

Edexcel (U.K.) Pre 2017

Questions By Topic

C3 Chap06 07 Trigonometry

Compiled By: Dr Yu

Editors: Betül, Signal, Vivian

www.CasperYC.club

Last updated: February 7, 2026



DrYuFromShanghai@QQ.com

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6. (a) Using $\sin^2\theta + \cos^2\theta \equiv 1$, show that $\operatorname{cosec}^2\theta - \cot^2\theta \equiv 1$.

(2)

(b) Hence, or otherwise, prove that

$$\operatorname{cosec}^4\theta - \cot^4\theta \equiv \operatorname{cosec}^2\theta + \cot^2\theta.$$

(2)

(c) Solve, for $90^\circ < \theta < 180^\circ$,

$$\operatorname{cosec}^4\theta - \cot^4\theta = 2 - \cot \theta.$$

(6)

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8. (a) Given that $\cos A = \frac{3}{4}$, where $270^\circ < A < 360^\circ$, find the exact value of $\sin 2A$.

(5)

(b) (i) Show that $\cos\left(2x + \frac{\pi}{3}\right) + \cos\left(2x - \frac{\pi}{3}\right) \equiv \cos 2x$.

(3)

Given that

$$y = 3 \sin^2 x + \cos\left(2x + \frac{\pi}{3}\right) + \cos\left(2x - \frac{\pi}{3}\right),$$

(ii) show that $\frac{dy}{dx} = \sin 2x$.

(4)

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1. (a) By writing $\sin 3\theta$ as $\sin (2\theta + \theta)$, show that

$$\sin 3\theta = 3\sin \theta - 4\sin^3 \theta.$$

(5)

- (b) Given that $\sin \theta = \frac{\sqrt{3}}{4}$, find the exact value of $\sin 3\theta$.

(2)

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5.

Figure 1

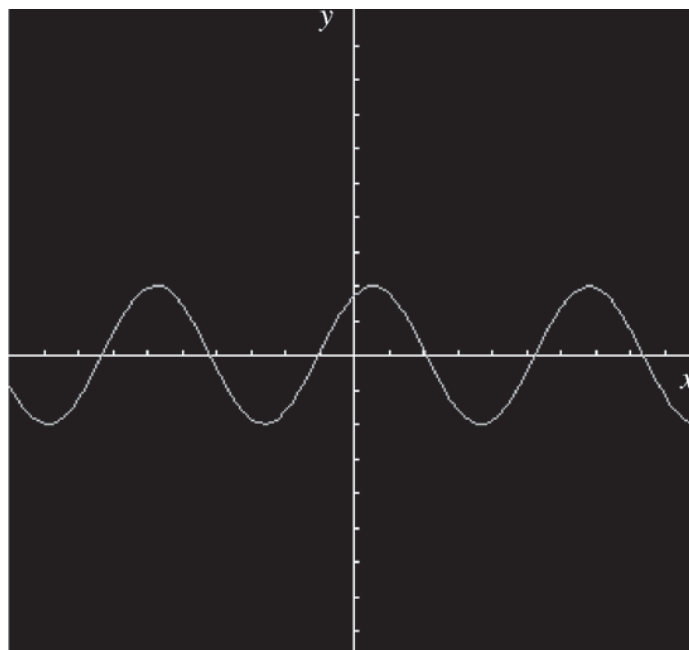


Figure 1 shows an oscilloscope screen.

The curve shown on the screen satisfies the equation

$$y = \sqrt{3} \cos x + \sin x.$$

- (a) Express the equation of the curve in the form $y = R \sin(x + \alpha)$, where R and α are constants, $R > 0$ and $0 < \alpha < \frac{\pi}{2}$.

(4)

- (b) Find the values of x , $0 \leq x < 2\pi$, for which $y = 1$.

(4)

6. (a) Express $3 \sin x + 2 \cos x$ in the form $R \sin(x + \alpha)$ where $R > 0$ and $0 < \alpha < \frac{\pi}{2}$. (4)

(c) Solve, for $0 < x < 2\pi$, the equation

giving your answers to 3 decimal places. (5)

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5. (a) Given that $\sin^2\theta + \cos^2\theta \equiv 1$, show that $1 + \cot^2\theta \equiv \operatorname{cosec}^2\theta$.

