

Question Number	Scheme				Marks
1	H_0 : The aptitude test result is independent of the test centre H_1 : The aptitude test result is not independent of the test centre				B1
	Observed	Pass	Fail	Total	
	Centre A	60	30	90	M1
	Centre B	80	30	110	
	Total	140	60	200	
	Expected	Pass	Fail		
	Centre A	$\frac{140 \times 90}{200} [= 63]$	$\frac{60 \times 90}{200} [= 27]$		M1
	Centre B	$\frac{140 \times 110}{200} [= 77]$	$\frac{60 \times 110}{200} [= 33]$		
	$\sum \frac{(O-E)^2}{E} = \frac{(60-63)^2}{63} + \frac{(80-77)^2}{77} + \frac{(30-27)^2}{27} + \frac{(30-33)^2}{33}$ or $\sum \frac{O^2}{E} - 200 = \frac{60^2}{63} + \frac{80^2}{77} + \frac{30^2}{27} + \frac{30^2}{33} - 200$				dM1
	= 0.8658...				awrt 0.866
$\nu = (2-1)(2-1) = 1$					B1
$\chi^2(0.05) = 3.841$					B1ft
[Do not reject H_0 /not significant/not in the CR] There is insufficient evidence that aptitude test <u>result</u> differs by test <u>centre</u>					dA1ft
					(8)
Notes				Total 8	
B1	both hypotheses correct with result and centre (Condone aptitude test and test centre). May be written in terms of association				
M1	for a correct contingency table. May be implied by awrt 0.866				
M1	attempt at $\frac{\text{row total} \times \text{column total}}{\text{total}}$ (can be implied by at least one correct expected value)				
dM1	dependent on previous M1. For using $\sum \frac{(O-E)^2}{E}$ or $\sum \frac{O^2}{E} - 200$ (There must be 4 values of $\sum \frac{(O-E)^2}{E}$ or $\sum \frac{O^2}{E}$ calculated)				
A1	awrt 0.866				
B1	$\nu = 1$				
B1ft	3.841 (or better) allow ft from their stated degrees of freedom				
dA1ft	dependent on 3 rd M1 and 3 rd B1. For a correct contextual conclusion. Must include result and centre. (Condone aptitude test and test centre)				

Question Number	Scheme		Marks
2 (a)	$H_0 : \rho_s = 0$ $H_1 : \rho_s > 0$		B1
			(1)
(b)	$[r_s =]1 - \frac{6\sum d^2}{5(24)} \geq 0.9$		M1 B1
	$\sum d^2 \leq 2$ So largest possible value is 2*		A1*
			(3)
(c)	e.g. $d = 0, 0, 0, 1, -1$		M1
	So e.g. $A B C E D$		A1
			(2)
Notes			Total 6
(a)	B1	for both hypotheses correct in terms of ρ or ρ_s . Condone use of p	
(b)	M1	for use of formula for r in an equation or an inequality (condone $>$ rather than \geq)	
	B1	for 0.9	
	A1*	answer is given so at least one correct line of working is needed between the M mark and the given answer. Allow $\sum d^2 = 2$ if written as an equation throughout but do not allow $\sum d^2 \geq 2$ or $\sum d^2 > 2$ or $\sum d^2 < 2$	
(c)	M1	for a correct possibility for d or $ d $ May be implied by a correct possibility for rankings	
	A1	for a correct possibility for rankings or eg 1, 2, 3, 5, 4	

Question Number	Scheme		Marks
3 (a)	$\bar{x} = \left[\frac{509.1572 + 510.8428}{2} \right] = 510$		B1
	$2 \times 1.96 \times \frac{\sigma}{\sqrt{n}} = 510.8428 - 509.1572$		M1
	$\frac{\sigma}{\sqrt{n}} = 0.43$		A1
	'510' ± 1.6449 × '0.43'		M1 B1
	(509.292..., 510.707...)		(awrt 509.3, awrt 510.7) A1
			(6)
(b)	Let $X =$ The number of confidence intervals containing μ so $X \sim B(3, 0.9)$		
	$P(X \geq 1) = 1 - P(X = 0) = 1 - [{}^3C_0 \times 0.9^0] \times 0.1^3$		M1
	$= 0.999$		A1
			(2)
Notes			Total 8
(a)	B1	for $\bar{x} = 510$	
	M1	for use of $2 \times z$ value $\times \frac{\sigma}{\sqrt{n}} = 510.8428 - 509.1572$ oe	
	A1	Cao	
	M1	for use of $\bar{x} \pm z$ value $\times \frac{\sigma}{\sqrt{n}}$ ft their \bar{x} and their $\frac{\sigma}{\sqrt{n}}$	
	B1	$z = 1.96$ or better and $z = 1.6449$ or better	
	A1	(awrt 509.3, awrt 510.7)	
(b)	M1	for writing or using $P(X \geq 1) = 1 - P(X = 0)$ or $P(X = 1) + P(X = 2) + P(X = 3)$	
	A1	Cao	

