

Question Number	Scheme	Marks
1		
(a)	$2n+1 = A(n+1)^2 + Bn^2 \Rightarrow 2n+1 = An^2 + 2An+1 + Bn^2$	
	$A=1 \quad B=-1 \text{ or } \frac{1}{n^2} - \frac{1}{(n+1)^2}$	B1 (1)
(b)	$\sum_{r=5}^n \frac{2r+1}{r^2(r+1)^2} = \sum_{r=5}^n \left(\frac{1}{r^2} - \frac{1}{(r+1)^2} \right)$ $= \left(\frac{1}{5^2} - \frac{1}{6^2} \right) + \left(\frac{1}{6^2} - \frac{1}{7^2} \right) + \dots + \left(\frac{1}{n^2} - \frac{1}{(n+1)^2} \right)$	M1
	$\sum_{r=5}^n \frac{2r+1}{r^2(r+1)^2} = \frac{1}{5^2} - \frac{1}{(n+1)^2}$	A1
	$= \frac{n^2 + 2n + 1 - 25}{25(n+1)^2} = \frac{n^2 + 2n - 24}{25(n+1)^2}$	M1A1 (4)
		[5]
Notes		
(a) B1	Both values correct with or without working seen, may be in the expression. Ignore incorrect working.	
(b) M1	Show sufficient terms to demonstrate the cancelling. Require at least one cancelling term seen. Must start at $r = 5$ - M0 if starting at e.g. $r = 1$ unless there is a full process to complete the difference method (same condition) and apply $f(n) - f(4)$	
A1	Extract the two correct terms, or in the Alt obtains a correct overall expression.	
M1	Write the terms with a (non-zero) common denominator with at least numerator correct for their terms. Not dependent - may be scored following M0 if no cancelling terms were shown, but must have had exactly two terms to combine from differences.	
A1	Correct answer in the required form or accept correct values stated following an unsimplified form. (Allow as long as correct terms were extracted, even if no cancelling terms were shown.) Note: this means M0A0M1A1 can be scored for answers which show only the last two lines of the scheme with no cancelling process shown. Note: if e.g. r is used in place of n allow full marks if recovered, but A0 if left in terms of r .	
Alt (b) for first two marks	$\sum_{r=1}^n \frac{2r+1}{r^2(r+1)^2} = \sum_{r=1}^n \left(\frac{1}{r^2} - \frac{1}{(r+1)^2} \right)$ $= \left(\frac{1}{1^2} - \frac{1}{2^2} \right) + \left(\frac{1}{2^2} - \frac{1}{3^2} \right) + \dots + \left(\frac{1}{n^2} - \frac{1}{(n+1)^2} \right) = 1 - \frac{1}{(n+1)^2}$ $\rightarrow \sum_{r=5}^n \frac{2r+1}{r^2(r+1)^2} = 1 - \frac{1}{(n+1)^2} - \left(1 - \frac{1}{25} \right) = \frac{n^2 + 2n - 24}{(n+1)^2} - \frac{24}{25}$	M1A1

Question Number	Scheme	Marks	
2 (a)	E.g. $(x+3)(x-5) = 9 \Rightarrow x^2 - 2x - 24 = 0 \Rightarrow x = \dots$ OR $(x-5)(x+3)^2 - 9(x+3) = 0 \Rightarrow (x+3)(x-6)(x+4) = 0 \Rightarrow x = \dots$ OR $\frac{(x+3)(x-5)-9}{x+3} < 0 \Rightarrow x^2 - 2x - 24 = 0 \Rightarrow x = \dots$	M1	
	CVs: 6, -4 ; -3	A1;B1	
	$x < -4, -3 < x < 6$	dM1A1A1	
	OR: $x \in (-3, 6) \cup (-\infty, -4)$ or any equivalent notation.	(6)	
	(b)	$x < 6, x \neq -3$ or any equivalent notation.	B1ftB1 (2)
	[8]		
Notes			
(a) M1	For a correct algebraic method to find the intersection points of $y = x - 5$ and $y = \frac{9}{x+3}$. May set these equal and form a quadratic and solve. May multiply through by $(x+3)^2$ and collect on one side or use any other valid method Eg work from $\frac{(x+3)(x+2)-12}{x+3} > 0$ Answers only from a calculator score M0. Must reach at least a quadratic or cubic before answers given. Do not be concerned with the equality or inequality for this mark.		
