

# Solomon Practice Paper

## Core Mathematics 3C

Time allowed: 90 minutes

Centre: [www.CasperYC.club](http://www.CasperYC.club)

Name:

Teacher:

Question	Points	Score
1	6	
2	7	
3	8	
4	8	
5	9	
6	10	
7	13	
8	14	
Total:	75	

How I can achieve better:

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Last updated: July 14, 2025



1. (a) Express

[3]

$$\frac{x+4}{2x^2+3x+1} - \frac{2}{2x+1}$$

as a single fraction in its simplest form.

(b) Hence, find the values of  $x$  such that

[3]

$$\frac{x+4}{2x^2+3x+1} - \frac{2}{2x+1} = \frac{1}{2}.$$

Total: 6



2. (a) Prove, by counter-example, that the statement

[2]

$$\csc(\theta) - \sin(\theta) > 0 \text{ for all values of } \theta \text{ in the interval } 0 < \theta < \pi$$

is false.

(b) Find the values of  $\theta$  in the interval  $0 < \theta < \pi$  such that

[5]

$$\csc(\theta) - \sin(\theta) = 2,$$

giving your answers to 2 decimal places.

Total: 7



3. Solve each equation, giving your answers in exact form.

(a)  $\ln(2x - 3) = 1$

[3]

(b)  $3e^y + 5e^{-y} = 16$

[5]

Total: 8



4. Differentiate each of the following with respect to  $x$  and simplify your answers.

(a)  $\ln(3x - 2)$

[2]

(b)  $\frac{2x+1}{1-x}$

[3]

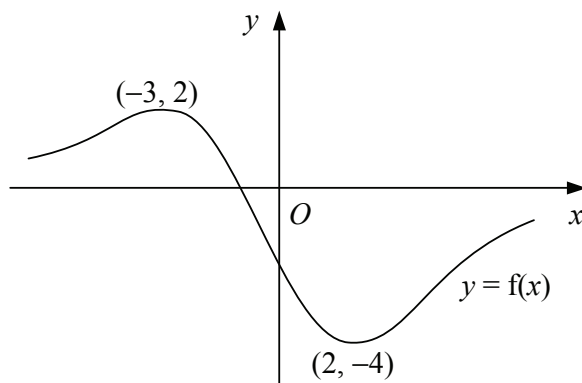
(c)  $x^{\frac{3}{2}}e^{2x}$

[3]

Total: 8

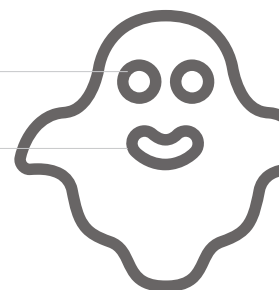


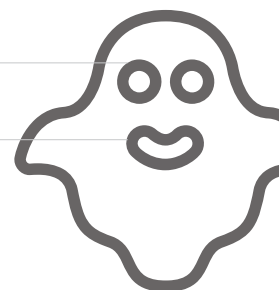
5. Figure shows the curve  $y = f(x)$  which has a maximum point at  $(-3, 2)$  and a minimum point at  $(2, -4)$ .



- (a) Showing the coordinates of any stationary points, sketch on separate diagrams the graphs of [7]
- i.  $y = f(|x|)$ ,
  - ii.  $y = 3f(2x)$ .
- (b) Write down the values of the constants  $a$  and  $b$  such that the curve with equation  $y = a + f(x + b)$  has a minimum point at the origin  $O$ . [2]

Total: 9





$$f(x) \equiv 4 - \ln(3x), x \in \mathbb{R}, x > 0.$$

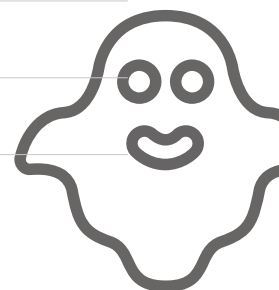
- The function  $g$  is defined by

$$g(x) \equiv e^{2-x}, x \in \mathbb{R}.$$

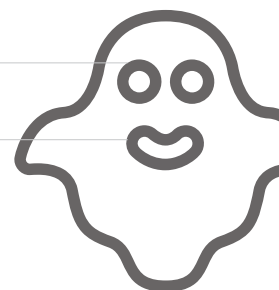
- $$\text{fg}(x) = x + a - \ln(b),$$

where  $a$  and  $b$  are integers to be found.

Total: 10







7. (a) Express  $4 \sin(x) + 3 \cos(x)$  in the form  $R \sin(x + \alpha)$  where  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$ . [4]
- (b) State the minimum value of  $4 \sin(x) + 3 \cos(x)$  and the smallest positive value of  $x$  for which this minimum value occurs. [3]
- (c) Solve the equation [6]

$$4 \sin(2\theta) + 3 \cos(2\theta) = 2,$$

for  $\theta$  in the interval  $0 \leq \theta \leq \pi$ , giving your answers to 2 decimal places.

Total: 13





8. The curve  $C$  has the equation  $y = \sqrt{x} + e^{1-4x}$ ,  $x \geq 0$ .

(a) Find an equation for the normal to the curve at the point  $(\frac{1}{4}, \frac{3}{2})$ . [4]

The curve  $C$  has a stationary point with  $x$ -coordinate  $\alpha$  where  $0.5 < \alpha < 1$ .

(b) Show that  $\alpha$  is a solution of the equation [3]

$$x = \frac{1}{4} [1 + \ln(8\sqrt{x})].$$

(c) Use the iteration formula [3]

$$x_{n+1} = \frac{1}{4} [1 + \ln(8\sqrt{x_n})],$$

with  $x_0 = 1$  to find  $x_1, x_2, x_3$  and  $x_4$ , giving the value of  $x_4$  to 3 decimal places.

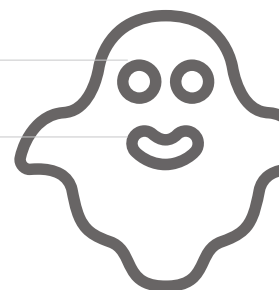
(d) Show that your value for  $x_4$  is the value of  $\alpha$  correct to 3 decimal places. [2]

(e) Another attempt to find  $\alpha$  is made using the iteration formula [2]

$$x_{n+1} = \frac{1}{64} e^{8x_n - 2},$$

with  $x_0 = 1$ . Describe the outcome of this attempt.

Total: 14



Lined area for writing answers, consisting of 20 horizontal lines.

