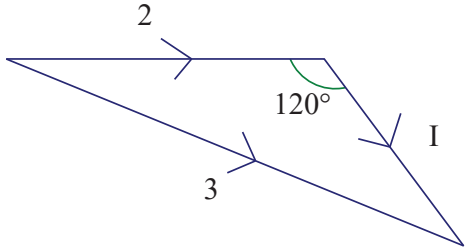


Question	Scheme	Mark	Notes
<b>1</b>	Accept column vectors throughout this question		
1a	Differentiate $\mathbf{r}$ (both components)	M1	In each component at least one power going down by 1
	$\mathbf{v} = (4t^3 - 16t)\mathbf{i} + (12t - 3\sqrt{t})\mathbf{j}$	A1	Accept as two separate components
	Equate $\mathbf{i}$ component of $\mathbf{v}$ to zero and solve for $t$	DM1	Dependent on the first M1. Must start with a component of the vector for $\mathbf{v}$ Can have more than one value at this stage.
	Obtain $(24 - 3\sqrt{2})\mathbf{j} \text{ (ms}^{-1}\text{)}$	A1	Accept $20\mathbf{j} \text{ (ms}^{-1}\text{)}$ or better. (19.757359...) Correct answer only Answer must be a vector
		<b>[4]</b>	
1b	Differentiate $\mathbf{v}$ (both components)	M1	For differentiating their $\mathbf{v}$ , even if the method for obtaining it was incorrect. Their $\mathbf{v}$ must be a vector. In each component at least one power going down by 1
	Obtain $\mathbf{a} = (12t^2 - 16)\mathbf{i} + (12 - \frac{3}{2}t^{-\frac{1}{2}})\mathbf{j}$	A1	Any equivalent form for acceleration
	Obtain $176\mathbf{i} + \frac{45}{4}\mathbf{j} \text{ (ms}^{-2}\text{)}$	A1	Accept $180\mathbf{i} + 11\mathbf{j} \text{ (ms}^{-2}\text{)}$ or better ISW
		<b>[3]</b>	
		<b>(7)</b>	

Question	Scheme				Mark	Notes
2a		$PQUY$	$RSTU$	$VWXY$	B1 B1	Correct mass ratios (accept 2:1:1) Correct vertical distances
	Mass	$16a^2$	$2 \times 4a^2$	$2 \times 4a^2$		
	From $PX$	$2a$	$5a$	$a$		
	Moments about $PX$ or a parallel axis				M1	Dimensionally correct equation. All terms required Allow for an equation within a vector equation.
	$16a^2 \times 2a + 8a^2 \times 5a + 8a^2 \times a = 32a^2 d$ $(= (16 + 8 + 8)a^2 \times d)$ or equivalent for a parallel axis				A1	Correct unsimplified equation Allow for an equation within a vector equation. Could have $y$ for $d$ here o.e.
	$80a = 32d \Rightarrow d = \frac{5}{2}a$ *				A1*	Obtain given answer from correct working. At least one stage of simplifying the moments equation is required. e.g. $32a^3 + 40a^3 + 8a^3$ seen, or they might have simplified the mass ratios at the start. Must get to $d = \dots$ in the final line
					[5]	
2b	Moments about $PQ$ or a parallel axis				M1	Dimensionally correct equation. All terms required
	$16a^2 \times 2a + 8a^2 \times 3a + 8a^2 \times 5a$ $= (16 + 8 + 8)a^2 \times h$ or equivalent for a parallel axis				A1ft A1	Unsimplified equation with at most one error. Follow their mass ratios. Correct unsimplified equation
	$\Rightarrow h = 3a$ from $PQ$				A1	$a$ from $YT$ , $3a$ from $XW$
	The working for the first 4 marks must be seen or used in part (b)					
	Correct use of trig. to find the tangent of a relevant angle.				M1	With <i>their</i> $3a$ e.g. $\tan \theta = \frac{3}{4 - \frac{5}{2}}$
	$\tan \theta = 2$				A1	Correct only
					[6]	
2c	Complete method to obtain an equation in $M$ and $F$				M1	e.g. Moments about $Q$ Dimensionally correct equation.
	$3a \times Mg = 4a \times F$				A1	Correct unsimplified equation Condone if $a$ missing throughout
	$F = \frac{3}{4}Mg$				A1	Correct only
					[3]	
					(14)	