(2)

(b) Solve, for $0 \leq \theta < 180^\circ$, the equation

$$2 \cot^2\theta - 9 \operatorname{cosec}\theta = 3,$$

giving your answers to 1 decimal place.

(6)

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8. Solve

$$\operatorname{cosec}^2 2x - \cot 2x = 1$$

for $0 \leq x \leq 180^\circ$.

(7)

(6)

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blank

6. (a) Prove that

$$\frac{1}{\sin 2\theta} - \frac{\cos 2\theta}{\sin 2\theta} = \tan \theta, \quad \theta \neq 90n^\circ, \quad n \in \mathbb{Z} \quad (4)$$

(b) Hence, or otherwise,

$$(i) \text{ show that } \tan 15^\circ = 2 - \sqrt{3}, \quad (3)$$

(ii) solve, for $0 < x < 360^\circ$,

$$\operatorname{cosec} 4x - \cot 4x = 1 \quad (5)$$

(10)

8. $f(x) = 7 \cos 2x - 24 \sin 2x$

(a) find the value of R and the value of α . (3)

for $0 \leq x < 180^\circ$, giving your answers to 1 decimal place. (5)

(c) Express $14\cos^2 x - 48\sin x \cos x$ in the form $a\cos 2x + b\sin 2x + c$, where a , b , and c are constants to be found.

$$14\cos^2 x - 48\sin x \cos x \quad (2)$$

8.

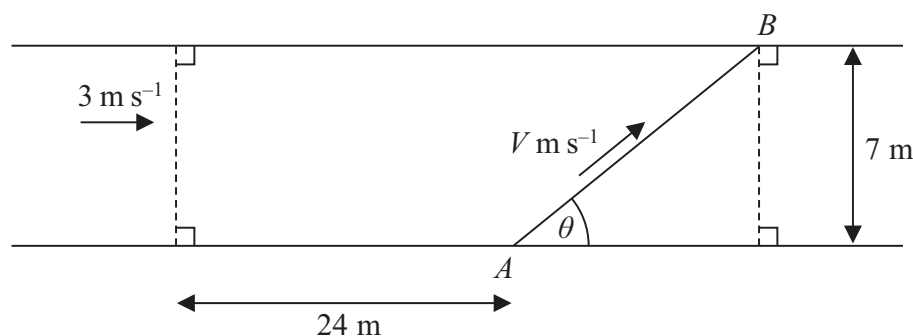


Figure 2

Kate crosses a road, of constant width 7 m, in order to take a photograph of a marathon runner, John, approaching at 3 m s^{-1} .

Kate is 24 m ahead of John when she starts to cross the road from the fixed point A .

John passes her as she reaches the other side of the road at a variable point B , as shown in Figure 2.

Kate's speed is $V \text{ m s}^{-1}$ and she moves in a straight line, which makes an angle θ , $0 < \theta < 150^\circ$, with the edge of the road, as shown in Figure 2.

You may assume that V is given by the formula

$$V = \frac{21}{24 \sin \theta + 7 \cos \theta}, \quad 0 < \theta < 150^\circ$$

- (a) Express $24 \sin \theta + 7 \cos \theta$ in the form $R \cos(\theta - \alpha)$, where R and α are constants and where $R > 0$ and $0 < \alpha < 90^\circ$, giving the value of α to 2 decimal places.

(3)

Given that θ varies,

- (b) find the minimum value of V .

(2)

Given that Kate's speed has the value found in part (b),

- (c) find the distance AB .

(3)

Given instead that Kate's speed is 1.68 m s^{-1} ,

- (d) find the two possible values of the angle θ , given that $0 < \theta < 150^\circ$.

(6)

3. $f(x) = 7\cos x + \sin x$

(a) find the exact value of R and the value of α to one decimal place.

(3)

$$7\cos x + \sin x = 5$$

for $0 \leq x < 360^\circ$, giving your answers to one decimal place.

(5)

$$7\cos x + \sin x = k$$

has only one solution in the interval $0 \leq x < 360^\circ$

(2)