A1 B1 dM1 A1 A1cso	For 6, -4 obtained via a valid algebraic method. for the CV -3 seen anywhere Obtaining (any) inequalities using all of their critical values and no other numbers. For at least one correct interval allowing for ... or ,, used instead of < and > Both correct ranges and no extras. Use of ... or ,, scores A0. May be written in set notation, and all work should have been correct so penalise if incorrect inequalities method was used at the start. Accept $x < -4$ and/or $-3 < x < 6$ with "and" or "or" For candidates who draw a sketch graph and follow with the cvs without any algebra shown only the B mark is available. Those who use some algebra after their graph may gain marks as earned (possibly all)		
(b) B1ft	For the " $x < 6$ " in some form with the possible exception of the CVs from (a). Allow $x, 6$ if already penalised in (a). It is essentially for realising all the extra (valid) values less than -3 are solutions while retaining all their given solutions. If only the CVs themselves are excluded allow B1. Follow through their answer to (a).		
B1	Fully correct answer. May give as intervals $x < -3, -3 < x < 6$		

Question Number	Scheme	Marks
3	$w = \frac{z}{z + 4i}$	
	$w(z + 4i) = z \Rightarrow z(1 - w) = 4iw$ or $z = \frac{4iw}{1 - w}$ oe	M1A1
	$ z = 3 \quad \left \frac{4iw}{1 - w} \right = 3$	dM1
	$ 4iw = 3 1 - w $	
	$w = u + iv \quad 16(u^2 + v^2) = 9((1 - u)^2 + v^2)$	ddM1A1
	$16u^2 + 16v^2 = 9(1 - 2u + u^2 + v^2)$	
	$7u^2 + 7v^2 + 18u - 9 = 0$	
	$\left(u + \frac{9}{7}\right)^2 + v^2 = \frac{144}{49}$	dddM1
	Centre $\left(-\frac{9}{7}, 0\right)$ Radius $\frac{12}{7}$	A1A1 (8)
	Notes	
(a) M1 A1 dM1 ddM1 A1 dddM1 A1 A1	re-arrange to $z = \dots$ or an expression $z(\alpha w + \beta) = \gamma w + \delta$ correct result dep (on first M1) using $ z = 3$ with their previous result dep (on both previous M marks) use $w = u + iv$ (or $w = x + iy$ or any other pair of letters) and attempts the squares of the moduli. The i's must be dealt with correctly, but allow e.g. $3^2 \rightarrow 3$ for a correct equation quadratic in u and v after squaring (including squaring coefficients). dep (on all previous M marks) re-arrange to the completed square form of the equation of a circle (same coeffs for the squared terms) or implied by a correct centre or radius following a correct equation with terms gathered. either correct and exact. both correct and exact. Note: Allow recovery for the last three A's if all that is incorrect in is the wrong sign in their expression for z , ie $z = \frac{-4iw}{1 - w}$ If you see alternative methods, e.g. via Apollonian approaches or attempts to use $z = x + iy$ in the original equation, that you feel are worthy of credit please use Review to consult your team leader.	