Question	Scheme	Mark	Notes
3	Form impulse-momentum equation	M1	Dimensionally correct. Accept answers in “vector” form, or as separate components. Condone sine / cosine confusion.
	One correct equation	A1	e.g. one correct component of $\begin{pmatrix} I \cos 60^\circ \\ I \sin 60^\circ \end{pmatrix} = \frac{1}{4} \left[ \begin{pmatrix} 12 \cos \alpha \\ 12 \sin \alpha \end{pmatrix} - \begin{pmatrix} 8 \\ 0 \end{pmatrix} \right]$ or $\begin{pmatrix} \\ \\ \end{pmatrix} = \begin{pmatrix} 3 \cos \alpha - 2 \\ 3 \sin \alpha \end{pmatrix}$ $\begin{pmatrix} I \cos 60^\circ \\ I \sin 60^\circ \end{pmatrix} = \frac{1}{4} \left[ \begin{pmatrix} v_x \\ v_y \end{pmatrix} - \begin{pmatrix} 8 \\ 0 \end{pmatrix} \right]$ $\begin{pmatrix} \\ \\ \end{pmatrix} = \begin{pmatrix} 3 \cos \alpha - 2 \\ 3 \sin \alpha \end{pmatrix}$ if working parallel and perpendicular to the initial direction or one of $8 \sin 60^\circ = 12 \cos(30^\circ + \alpha)$ or $I = 0.25(12 \sin(30^\circ + \alpha) - 8 \cos 60^\circ)$ if working parallel and perpendicular to the impulse
	Form a second impulse-momentum equation	M1	
	correct second equation	A1	
	Complete method to solve for $I$	DM1	Dependent on the two preceding M marks. e.g. from $36 = (I + 4)^2 + 3I^2 \quad (4I^2 + 8I - 20 = 0)$
	$I = \sqrt{6} - 1$ (or 1.45 or 1.4)	A1	
		[6]	
3 alt		M1	Use of $I = mv - mu$ to draw a vector triangle. Dimensionally consistent.
		A1	Correct diagram
	Form an equation in $I$	M1	e.g. by using cosine rule
	$4 + I^2 - 4I \cos 120^\circ = 9$	A1	Correct unsimplified equation A correct cosine rule equation can imply the first M1A1 if no diagram seen
	Solve for $I$	DM1	Dependent on the 2 preceding M marks $I^2 + 2I - 5 = 0$
	$I = \sqrt{6} - 1$ (or 1.45 or 1.4)	A1	
		(6)	