Question Number	Scheme		Marks
4 (a)	$\frac{273}{150 \times 10} = 0.18$		M1 A1
			(2)
(b)	${}^{10}C_5 \times 0.18^5 \times 0.82^5 \times 150 [= 2.65] *$		B1*
			(1)
(c)	0.54		B1
			(1)
(d)	To ensure that no expected frequency < 5		B1
			(1)
(e)	H ₀ : Binomial distribution is a good fit. H ₁ : Binomial distribution is not a good fit		B1
	Combine cells 8 + 6 + 3 = 17 and 10.05 + 2.65 + '0.54' = 13.24		M1
	$\sum \frac{(O_i - E_i)^2}{E_i} = 2.51 + \frac{(17 - 13.24)^2}{13.24}$		M1
	= 3.5777		awrt 3.58 A1
	$\nu = 5 - 1 - 1 = 3$		B1
	$\chi^2_3(0.05) = 6.251$		B1ft
	[Do not reject H ₀ /not significant] Binomial distribution is a suitable model		dA1
			(7)
Notes			Total 12
(a)	M1	for a correct method to find the value of p	
	A1	Awrt 0.18	
(b)	B1*	for a correct expression for r	
(c)	B1	for 0.54	
(d)	B1	for a correct explanation	
(e)	B1	for both hypotheses correct (any mention of B(10, p) is B0)	
	M1	for combining cells	
	M1	Dep on an attempt to combine cells. Use of $2.51 + \sum \frac{(O_i - E_i)^2}{E_i}$ for remaining cells	
	A1	awrt 3.58	
	B1	$\nu = 3$	
	B1ft	6.251 or better. Allow ft from their stated DoF	
	dA1	dependent on 2 nd M1. For a correct conclusion which states that the data are consistent with a binomial distribution which must be consistent with the test statistic and CV (Condone any mention of n and p or it supports the managers belief)	

Question Number	Scheme		Marks
5 (a)	$\left[m = \frac{3085}{50} \Rightarrow m = 61.7 \right]$		B1
	$v = \frac{190457.2 - 50(61.7)^2}{50-1} = 2.3$		M1 A1
			(3)
(b)	$H_0: \mu_A - \mu_B = 10$ $H_1: \mu_A - \mu_B > 10$		B1
	$z = \frac{72.2 - '61.7' - 10}{\sqrt{\frac{6.4}{50} + \frac{'2.3'}{50}}}$		M1 M1
	= 1.1986... awrt 1.20		A1
	One tailed c.v. $Z = 1.6449$ or CR: $Z \geq 1.6449$		B1
	Not in CR/Not significant/Do not reject H_0		M1
	No significant evidence to support the head of department's claim		A1
			(7)
(c)	Assume that $s^2 = \sigma^2$ for both samples		B1
	Assume sample sizes are large enough so that CLT applies or the CLT allows us to assume that the distributions of the sample means are (approximately) normal		B1
			(2)
Notes			Total 12
(a)	B1	Cao	
	M1	for a full attempt at s^2 ft their \bar{x}	
	A1	Cao	
(b)	B1	for both hypotheses correct in terms of μ_A and μ_B . Allow equivalent rearrangements. Allow other letters as long it is clear which is professor A and which is professor B. Must be attached to H_0 and H_1	
	M1	for $z = \frac{a-b-10}{\sqrt{\frac{c}{50} + \frac{d}{50}}}$ with at least 2 of a, b, c or d correct (allow \pm) ft their 61.7 and their 2.3	
	M1	for $z = \frac{72.2 - '61.7' - 10}{\sqrt{\frac{6.4}{50} + \frac{'2.3'}{50}}}$ (allow \pm) ft their 61.7 and their 2.3	
	A1	awrt 1.20	
	B1	for CV = ± 1.6449 and compatible sign with their test statistic	
	M1	for correct statement consistent with their test statistic and CV (no contradictory non-contextual comments) May be implied by correct contextual comment on its own	
	A1	for a contextual conclusion that is consistent with their test statistic and their CV. Must mention head of department's claim	
(c)	B1	for one correct assumption. Must mention both samples.	
	B1	for a second correct assumption. Must mention both samples.	