Question Number	Scheme	Marks
4	$\frac{dy}{dx} - 3y \tan x = e^{4x} \sec^3 x$	
(a)	$e^{-3 \int \tan x dx} = e^{-3 \ln \sec x} = \sec^{-3} x \text{ or } \cos^3 x$	M1A1
	$\cos^3 x \frac{dy}{dx} - 3y \sin x \cos^2 x = e^{4x} \cos^3 x \sec^3 x$	
	$\frac{d}{dx}(y \cos^3 x) = e^{4x} \Rightarrow y \cos^3 x = \int e^{4x} dx$	M1
	$y \cos^3 x = \frac{1}{4} e^{4x} (+c)$	M1
	$y = \left(\frac{1}{4} e^{4x} + c\right) \sec^3 x \text{ or } y = \left(\frac{1}{4} e^{4x} + c\right) \cos^{-3} x \text{ oe}$	A1
		(5)
(b)	$y = 4, x = 0 \quad 4 = \left(\frac{1}{4} + c\right)$	
	$c = \frac{15}{4}$	M1
	$y = \frac{1}{4}(e^{4x} + 15) \sec^3 x \text{ or } \frac{1}{4}(e^{4x} + 15) \cos^{-3} x \text{ oe}$	A1
		(2)
		[7]
(a) M1 A1 M1 M1 A1	<p style="text-align: center;">Notes</p> <p>Attempt the integrating factor, including integration of $(-3)\tan x$; $\ln \cos$ or $\ln \sec$ seen</p> <p>Correct simplified integrating factor $\sec^{-3} x$ or $\cos^3 x$</p> <p>Multiply the equation by the integrating factor and integrate the LHS. Look for $y \times$ their IF = $\int (e^{4x} \sec^3 x \times \text{their IF}) dx$ (condone missing dx)</p> <p>Integrate RHS, constant not needed. Must be a function they can integrate and a valid attempt (e.g. allowing coefficient slips).</p> <p>Correct result in the demanded form, including $y = \dots$, constant included</p>	
(b) M1 A1	<p>Use the given initial conditions to obtain a value for c</p> <p>Fully correct final answer. Must include $y = \dots$ but allow A1 if missing and penalised in (a). May be in the form $y \cos^3 x = \dots$ or $4y \cos^3 x = \dots$</p>	

Question Number	Scheme	Marks
5. (a)	$\frac{d^2y}{dx^2} = -\frac{2}{y}\left(\frac{dy}{dx}\right)^2 + 2$	
	$\left(\frac{dy}{dx}\right)\frac{d^2y}{dx^2}$ seen	B1
	$\frac{d^3y}{dx^3} = -\frac{4}{y}\left(\frac{dy}{dx}\right)\frac{d^2y}{dx^2} + \frac{2}{y^2}\left(\frac{dy}{dx}\right)^3$	M1A1A1
		(4)
ALT:	$\left(\frac{dy}{dx}\right)^2 \rightarrow 2\left(\frac{dy}{dx}\right)\frac{d^2y}{dx^2}$ seen	B1
	$\frac{dy}{dx}\left(\frac{d^2y}{dx^2}\right) + y\frac{d^3y}{dx^3} + 4\left(\frac{dy}{dx}\right)\left(\frac{d^2y}{dx^2}\right) - 2\frac{dy}{dx} = 0$	M1A1
	$\frac{d^3y}{dx^3} = \frac{1}{y}\left(-5\frac{d^2y}{dx^2} + 2\right)\frac{dy}{dx}$	A1 (4)
(b)	At $x = 0$ $\frac{d^2y}{dx^2} = \frac{1}{2}(-2 \times (1)^2 + 4) = 1$	B1
	$\frac{d^3y}{dx^3} = \frac{1}{2}(-5 \times 1 + 2) \times 1 = \frac{-3}{2}$	M1
	$(y =) 2 + x + (1)\frac{x^2}{2!} + \left(\frac{-3}{2}\right)\frac{x^3}{3!} + \dots$	M1
	$y = 2 + x + \frac{1}{2}x^2 - \frac{1}{4}x^3 + \dots$	A1 (4)
		[8]
Notes		
(a) B1 M1 A1 A1 ALT B1 M1 A1 A1	$\left(\frac{dy}{dx}\right)\frac{d^2y}{dx^2}$ seen in the differentiation Divide equation by y and differentiate wrt x chain and product rules needed. LHS correct Either RHS term correct. Need not be simplified. Both RHS terms correct. Need not be simplified. $\left(\frac{dy}{dx}\right)^2 \rightarrow 2\left(\frac{dy}{dx}\right)\frac{d^2y}{dx^2}$ correct differentiation of middle term. Differentiate before dividing. Product rule must be used. Correct differentiation of $y\frac{d^2y}{dx^2}$ and $-2y$ Rearrange to a correct expression for $\frac{d^3y}{dx^3}$ (need not be simplified)	

Notes	
(b)	
B1	Correct value for $\frac{d^2y}{dx^2}$. May be implied by the term in their expansion.
