

Edexcel (U.K.) Pre 2017

Questions By Topic

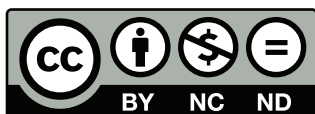
C3 Chap03 Exponentials and Logarithms

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7. A particular species of orchid is being studied. The population p at time t years after the study started is assumed to be

$$p = \frac{2800ae^{0.2t}}{1 + ae^{0.2t}}, \text{ where } a \text{ is a constant.}$$

Given that there were 300 orchids when the study started,

- (a) show that $a = 0.12$,
- (3)**

- (b) use the equation with $a = 0.12$ to predict the number of years before the population of orchids reaches 1850. (4)

- (c) Show that $p = \frac{336}{0.12 + e^{-0.2t}}$. (1)

- (d) Hence show that the population cannot exceed 2800. (2)

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1. Find the exact solutions to the equations

(a) $\ln x + \ln 3 = \ln 6$,

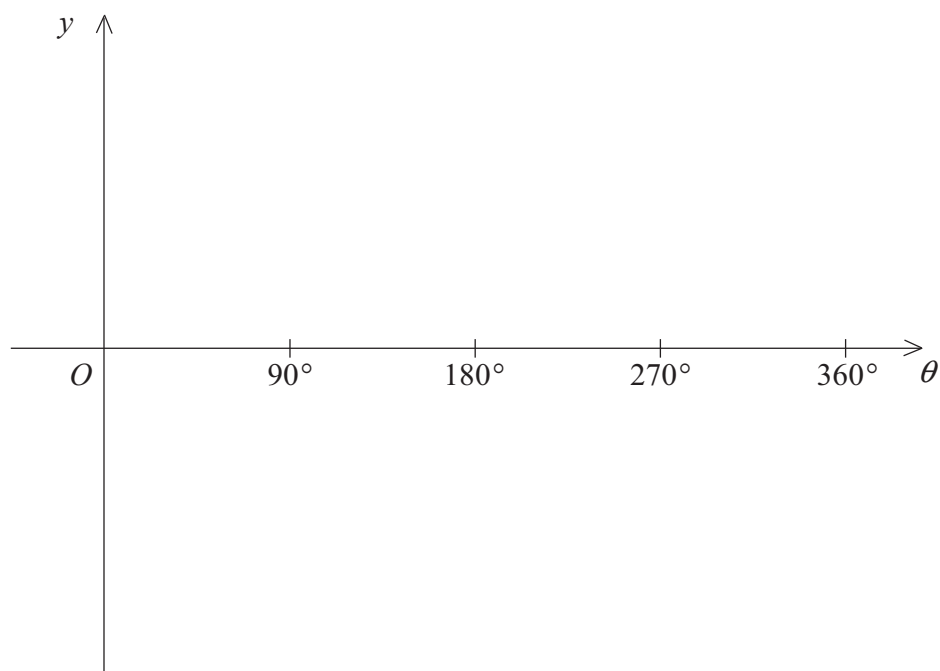
(2)

(b) $e^x + 3e^{-x} = 4$.

(4)

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Question 7 continued



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5.

