

Question Number	Scheme	Notes	Marks																														
1(a)	<table border="1"> <tr> <td></td> <td><i>A</i></td> <td><i>B</i></td> <td><i>C</i></td> <td><i>D</i></td> <td><i>E</i></td> </tr> <tr> <td><i>C</i></td> <td>3</td> <td>2</td> <td>1</td> <td>5</td> <td>4</td> </tr> <tr> <td><i>M</i></td> <td>2</td> <td>4</td> <td>1</td> <td>5</td> <td>3</td> </tr> <tr> <td><i>d</i></td> <td>1</td> <td>-2</td> <td>0</td> <td>0</td> <td>1</td> </tr> <tr> <td><i>d</i><sup>2</sup></td> <td>1</td> <td>4</td> <td>0</td> <td>0</td> <td>1</td> </tr> </table>		<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>	<i>C</i>	3	2	1	5	4	<i>M</i>	2	4	1	5	3	<i>d</i>	1	-2	0	0	1	<i>d</i> <sup>2</sup>	1	4	0	0	1	Attempt to rank at least 1 row with at least 3 correct. Allow reverse rankings.	M1
			<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>																										
<i>C</i>	3	2	1	5	4																												
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<i>d</i>	1	-2	0	0	1																												
<i>d</i> <sup>2</sup>	1	4	0	0	1																												
		Attempt at $d^2$ for their <b>rankings</b> , can be implied by $\sum d^2 = 6$	M1																														
	$\sum d^2 = 6$	Can be implied by correct answer. Must come from correct rankings.	A1																														
	$r_s = 1 - \frac{6(6)}{5(24)}$	(dep on 1 <sup>st</sup> M1) Use of correct formula with their $\sum d^2$	dM1																														
	$r_s = 0.7$	0.7 o.e. Must come from correct rankings.	A1																														
			(5)																														
1(b)	$H_0 : \rho = 0, H_1 : \rho > 0$	Both correct in terms of $\rho$ or $\rho_s$ . Must be compatible with their ranking.	B1																														
	cv 0.9 or cr $r_s \geq 0.9$	0.9 sign should match $H_1$ or their $r_s$	B1																														
	$r_s = 0.7$ does not lie in cr so do not reject $H_0$	Correct non-contextual statement e.g. “do not reject $H_0$ ”, “not in critical region”, “not significant”, “no positive correlation”. $ \text{test value} $ or $ \text{cv}  > 1$ award M0	M1																														
	Data does not support plant <b>biologist’s claim</b> .	Correct conclusion in context. Must mention “biologist’s claim” o.e. or <b>moisture and plant coverage</b> . All previous marks in (b) must have been scored.	A1ft																														
SC	For use of two-tailed test: May score B0B1M1A0 for cv = 1(.000) and ‘not significant’ oe																																
			(4)																														
			<b>Total 9</b>																														

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2	$H_0$ : Diet and health are independent (or not associated). $H_1$ : Diet and health are not independent (or associated).	“diet” and “health” mentioned at least once. Use of correlation is B0.	B1																								
	<table border="1"> <thead> <tr> <th>EXPECTED</th> <th>Good health</th> <th>Poor health</th> <th>Totals</th> </tr> </thead> <tbody> <tr> <td>Good diet</td> <td>83.19</td> <td>10.81</td> <td>94</td> </tr> <tr> <td>Poor diet</td> <td>93.81</td> <td>12.19</td> <td>106</td> </tr> <tr> <td>Totals</td> <td>177</td> <td>23</td> <td>200</td> </tr> </tbody> </table>	EXPECTED	Good health	Poor health	Totals	Good diet	83.19	10.81	94	Poor diet	93.81	12.19	106	Totals	177	23	200	Attempt $\frac{RT \times CT}{GT}$ with at least one correct to 1dp; all correct to 1dp.	M1; A1								
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Totals		1.557	201.557																								
	$\sum \frac{(O-E)^2}{E} \text{ or } \sum \frac{O^2}{E} - 200 = 1.557$	awrt 1.6	A1																								
	$\nu = (2-1)(2-1) = 1$ $\chi_1^2(5\%) = 3.841$	1 (may be implied) 3.841 NB: may see $\chi_3^2(5\%) = 7.815$ for f.t. NB: $p$ -value 0.212 but scores B0B0 on its own	B1 B1f.t.																								