Question	Scheme	Mark	Notes
4a	$4 - gT_1 = 0$ or $T_1 = \frac{\sqrt{32} \sin 45^\circ}{g}$	M1	Complete method using <i>suvat</i>
	$T_1 = 0.408$ (0.41)	A1	3 sf or 2 sf only. Not $\frac{20}{49}$
		[2]	
4b	Height of $Q$ above $P$ :	M1	Complete method using <i>suvat</i> and 7 and 4 for the initial vertical components
	$h = (7T_1 - \frac{1}{2}gT_1^2) - (4T_1 - \frac{1}{2}gT_1^2) (= 3T_1)$	A1	Correct unsimplified expression in $T_1$ or their $T_1$ . They do not need to have substituted for $T_1$ (2.0408... - 0.8163...)
	$h = 1.2$ (m)	A1ft	2 sf only ( $3 \times \text{their } T_1$ )
		[3]	
4c	Correct time for $P$ to reach $B$ . ( $\frac{40}{49}$ , 0.816, or $\frac{8}{g}$ or better)	B1	Seen or implied.
	Vertical component of speed $= 7 - g \times 2T_1 (= -1)$	M1	Complete method using <i>suvat</i> with $2T_1$ or their $t$ for the time at $B$ M0 if not using 7
	$\tan \alpha = \pm \frac{\text{their } 1}{5}$	M1	Correct use of <i>their</i> 1 and 5 to find an equation in a relevant angle (e.g. $90 - \alpha$ )
	$\alpha = 11$	A1	11 or better (e.g. 11.3)
	<b>If they use <math>T_1</math> in place of <math>2T_1</math> can score B0M0M1A0</b>		
		[4]	
4d	Form an equation in $T_2$ only	M1	Complete method using <i>suvat</i> and perpendicular gradients. e.g. $\begin{pmatrix} 5 \\ 7 \end{pmatrix} \cdot \begin{pmatrix} 5 \\ 7 - gT_2 \end{pmatrix} = 0$ Condone sign errors (Vertical component of speed $= \pm \frac{25}{7}$ ) (perpendicular direction is downwards at $35.5^\circ$ to the horizontal)
	$-\frac{25}{7} = 7 - gT_2$	A1	Correct unsimplified equation
	$T_2 = 1.08$ or $T_2 = 1.1$	A1	3 sf or 2 sf only
		[3]	
		(12)	

Question	Scheme	Mark	Notes
5a	Use of $P = Fv$ $\left(F = \frac{500}{6}\right)$	M1	
	Equation of motion	M1	Dimensionally correct. Required terms and no extras
	$F - 60 = 80a$	A1	Correct unsimplified equation in $F$
	$a = \frac{7}{24} (\text{ms}^{-2})$	A1	0.29 or better (0.291666666..)
		[4]	
5b	Gain in KE = $\frac{1}{2} \times 80 \times 8^2 (\text{J}) (= 2560(\text{J}))$ Gain in GPE = $80 \times 9.8 \times 300 (\text{J}) (= 235200(\text{J}))$ Work done against resistance = $20000 \times 60$	B1 B1	Any one correct (seen or implied) A second term correct (seen or implied)  (KE gain + GPE gain = 237760 J)
	<b>Use of suvat and <math>F = ma</math> is M0A0A0</b>		
	expression for combined work and energy	M1	All terms required and no double counting. Mass replaced with 80. Condone sign errors. Dimensionally correct. Condone error in zeros in 20000
	Total work done $= 40 \times 64 + 80 \times 9.8 \times 300 + 20000 \times 60$	A1	Correct unsimplified expression for the work done
	1440(kJ) or 1400(kJ)	A1	Accept answers in joules. 3 sf or 2 sf (1437760)
		[5]	
5c	Equation of motion	M1	Dimensionally correct. Required terms and no extras
	$F - 60 - 80g \times \sin \alpha = 0$ $\frac{P}{7} - 60 - 80g \times \frac{1}{20} = 0$	A1 A1	Unsimplified equation in $P$ or $F$ with at most one error Correct unsimplified equation in $P$
	$P = 694$ or $P = 690$	A1	3sf or 2 sf only
		[4]	
		(13)	