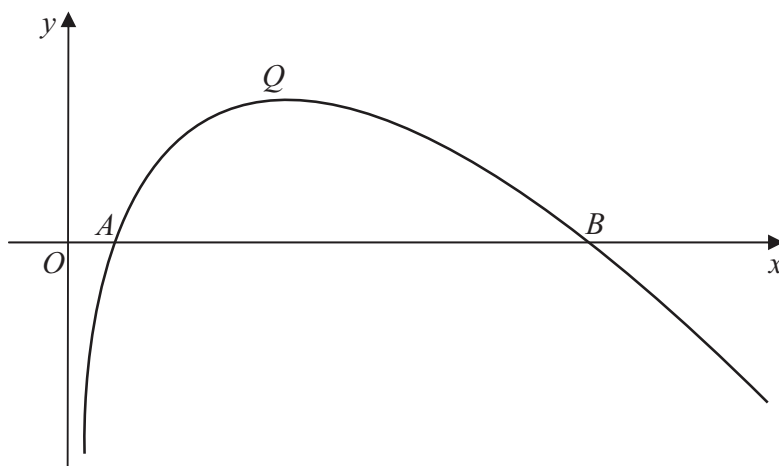
**Figure 1**

Figure 1 shows a sketch of part of the curve with equation $y = f(x)$, where

$$f(x) = (8 - x) \ln x, \quad x > 0$$

The curve cuts the x -axis at the points A and B and has a maximum turning point at Q , as shown in Figure 1.

- (a) Write down the coordinates of A and the coordinates of B .

(2)

- (b) Find $f'(x)$.

(3)

- (c) Show that the x -coordinate of Q lies between 3.5 and 3.6

(2)

- (d) Show that the x -coordinate of Q is the solution of

$$x = \frac{8}{1 + \ln x}$$

(3)

To find an approximation for the x -coordinate of Q , the iteration formula

$$x_{n+1} = \frac{8}{1 + \ln x_n}$$

is used.

- (e) Taking $x_0 = 3.55$, find the values of x_1 , x_2 and x_3 .
Give your answers to 3 decimal places.

(3)

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6. Find algebraically the exact solutions to the equations

(a) $\ln(4 - 2x) + \ln(9 - 3x) = 2\ln(x + 1)$, $-1 < x < 2$

(5)

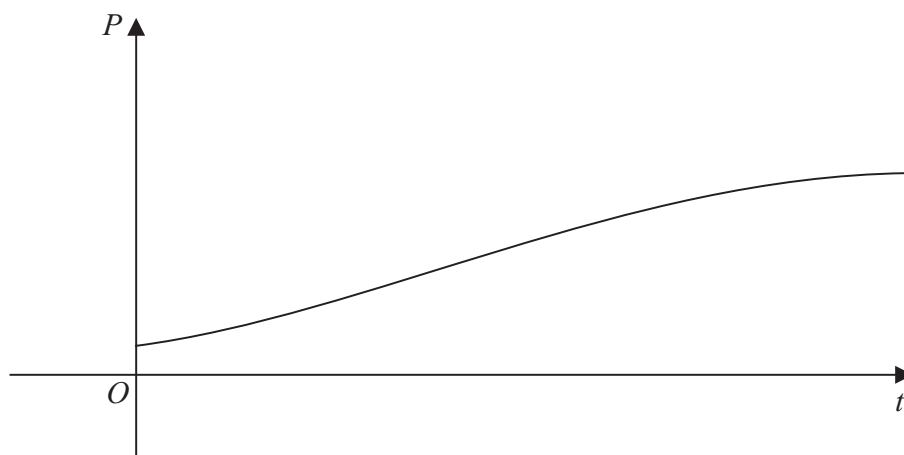
(b) $2^x e^{3x+1} = 10$

Give your answer to (b) in the form $\frac{a + \ln b}{c + \ln d}$ where a , b , c and d are integers.

(5)

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8.

**Figure 3**

The population of a town is being studied. The population P , at time t years from the start of the study, is assumed to be

$$P = \frac{8000}{1 + 7e^{-kt}}, \quad t \geq 0,$$

where k is a positive constant.

The graph of P against t is shown in Figure 3.

Use the given equation to

(a) find the population at the start of the study, (2)

(b) find a value for the expected upper limit of the population. (1)

Given also that the population reaches 2500 at 3 years from the start of the study,

(c) calculate the value of k to 3 decimal places. (5)

Using this value for k ,

(d) find the population at 10 years from the start of the study, giving your answer to 3 significant figures. (2)

(e) Find, using $\frac{dP}{dt}$, the rate at which the population is growing at 10 years from the start of the study. (3)