Question Number	Scheme		Marks
6 (a)	$\left[P(\bar{H} < 55.08) = 0.1151 \right] \Rightarrow \frac{55.08 - \mu}{\frac{6}{\sqrt{n}}} = -1.20$		M1
	$55.08 + \frac{7.2}{\sqrt{n}} = \mu$		A1
	$\left[P(\bar{H} > 56.976) = 0.0250 \right] \Rightarrow \frac{56.976 - \mu}{\frac{6}{\sqrt{n}}} = 1.96$		M1
	$56.976 - \frac{11.76}{\sqrt{n}} = \mu$		A1
	$55.08 + \frac{7.2}{\sqrt{n}} = 56.976 - \frac{11.76}{\sqrt{n}}$		M1
	Either $\frac{18.96}{\sqrt{n}} = 1.896$ or $\sqrt{n} = 10$ leading to $n = 100^*$		A1*
			(6)
(b)	$\mu = 55.08 + \frac{7.2}{\sqrt{10}} = 55.8$ or $\mu = 56.976 - \frac{11.76}{\sqrt{10}} = 55.8$		M1 A1
Notes			Total 8
(a)	M1	for standardising with μ and $\frac{6}{\sqrt{n}}$ and setting = to ± 1.2	
	A1	for a correct equation	
	M1	for standardising with μ and $\frac{6}{\sqrt{n}}$ and setting = to ± 1.96	
	A1	for a correct equation	
	M1	for solving simultaneously	
	A1*	for a correct equation leading to the given answer	
(b)	M1	substitution of $n = 10$ into an equation to find μ	
	A1	Cao	

Question Number	Scheme		Marks
7 (a)	$E(\bar{X}) = \frac{(a-1)+(a+5)}{2} = a+2$		M1 A1
	So $\bar{X} - 2$ is an unbiased estimator for a		A1
			(3)
(b)	$SE(\bar{X} - 2) = SE(\bar{X})$		B1ft
	$Var(X) = \frac{((a+5)-(a-1))^2}{12} = 3$		M1 A1
	$SE = \frac{s}{\sqrt{n}} = \frac{\sqrt{3}}{3} = 0.57735\dots$	awrt 0.577	M1 A1
		(5)	
Notes			Total 8
(a)	M1	for use of $\frac{a+b}{2}$	
	A1	for $a+2$	
	A1	Cao	
(b)	B1ft	for $SE(\bar{X} - 2) = SE(\bar{X})$ ft their unbiased estimator in part (a) May be implied by awrt 0.577	
	M1	for use of $\frac{(b-a)^2}{12}$	
	A1	Cao	
	M1	for use of $\frac{s}{\sqrt{n}}$	
	A1	awrt 0.577	

Question Number	Scheme		Marks
8 (a)	[a =]625 + 625 - 886 =]364		B1
	[b =]42 ² + 42 ² + 45 ² = 5553		M1 A1
			(3)
(b)	$X = L - 3S$		
	[E(X) = 886 - 3 × 265 =]91		M1
	[Var(X) =]45 ² + 3 ² × 78 ² = 56781		M1 A1
	[P(X > 0) =]P $\left(Z > \frac{0 - 91}{\sqrt{56781}}\right)$		M1
	[P(Z > -0.38) =]0.6480 Cal gives 0.64865... So awrt 0.648 - 0.649		A1
		(5)	
(c)	$Y = \frac{S_1 - S_2}{2}$	$R = S_1 - S_2$	M1
	$\left[E(Y) = \frac{265 - 265}{2} =\right]0$	$[E(R) = 265 - 265 =]0$	M1
	$[\text{Var}(Y) =] \frac{78^2 + 78^2}{4} = 3042$	$[\text{Var}(R) =]78^2 + 78^2 = 12168$	M1
	$[P(Y > 100) =]P\left(Z > \frac{100 - 0}{\sqrt{3042}}\right)$	$[P(R > 200) =]P\left(Z > \frac{200 - 0}{\sqrt{12168}}\right)$	M1
	[P(Z > 1.81) = 1 - 0.9649 =]0.0351 Cal gives 0.0349 So awrt 0.0349 - 0.0351		A1
			(5)
Notes			Total 13
(a)	B1	Cao	
	M1	For writing or using $2 \times \text{Var}(M) + \text{Var}(L)$	
	A1	Cao	
(b)	M1	for seeing or using $E(X) = 91$ or correct expression for mean	
	M1	for writing or using $\text{Var}(L) + 3^2 \text{Var}(S)$	
	A1	Cao	
	M1	for standardising using their mean and standard deviation (Allow \pm)	
	A1	awrt 0.648 - awrt 0.649	
(c)	M1	for use of $\frac{S_1 - S_2}{2}$ or $S_1 - S_2$	
	M1	for writing or using $E(Y) = 0$ or $E(R) = 0$	
	M1	for using $\text{Var}(Y) = 3042$ or $\text{Var}(R) = 12168$	
	M1	for standardising using their mean and standard deviation (Allow \pm)	
	A1	awrt 0.0349 - awrt 0.0351	