Question	Scheme	Mark	Notes
6a			
	Moments about A: <b>M0 if there is no resolving</b>	M1	Need all terms and no extras. Dimensionally consistent. Condone sign errors and sine/cosine confusion.
	$4a \cos 30^\circ \times W + 8a \cos 30^\circ \times \frac{W}{4} = 5a \cos 30^\circ \times T$	A1	Correct unsimplified equation
	$6W = 5T \Rightarrow T = \frac{6}{5}W \quad *$	A1*	Obtain <b>given answer</b> from correct working, e.g. show cancelling of the common factors or some simplification of the moments equation
		[3]	
6b	They need 2 equations. Award M1A1 for the first correct equation seen and M1A1 for the second correct equation. Common alternatives: $M(B): T \cos 30^\circ \times 3a + V \cos 30^\circ \times 8a = W \cos 30^\circ \times 4a + H \cos 60^\circ \times 8a$ $M(C): W \cos 30^\circ \times a + H \cos 60^\circ \times 5a = \frac{1}{4}W \cos 30^\circ \times 3a + V \cos 30^\circ \times 5a$ Perpendicular to rod: $\frac{1}{4}W \cos 30^\circ + W \cos 30^\circ + H \cos 60^\circ = T \cos 30^\circ + V \cos 30^\circ$ Parallel to rod: $\frac{1}{4}W \cos 60^\circ + T \cos 60^\circ + W \cos 60^\circ = V \cos 60^\circ + H \cos 30^\circ$		
	First equation dimensionally correct. Condone sine/cosine confusion and sign errors	M1	e.g. Resolve horizontally
	Correct unsimplified equation	A1	$H = T \cos 30^\circ \quad \left( H = \frac{3\sqrt{3}}{5}W \right)$
	Second equation dimensionally correct. Condone sine/cosine confusion and sign errors	M1	e.g. resolve vertically
	Correct unsimplified equation	A1	$V + T \cos 60^\circ = W + \frac{W}{4} \quad \left( V = \frac{13}{20}W \right)$
	$ R  = \sqrt{V^2 + H^2}$ or $ R ^2 = V^2 + H^2$	DM1	Correct use of Pythagoras Dependent on two preceding M marks.
	$ R  = \frac{W}{20} \sqrt{3 \times 144 + 169} = \frac{\sqrt{601}}{20}W$	A1	1.2W or better (1.22576...)
		[6]	
		(9)	

Question	Scheme	Mark	Notes
7a			
	Equation for CLM	M1	Dimensionally correct. All terms required. Condone sign errors.
	$8mu - 6mu = 2my - 4mx$ $(u = y - 2x)$	A1	Correct unsimplified equation
	Equation for kinetic energy ( $\frac{1}{2}$ or 2 must be used)	M1	Dimensionally correct. Correct masses paired with correct velocities. All terms required. No sign errors. Condone 2 on the wrong side.
	$2mx^2 + my^2 = \frac{1}{2}(2m \times 4u^2 + m \times 9u^2)$ $(17u^2 = 4x^2 + 2y^2)$	A1	Correct unsimplified equation
	Solve for y: $17u^2 = 2y^2 + (y - u)^2$ $\Rightarrow 3y^2 - 2yu - 16u^2 = 0$	DM1	Some working must be shown to obtain the quadratic in y (and u). Dependent on the preceding M marks $((3y - 8u)(y + 2u) = 0)$
	$\Rightarrow y = \frac{8}{3}u$ *	A1*	Obtain given answer from correct working
		[6]	
7b	Use of Impact Law: $x + y = e \times 5u$	M1	Condone sign errors but must be used the right way round.
	$e = \frac{\frac{1}{2}\left(\frac{8}{3}u - u\right) + \frac{8}{3}u}{5u}$	A1	Correct unsimplified equation. $\left(x = \frac{5u}{6}\right)$
	$= \frac{7}{10}$	A1	Correct only
		[3]	
7c	Velocity of Q after impact $= f \times \frac{8}{3}u$	B1	Allow $\pm$
	No collision if $f \times \frac{8}{3}u \leq \frac{5}{6}u$ i.e. speed of P $\geq$ speed of Q	M1	Correct inequality with their values Accept strict inequality. Dimensionally correct.
	$\Rightarrow 0 < f \leq \frac{5}{16}$	A1	Both ends required. $(0 < f \leq 0.3125)$
		[3]	
7d	Use of $I = \pm 2m \left( y - \left( -\frac{1}{4}y \right) \right)$	M1	Subtraction seen or implied with <i>their</i> $\frac{1}{4}y$ Requires correct mass Requires correct impact law
	$ I  = \frac{20}{3}mu$	A1	Or equivalent. Must be positive 6.7mu or better Condone $-\frac{20}{3}mu \rightarrow \frac{20}{3}mu$ with no explanation
		[2]	
		(14)	