M1	Use their expression from (a) to obtain a value for $\frac{d^3y}{dx^3}$ (May be implied - you may need to check if their value follows from their expression in (a).)
M1	Taylor's series formed using their values for the derivatives, accept 2! or 2 and 3! or 6 Correct series, must start $y = \dots$, or allow $f(x) = \dots$ as long as $y = f(x)$ has been defined in the question.
A1	Must come from a correct expression for $\frac{d^3y}{dx^3}$

Question Number	Scheme	Marks
6 (a)	$\frac{d(r \sin \theta)}{d\theta} = 4a \cos \theta + 4a \cos^2 \theta - 4a \sin^2 \theta$ or $4a \cos \theta + 4a \cos 2\theta$ oe (Or allow $\frac{d(r \cos \theta)}{d\theta} = -4a \sin \theta - 8a \cos \theta \sin \theta$ or $-4a \sin \theta - 4a \sin 2\theta$)	M1
	E.g. $4a \cos \theta + 4a \cos^2 \theta - 4a \sin^2 \theta = 0 \Rightarrow \cos \theta + \cos^2 \theta - (1 - \cos^2 \theta) = 0$	M1
	$2 \cos^2 \theta + \cos \theta - 1 = 0$ terms in any order	A1
	$(2 \cos \theta - 1)(\cos \theta + 1) = 0 \Rightarrow \cos \theta = \dots$	ddM1
	$\left(\cos \theta = \frac{1}{2} \Rightarrow \right) \theta = \frac{\pi}{3}$ ($\theta = \pi$ need not be seen)	A1
	$r = 4a \times \frac{3}{2} = 6a$	A1 (6)
(b)	Area = $\frac{1}{2} \int r^2 d\theta = \frac{1}{2} \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} 16a^2 (1 + \cos \theta)^2 d\theta$	
	$= \frac{16a^2}{2} \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} (1 + 2 \cos \theta + \cos^2 \theta) d\theta$	M1
	$= 8a^2 \int_{\frac{\pi}{6}}^{\frac{\pi}{3}} \left(1 + 2 \cos \theta + \frac{1}{2} (\cos 2\theta + 1) \right) d\theta$	M1
	$= 8a^2 \left[\theta + 2 \sin \theta + \frac{1}{2} \left(\frac{1}{2} \sin 2\theta + \theta \right) \right]_{\frac{\pi}{6}}^{\frac{\pi}{3}}$	dM1A1
	$8a^2 \left[\frac{\pi}{3} + \sqrt{3} + \frac{1}{4} \times \frac{\sqrt{3}}{2} + \frac{\pi}{6} - \left(\frac{\pi}{6} + 1 + \frac{1}{4} \times \frac{\sqrt{3}}{2} + \frac{\pi}{12} \right) \right]$	A1
	$8a^2 \left[\frac{\pi}{4} + \sqrt{3} - 1 \right]$	
	Area R = $8a^2 \left[\frac{\pi}{4} + \sqrt{3} - 1 \right] - 6a^2 \left(1 + \frac{\sqrt{3}}{2} \right) = a^2 (2\pi + 5\sqrt{3} - 14)$	M1A1 (7)
	[13]	
	Notes	
(a) M1	Attempt the differentiation of $r \sin \theta$ using product rule or $\sin 2\theta = 2 \sin \theta \cos \theta$ OR for this mark only allow differentiation of $r \cos \theta$, inc use of product rule, chain rule or $\cos^2 \theta = \frac{1}{2}(1 \pm \cos 2\theta)$	
M1	Allow errors in coefficients as long as the form is correct.	
