

Solomon Practice Paper

Core Mathematics 3F

Time allowed: 90 minutes

Centre: www.CasperYC.club

Name:

Teacher:

Question	Points	Score
1	6	
2	7	
3	8	
4	8	
5	10	
6	11	
7	12	
8	13	
Total:	75	

How I can achieve better:

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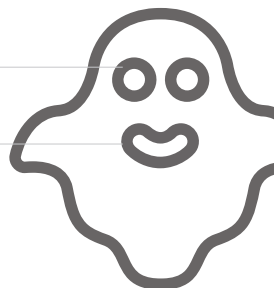


Last updated: July 14, 2025



[6]

for θ in the interval $0 \leq \theta \leq 180$, giving your answers to 1 decimal place.



$$\begin{aligned} \text{f: } & x \rightarrow 1 - ax, & x \in \mathbb{R}, \\ \text{g: } & x \rightarrow x^2 + 2ax + 2, & x \in \mathbb{R}, \end{aligned}$$

(a) Find the range of g in terms of a .

[3]

(b) find the two possible values of a .

[4]

Total: 7



3. (a) Solve the equation [3]

$$\ln(3x + 1) = 2$$

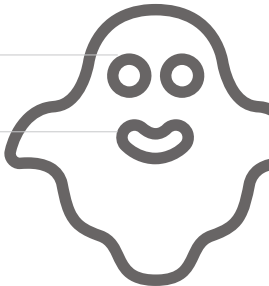
giving your answer in terms of e.

(b) Prove, by counter-example, that the statement [5]

$$\ln(3x^2 + 5x + 3) \geq 0 \text{ for all real values of } x$$

is false.

Total: 8



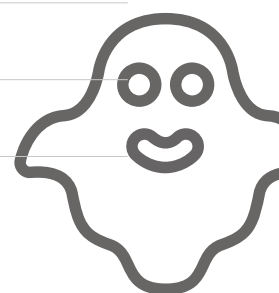
(a) Show that

$$\frac{dy}{dx} = \frac{\sqrt{1-2y}}{1-3y}.$$

(b) Show that the equation of tangent to the curve at A can be written in the form

$$\sqrt{3}x + py + q = 0$$

Total: 8



5. (a) Sketch the graph of

[5]

$$y = 2 + \sec \left(x - \frac{\pi}{6} \right)$$

for x in the interval $0 \leq x \leq 2\pi$.

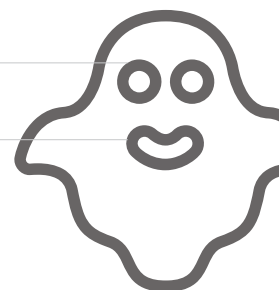
Show on your sketch the coordinates of any turning points and the equations of any asymptotes.

(b) Find, in terms of π , the x -coordinates of the points where the graph crosses the x -axis.

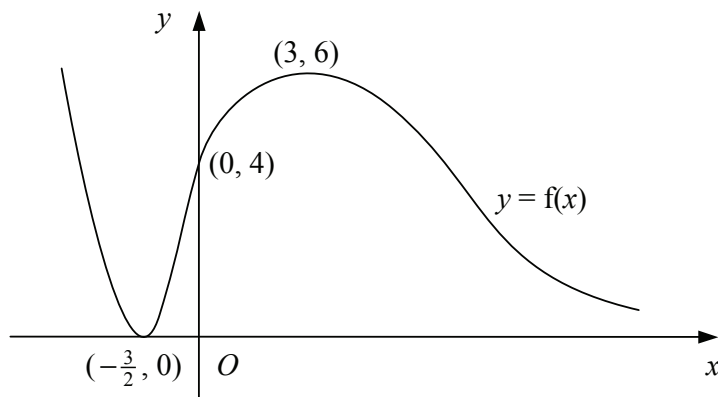
[5]

Total: 10





6. Figure shows the curve $y = f(x)$ which has a minimum point at $(-\frac{3}{2}, 0)$, a maximum point at $(3, 6)$ and crosses the y -axis at $(0, 4)$.



Sketch each of the following graphs on separate diagrams. In each case, show the coordinates of any turning points and of any points where the graph meets the coordinate axes.

- (a) $y = f(|x|)$ [3]
(b) $y = 2 + f(x + 3)$ [4]
(c) $y = \frac{1}{2}f(-x)$ [4]

Total: 11





7.

$$f(x) = 1 + \frac{4x}{2x - 5} - \frac{15}{2x^2 - 7x + 5}, x \in \mathbb{R}, x < 1.$$

(a) Show that

[5]

$$f(x) = \frac{3x + 2}{x - 1}.$$

(b) Find an expression for the inverse function $f^{-1}(x)$ and state its domain.

[5]

(c) Solve the equation $f(x) = 2$.

[2]

Total: 12





8. A curve has the equation $y = x^2 - \sqrt{4 + \ln(x)}$.

(a) Show that the tangent to the curve at the point where $x = 1$ has the equation [5]

$$7x - 4y = 11.$$

The curve has a stationary point with x -coordinate α .

(b) Show that $0.3 < \alpha < 0.4$. [3]

(c) Show that α is a solution of the equation [2]

$$x = \frac{1}{2} (4 + \ln(x))^{-\frac{1}{4}}$$

(d) Use the iteration formula [3]

$$x_{n+1} = \frac{1}{2} (4 + \ln(x_n))^{-\frac{1}{4}}$$

with $x_0 = 0.35$, to find x_1, x_2, x_3 and x_4 , giving your answers to 5 decimal places.

Total: 13



