

Solomon Practice Paper

Core Mathematics 3H

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	7	
3	7	
4	9	
5	10	
6	11	
7	12	
8	13	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025



1. The functions f and g are defined by

$$\begin{aligned} f: x &\rightarrow 2 - x^2, & x \in \mathbb{R}, \\ g: x &\rightarrow \frac{3x}{2x-1}, & x \in \mathbb{R}, x \neq \frac{1}{2}. \end{aligned}$$

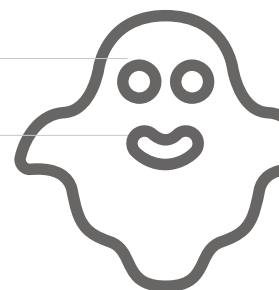
(a) Evaluate $fg(2)$.

[2]

(b) Solve the equation $gf(x) = \frac{1}{2}$.

[4]

Total: 6

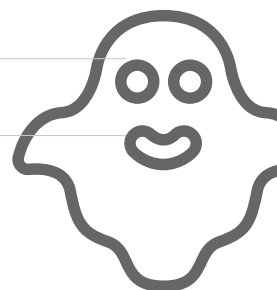


2. Giving your answers to 1 decimal place, solve the equation

[7]

$$5 \tan^2(2\theta) - 13 \sec(2\theta) = 1,$$

for θ in the interval $0 \leq \theta \leq 360^\circ$.



3. (a) Simplify

[3]

$$\frac{2x^2 + 3x - 9}{2x^2 - 7x + 6}.$$

(b) Solve the equation

[4]

$$\ln(2x^2 + 3x - 9) = 2 + \ln(2x^2 - 7x + 6),$$

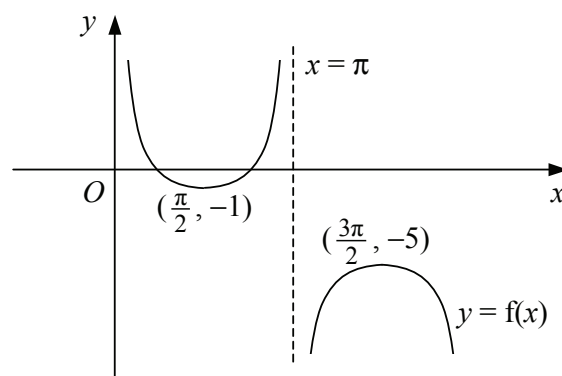
giving your answer in terms of e.

Total: 7





4. Figure shows the graph of $y = f(x)$.



The graph has a minimum at $(\frac{\pi}{2}, -1)$, a maximum at $(\frac{3\pi}{2}, -5)$ and an asymptote with equation $x = \pi$.

(a) Showing the coordinates of any stationary points, sketch the graph of $y = |f(x)|$. [3]

Given that

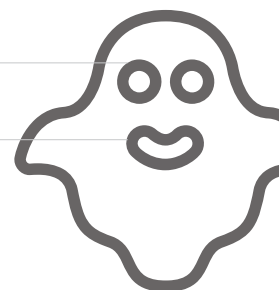
$$f: x \rightarrow a + b \csc(x), \quad x \in \mathbb{R}, 0 < x < 2\pi, x \neq \pi,$$

(b) find the values of the constants a and b , [3]

(c) find, to 2 decimal places, the x -coordinates of the points where the graph of $y = f(x)$ crosses the x -axis. [3]

Total: 9

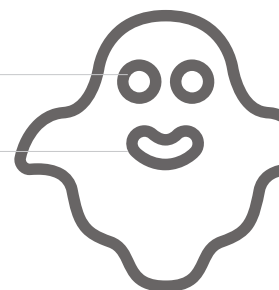




$$N = 2000e^{kt},$$

Given that when $t = 3$, $N = 18000$, find

- Total: 10





- [4]

The curve C has the equation

[4]

- [3]

Total: 11





7.

$f(x) = x^2 - 2x + 5, x \in \mathbb{R}, x \geq 1.$

- (a) Express $f(x)$ in the form $(x + a)^2 + b$, where a and b are constants. [2]
- (b) State the range of f . [1]
- (c) Find an expression for $f^{-1}(x)$. [3]
- (d) Describe fully two transformations that would map the graph of $y = f^{-1}(x)$ onto the graph of $y = \sqrt{x}, x \geq 0$. [2]
- (e) Find an equation for the normal to the curve $y = f^{-1}(x)$ at the point where $x = 8$. [4]

Total: 12





$$y = \frac{e^2}{x} + e^x, x \neq 0.$$

- The point A on the curve has x -coordinate 2.

- The tangent to the curve at A intersects the curve again at the point B .

$$x_{n+1} = -\frac{2}{3}\sqrt{3 + 3x_n e^{x_n-2}},$$

Total: 13