A1	Sets their derivative of $r \sin \theta$ equal to zero and achieves a quadratic expression in $\cos \theta$	
ddM1	Correct 3 term quadratic in $\cos \theta$ (any multiple, including a)	
A1	Dep on both M marks. Solve their quadratic (usual rules) giving one or two roots	
	Correct quadratic solved to give $\theta = \frac{\pi}{3}$	

	Notes
A1*	Correct r obtained from an intermediate step. Accept as shown in scheme, or $r = 4a \left(1 + \cos \frac{\pi}{3} \right) = 6a$ or equivalent in stages. No need to see coordinates together in brackets
(b)	Note : first 4 marks of (b) do not require limits.
M1	Use of correct area formula, $\frac{1}{2}$ may be seen later, inc squaring the bracket to obtain 3 terms - limits need not be shown.
M1	Use double angle formula (formula to be of form $\cos^2 \theta = \pm \frac{1}{2}(\cos 2\theta \pm 1)$) to obtain an integrable function - limits need not be shown, $\frac{1}{2}$ from area formula may be missing,
dM1	Attempt the integration $\cos \theta \rightarrow \pm k \sin \theta$ and $\cos 2\theta \rightarrow \pm m \sin 2\theta$ - limits not needed – dep on 2 nd M mark but not the first. Note if only two terms arise from squaring allow for $\cos 2\theta \rightarrow \pm m \sin 2\theta$
A1	Correct integration – substitution of limits not required (NB Not follow through)
A1	Include the $\frac{1}{2}$ and substitute the correct limits in a correct integral. Note may be attempted via integral from 0 to $\frac{\pi}{3}$ minus integral from 0 to $\frac{\pi}{6}$ - but attempts at sector formula for the latter is A0.
M1	Attempt the area of the triangle - accept valid attempt even if not subtracted from area. E.g. attempts $\frac{1}{2} OA \cdot OB \sin \frac{\pi}{6}$
A1	Correct final answer in the demanded the form.

Question Number	Scheme	Marks
7(a)	$\frac{dy}{dx} = v + x \frac{dv}{dx}$ or $\frac{dv}{dx} = x^{-1} \frac{dy}{dx} - x^{-2}y$ (oe)	M1A1
	$\frac{d^2y}{dx^2} = \frac{dv}{dx} + \frac{dv}{dx} + x \frac{d^2v}{dx^2}$ or $\frac{d^2v}{dx^2} = -x^{-2} \frac{dy}{dx} + x^{-1} \frac{d^2y}{dx^2} + 2x^{-3}y - x^{-2} \frac{dy}{dx}$ (oe)	dM1A1
	$3 \left(2 \frac{dv}{dx} + x \frac{d^2v}{dx^2} \right) - \frac{6}{x} \left(v + x \frac{dv}{dx} \right) + \frac{6xv}{x^2} + 3xv = x^2$ (oe in reverse)	ddM1
	$3x \frac{d^2v}{dx^2} + 6 \frac{dv}{dx} - 6 \frac{dv}{dx} - \frac{6}{x}v + \frac{6v}{x} + 3xv = x^2$	
	$3 \frac{d^2v}{dx^2} + 3v = x$ *	A1 * (6)
(b)	$3\lambda^2 + 3 = 0$ so $\lambda = \pm i$	M1
	$(v =) Ae^{ix} + Be^{-ix}$ or $(v =) C \cos x + D \sin x$	A1
	P.I: Try $(v =) kx (+l)$	B1
	$\frac{dv}{dx} = k \quad \frac{d^2v}{dx^2} = 0$	
	$3 \times 0 + 3(kx (+l)) = x$	M1
	$k = \frac{1}{3} \quad (l = 0)$	
	$v = Ae^{ix} + Be^{-ix} + \frac{1}{3}x$ or $v = C \cos x + D \sin x + \frac{1}{3}x$	A1
	$y = x \left(Ae^{ix} + Be^{-ix} + \frac{1}{3}x \right)$ or $y = x \left(C \cos x + D \sin x + \frac{1}{3}x \right)$	B1ft (6)
	[12]	
Notes		
(a)		
M1	Attempt to find a relevant first derivative from $y = xv$ e.g to get $\frac{dy}{dx}$ or $\frac{dv}{dx}$ - product or quotient rule must be used. Methods via $\frac{d..}{dv}$ would require a chain rule to reach a relevant derivative.	