	$\chi^2 = 1.557$ does not lie in cr so insufficient evidence to reject $H_0$	For correct non-contextual statement linking their test statistic and their cv.	M1																								
	E.g. Diet and health are independent <b>or</b> There is no association between diet and health <b>or</b> The doctor’s belief is not supported by this data.	Dependent on a cv of 3.841 and 3 <sup>rd</sup> M1 Correct conclusion in context with “diet” and “health” or “doctor”. Condone “connection” or “relationship” but not “correlation”.	A1ft																								
			(9)																								
			<b>Total 9</b>																								

Question Number	Scheme	Notes	Marks
<b>3.</b>			
<b>3(a)</b>	$\bar{x} = \frac{1}{2}(11.52 + 13.75) = 12.635$	12.635 (may be implied by correct CI)	B1
		Use of 1.96	B1
	$\left(\frac{\sigma}{\sqrt{n}} = \frac{13.75 - 12.635}{1.96} (= 0.56887\dots)\right)$ $\left(\frac{\sigma}{\sqrt{n}} = \frac{13.75 - 11.52}{2 \times 1.96} (= 0.56887\dots)\right)$	For attempt at standard error (may be implied by awrt 0.569)	M1
		Use of 1.6449 or better (1.644853... from calc) Use of 1.64 or 1.65 is B0	B1
	$12.635 \pm 1.6449 \times 0.56887\dots$	For $(\text{their } \bar{x}) \pm (\text{their } 1.6449) \left( \text{their } \frac{\sigma}{\sqrt{n}} \right)$ their $\frac{\sigma}{\sqrt{n}}$ must be numerical	M1
	90% CI is (11.699..., 13.5707...)	awrt (11.7, 13.6) from correct working Correct answer with no working scores B1B1M1B0M1A1	A1
			(6)
<b>3(b)</b>	$4 \times 0.9^3 \times 0.1$ $= 0.2916$	$4p^3(1-p)$ (where $0 < p < 1$ ) awrt 0.292	M1 A1
			(2)
			<b>Total 8</b>

Question Number	Scheme	Notes	Marks
4. (a)	Label academic (1-1680) and vocational (1-2520)	For numbering/labelling/ordering (o.e.) students in <b>each</b> group	B1
	Use <b>random</b> numbers to select from each group.	For use of random sample/numbers/selection	B1
	28 academic and 42 vocational	Both numbers correct with the associated group	B1
			(3)
4(b)	$H_0 : \mu_v - \mu_a = 0$ $H_1 : \mu_v - \mu_a > 0$	If the hypotheses are given in terms of $\mu_a - \mu_b$ , $a$ and $b$ must be defined.	B1
	$se = \sqrt{\frac{70}{80} + \frac{60}{50}}$	Correct attempt at se – condone slip in sample sizes.	M1
	$z = \frac{62 - 57}{\sqrt{\frac{70}{80} + \frac{60}{50}}}$	Dep on previous M1 standardising with (62 – 57) and their se (Allow $\pm$ )	dM1
	$z = 3.471...$ (or probability of 0.0003)	awrt $\pm 3.47$ (or awrt 0.0003)	A1
	cv $z = 1.6449$	Allow $\pm$ but signs must be compatible Or allow comparison with probability of 0.05	B1
	Reject $H_0$ / significant	Dependent on 2 <sup>nd</sup> M1. A correct non-contextual statement based on their <b>normal</b> cv and their test statistic.	dM1
	There is evidence that the <b>mean(o.e.)</b> basic skills score for <b>vocational</b> students is greater than the <b>mean</b> basic skills score for <b>academic</b> students.	Correct comment in context. Must mention “mean”, “academic” and “vocational”. Allow f.t. on their normal cv and their test statistic.	A1f.t.
