $t = \frac{\pi}{6}$  has the equation [3]

$$2x + 3\sqrt{3}y = 9.$$

(d) Find a Cartesian equation for the curve in the form  $y^2 = f(x)$ . [4]

Total: 14