A1	Correct derivative	
dM1	Attempt to differentiate their $\frac{dy}{dx}$ or $\frac{dv}{dx}$ to obtain an expression for $\frac{d^2y}{dx^2}$ or $\frac{d^2v}{dx^2}$ - product rule must be used. Depends on the previous M mark	
A1	Correct expression for $\frac{d^2y}{dx^2}$ or $\frac{d^2v}{dx^2}$	

Question Number	Scheme	Marks
8 (a)	$(\cos \theta + i \sin \theta)^5 = \cos 5\theta + i \sin 5\theta$	B1
	$= \cos^5 \theta + 5 \cos^4 \theta (i \sin \theta) + \frac{5 \times 4}{2!} \cos^3 \theta (i \sin \theta)^2$ $+ \frac{5 \times 4 \times 3}{3!} \cos^2 \theta (i \sin \theta)^3 + \frac{5 \times 4 \times 3 \times 2}{4!} \cos \theta (i \sin \theta)^4 + (i \sin \theta)^5$	M1
	$= \cos^5 \theta + 5i \cos^4 \theta \sin \theta - 10 \cos^3 \theta \sin^2 \theta - 10i \cos^2 \theta \sin^3 \theta + 5 \cos \theta \sin^4 \theta + i \sin^5 \theta$	A1
	$\sin 5\theta = 5 \cos^4 \theta \sin \theta - 10 \cos^2 \theta \sin^3 \theta + \sin^5 \theta$ $= 5(1 - \sin^2 \theta)^2 \sin \theta - 10(1 - \sin^2 \theta) \sin^3 \theta + \sin^5 \theta \frac{dy}{dx}$ $= 5(1 - 2 \sin^2 \theta + \sin^4 \theta) \sin \theta - 10(1 - \sin^2 \theta) \sin^3 \theta + \sin^5 \theta$	M1
	$\sin 5\theta = 16 \sin^5 \theta - 20 \sin^3 \theta + 5 \sin \theta$ *	A1* (5)
Alternative:	Using " $z - \frac{1}{z}$ " $z^5 - \frac{1}{z^5} = 2i \sin 5\theta$ oe	B1
	Binomial expansion of $\left(z - \frac{1}{z}\right)^5$	M1
	$32 \sin^5 \theta = 2 \sin 5\theta - 10 \sin 3\theta + 20 \sin \theta$	A1
	Uses double angle formulae etc to obtain $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$ and then use it in their expansion	M1
	$\sin 5\theta = 16 \sin^5 \theta - 20 \sin^3 \theta + 5 \sin \theta$ *	A1* (5)
(b)	Let $x = \sin \theta$ $16x^5 - 20x^3 + 5x = -\frac{1}{5} \Rightarrow \sin 5\theta = \dots$	M1A1
	$\Rightarrow \theta = \frac{1}{5} \sin^{-1} \left(\pm \frac{1}{5}\right) = 38.306$ (or $-2.307, 69.692, 110.306, 141.693, 182.306$)	dM1
	(or in radians $-0.0402 \dots 0.6685 \dots, 1.216 \dots, 1.925 \dots, 2.473 \dots$)	
	Two of (awrt) $x = \sin \theta = -0.963, -0.555, -0.040, 0.620, 0.938$	A1
	All of (awrt) $x = \sin \theta = -0.963, -0.555, -0.040, 0.620, 0.938$	A1 (5)
(c)	$\int_0^{\frac{\pi}{4}} (4 \sin^5 \theta - 5 \sin^3 \theta - 6 \sin \theta) d\theta = \left(\int_0^{\frac{\pi}{4}} \frac{1}{4} (\sin 5\theta - 5 \sin \theta) - 6 \sin \theta d\theta \right)$	M1