			(7)
4(c)	Mean / $\bar{X}_a$ (basic skills) score for academic students and mean/ $\bar{X}_v$ (basic skills) score for vocational students...	Must mention <b>both</b> means.	B1
	...have (approximately) a normal distribution (as sample sizes are large.)	Must mention normal.	B1
			(2)
4(d)	Samples are (large enough) so that $s^2 = \sigma^2$	Must imply for both samples	B1
			(1)
4(e)	Test no longer significant so insufficient evidence to reject $H_0$	Can be implied by correct comment in context.	M1
	Insufficient evidence that mean (basic skills) <b>score</b> for vocational students is greater than the mean (basic skills) <b>score</b> for academic students/There is no longer a difference in <b>scores</b> /Academic students have improved their mean (basic skills) <b>score</b> .	Must mention scores (o.e).	A1
			(2)
4(f)	The course was <b>effective</b> (o.e.)	Dep on a significant result in (b) and a non-significant result in (e)	B1
			(1)
			<b>Total 16</b>

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5.(a)	Relief of symptoms is either a “success” or a “failure”. The probability the medicine being a success is constant. Samples from different medical practices are independent.	Any 2. Context required in one assumption.	B1 B1																														
			(2)																														
5(b)	Mean = $\frac{0 \times 4 + 1 \times 6 + 2 \times 3 + \dots + 8 \times 2}{50} = 3.54^*$	At least two correct terms on the numerator and 50 on the denominator, fully correct expression or $\frac{177}{50}$ dep on M1 scored cso.	M1, A1cso																														
			(2)																														
5(c)	$p = \frac{3.54}{8} = 0.4425$	Can be implied by at least 1 correct value for $f$ or $g$ .	B1																														
	$f = 50 \times C_4^8 \times 0.4425^4 \times 0.5575^4 = 12.96$ $g = 50 \times 0.4425^8 = 0.07$	Use of Bin(50, $p$ ) for M1, Allow awrt 12.96, awrt 0.07	M1A1A1																														
			(4)																														
5(d)	$H_0$ : Binomial distribution is a suitable model $H_1$ : Binomial distribution is not a suitable model	Both hypotheses correct If parameters used then B0.	B1																														
	<table border="1"> <thead> <tr> <th>No of successes</th> <th><math>O</math></th> <th><math>E</math></th> <th><math>\frac{(O-E)^2}{E}</math></th> <th><math>\frac{O^2}{E}</math></th> </tr> </thead> <tbody> <tr> <td>0,1,2</td> <td>13</td> <td>11.66</td> <td>0.154</td> <td>14.494</td> </tr> <tr> <td>3</td> <td>12</td> <td>13.07</td> <td>0.088</td> <td>11.018</td> </tr> <tr> <td>4</td> <td>10</td> <td>12.96</td> <td>0.676/7</td> <td>7.716</td> </tr> <tr> <td>5,6,7,8</td> <td>15</td> <td>12.31</td> <td>0.588/7</td> <td>18.278</td> </tr> <tr> <td></td> <td>50</td> <td>50</td> <td>1.506</td> <td>51.506</td> </tr> </tbody> </table>	No of successes	$O$	$E$	$\frac{(O-E)^2}{E}$	$\frac{O^2}{E}$	0,1,2	13	11.66	0.154	14.494	3	12	13.07	0.088	11.018	4	10	12.96	0.676/7	7.716	5,6,7,8	15	12.31	0.588/7	18.278		50	50	1.506	51.506	Combining 0,1,2 or 5,6,7,8.  M1 for attempting $\frac{(O-E)^2}{E}$ or $\frac{O^2}{E}$ with at least 2 correct expressions or 2 correct values to 2sf.	M1  M1
No of successes	$O$	$E$	$\frac{(O-E)^2}{E}$	$\frac{O^2}{E}$																													
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	50	50	1.506	51.506																													
	$\sum \frac{(O-E)^2}{E} = \sum \frac{O^2}{E} - 50 = 1.50\dots$	awrt 1.5 (calculator: 1.50498...)	A1																														
	$\nu = 4 - 2 = 2, \chi_2^2(10\%) = 4.605$	2 can be implied by 4.605 seen Only f.t. $\nu = r - 2$	B1 B1f.t.																														