	$= \left[\frac{1}{4} \left(-\frac{1}{5} \cos 5\theta + 5 \cos \theta \right) + 6 \cos \theta \right]_0^{\frac{\pi}{4}} = \left[-\frac{1}{20} \cos 5\theta + \frac{29}{4} \cos \theta \right]_0^{\frac{\pi}{4}}$	A1
	$\frac{1}{4} \left[-\frac{1}{5} \cos \frac{5\pi}{4} + 5 \cos \frac{\pi}{4} - \left(-\frac{1}{5} + 5 \right) \right] + 6 \cos \frac{\pi}{4} - 6$	
	$= \frac{1}{4} \left[\frac{1}{5} \times \frac{1}{\sqrt{2}} + \frac{5}{\sqrt{2}} - 4 \frac{4}{5} \right] + \frac{6}{\sqrt{2}} - 6$	dM1
	$= \frac{73\sqrt{2}}{20} - \frac{36}{5}$ oe	A1 (4)
		[14]
	Notes	

(a)	
B1	Applies de Moivre correctly. Need not see full statement, but must be correctly applied.
M1	Use binomial theorem to expand $(\cos \theta + i \sin \theta)^5$ May only show imaginary parts - ignore errors in real parts. Binomial coefficients must be evaluated.
A1	Simplify coefficients to obtain a simplified result with all imaginary terms correct
M1	Equate imaginary parts and obtain an expression for $\sin 5\theta$ in terms of powers of $\sin \theta$ No $\cos \theta$ now
A1*	Correct given result obtained from fully correct working with at least one intermediate line with the $(1 - \sin^2 \theta)^2$ expanded. Must see both sides of answer (may be split across lines). A0 if equating of imaginary terms is not clearly implied.
(b)	
	Note Answers only with no working score no marks as the “hence” has not been used. But if the first M1A1 gained then dM1 may be implied by a correct answer.
M1	Use substitution $x = \sin \theta$ and attempts to use the result from (a) to obtain a value for $\sin 5\theta$
A1	Correct value for $\sin 5\theta$
dM1	Proceeds to apply arcsin and divide by 5 to obtain at least one value for θ . Note for $\sin 5\theta = \frac{1}{5}$ the values you may see are the negatives of the true answers. FYI: ($5\theta = -11.53\dots, 191.53\dots, 348.46\dots, 551.53\dots, 708.46\dots, 911.53\dots$) (Or in radians $-0.201\dots, 3.3428\dots, 6.0819\dots, 9.6260\dots, 12.365\dots, 15.909\dots$)
A1	Proceeds to take sin and achieve at least 2 different correct values for x or $\sin \theta$
A1	For all 5 values of x or $\sin \theta$ awrt 3 d.p. (allow 0.62 and -0.04)
(c)	
M1	Use previous work to change the integrand into a function that can be integrated
A1	Correct result after integrating. Any limits shown can be ignored
dM1	Substitute given limits, subtracts and uses exact numerical values for trig functions
A1	Final answer correct (or provided in the given form)