	Insufficient evidence to reject $H_0$	For correct non-contextual statement linking their test statistic and their cv.	M1																														
	Data is consistent with a binomial distribution (oe)	A correct comment suggesting that binomial model is suitable / good fit. Hypotheses wrong way around scores A0 here. Condone parameters here.	A1																														
			(8)																														
			<b>Total 16</b>																														

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<b>6(a)</b>	$W = B - 1.1R$	May be implied by correct mean or variance	M1
	$W \sim N(55 - 1.1 \times 51, 1.3^2 + 1.1^2 \times 1.2^2)$ or $W \sim N(-1.1, 3.4324)$	( $\pm$ )1.1, awrt 3.43 (may be seen in standardisation)	A1, A1
	$P(W < 0) = P\left(Z < \frac{0 + 1.1}{\sqrt{3.4324}}\right)$	Standardising with their mean and their sd. leading to a probability > 0.5	M1
	$= P(Z < 0.5937\dots)$		
	$= 0.7224$ or $0.7237$	<b>awrt 0.72</b>	A1
			(5)
<b>6(b)</b>	$X = B_1 - B_2$	May be implied by correct mean or variance	M1
	$X \sim N(55 - 55, 2 \times 1.3^2)$ or $X \sim N(0, 3.38)$	0, 3.38	A1, A1
	$P\left(Z > \frac{1 - 0}{\sqrt{3.38}}\right)$ or $P\left(Z < \frac{-1 - 0}{\sqrt{3.38}}\right)$	dep on 1 <sup>st</sup> M1 for standardising with their mean and their sd.	dM1
	$P( X  > 1) = 2 \times P(X > 1)$	For 2 $\times$ seen or implied	M1
	$= 2 \times P(Z > 0.5439\dots) = 2 \times (1 - 0.7054)$	$2 \times 0.2946$ or $2 \times 0.2932$ (calc)	
	$= 0.5892$	<b>awrt 0.59</b>	A1
			(6)
<b>6(c)</b>	$V = B_1 + B_2 + B_3 + B_4 + B_5 + B_6 + B_7 + B_8 + B_9 + B_{10} + S$ $Y = R_1 + R_2 + R_3 + R_4 + R_5 + R_6 + R_7 + R_8 + R_9 + R_{10} + R_{11} + S$	May be implied by either correct distribution	M1
	$V \sim N(553, 16.94)$ and $Y \sim N(564, 15.88)$	Both correct	A1
	$D = Y - V$ so $D \sim N(11 \times 51 - 10 \times 55, 11 \times 1.2^2 + 10 \times 1.3^2 + 2 \times 0.2^2)$ or $D \sim N(11, 32.82)$	Attempt at their difference for the mean, and their sum for the variance.	M1
		( $\pm$ )11 and awrt 32.8	A1
	$P(D > 0) = P\left(Z > \frac{0 - 11}{\sqrt{32.82}}\right)$	dep on 1 <sup>st</sup> M1 for standardising using their mean and their standard deviation leading to a probability > 0.5	dM1
	$= P(Z > -1.920\dots)$		
	$= 0.9726$	<b>awrt 0.973</b>	A1
			(6)
			<b>Total 17</b>