[1]

**1** (a) Sketch the graph of y = |2x + 1|.

<b>(b)</b>	Solve the inequality $3x + 5 <  2x + 1 $ .	[3]

2 On a sketch of an Argand diagram shade the region whose points represent complex numbers z satisfying the inequalities  $|z| \le 3$ , Re  $z \ge -2$  and  $\frac{1}{4}\pi \le \arg z \le \pi$ . [4]



where $a$ and $b$ are integers.	the form $\frac{\ln a}{\ln b}$ ,	your answ	$= 5(3^{-x})$ . Giv	quation $2^{3x-1}$	Solve the e
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- The complex numbers u and w are defined by  $u = 2e^{\frac{1}{4}\pi i}$  and  $w = 3e^{\frac{1}{3}\pi i}$ .
  - (a) Find  $\frac{u^2}{w}$ , giving your answer in the form  $re^{i\theta}$ , where r > 0 and  $-\pi < \theta \le \pi$ . Give the exact values of r and  $\theta$ .

.....

**(b)** State the least positive integer n such that both  $\operatorname{Im} w^n = 0$  and  $\operatorname{Re} w^n > 0$ . [1]

6	(a)	Prove the identity $\cos 4\theta + 4\cos 2\theta + 3 \equiv 8\cos^4 \theta$ .	[4]
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	Hence solve the equation $\cos 4\theta + 4\cos 2\theta = 4$ for $0^{\circ} \le \theta \le 180^{\circ}$ .	[3
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The equation of a curve is $y =$	COS <sup>2</sup> Y	for $0 \le x$	$<\frac{1}{2}\pi.$	At the point	where $x = a$ ,	the tangent	to the
curve has gradient equal to 12.	005 77						

Show that $a = \cos^{-1} \left( \sqrt[3]{\frac{\cos a + 2a \sin a}{12}} \right)$	<u>a</u> ).	
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	rative formula based on the ve the result of each iteration		termine $a$ correct to 2 decim
	ve the result of each herativ	on to 1 decimal places.	

8 In a certain chemical reaction the amount, x grams, of a substance is increasing. The differential equation satisfied by x and t, the time in seconds since the reaction began, is

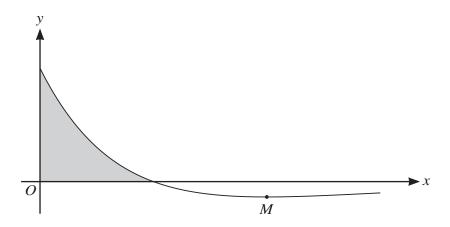
$$\frac{\mathrm{d}x}{\mathrm{d}t} = kx\mathrm{e}^{-0.1t},$$

where k is a positive constant. It is given that x = 20 at the start of the reaction.

Solve the differential equation, obtaining a relation between $x$ , $t$ and $k$ .	[
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	When $t = 10$ , find	d the value of $k$	and find the val	ue approached	
	) when $t = 10$ , find	d the value of <i>k</i>	and find the val	ue approached	
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	) when $t = 10$ , find	d the value of <i>k</i>	and find the val	ue approached	
	) when $t = 10$ , find	d the value of k	and find the val	ue approached	
	) when <i>t</i> = 10, find	d the value of k	and find the val	ue approached	
	) when $t = 10$ , find	d the value of k	and find the val	ue approached	
	) when <i>t</i> = 10, find	d the value of k	and find the val	ue approached	
	) when <i>t</i> = 10, find	d the value of k	and find the val	ue approached	
Given that $x = 40$ large.	) when <i>t</i> = 10, find	d the value of k	and find the val	ue approached	by x as t becomes [3]

9



The diagram shows part of the curve  $y = (3 - x)e^{-\frac{1}{3}x}$  for  $x \ge 0$ , and its minimum point M.

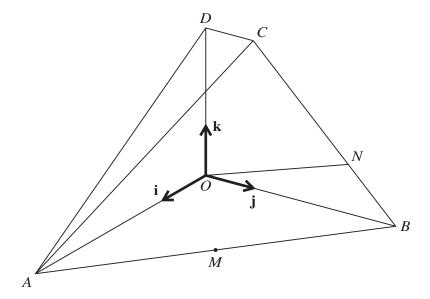
(a)	Find the exact coordinates of $M$ .	[5]

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10 Let  $f(x) = \frac{2x^2 + 7x + 8}{(1+x)(2+x)^2}$ .

(a)	Express $f(x)$ in partial fractions.	[5]
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	Hence obtain the expansion of $f(x)$ in ascending powers of $x$ , up to and including	[5
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In the diagram, OABCD is a solid figure in which OA = OB = 4 units and OD = 3 units. The edge OD is vertical, DC is parallel to OB and DC = 1 unit. The base, OAB, is horizontal and angle  $AOB = 90^{\circ}$ . Unit vectors  $\mathbf{i}$ ,  $\mathbf{j}$  and  $\mathbf{k}$  are parallel to OA, OB and OD respectively. The midpoint of AB is M and the point N on BC is such that CN = 2NB.

(a)	Express vectors $\overrightarrow{MD}$ and $\overrightarrow{ON}$ in terms of <b>i</b> , <b>j</b> and <b>k</b> .	[4]
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<b>(b)</b>	Calculate the angle in degrees between the directions of $\overrightarrow{MD}$ and $\overrightarrow{ON}$ .	[3]
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(c)	Show that the length of the perpendicular from $M$ to $ON$ is $\sqrt{\frac{22}{5}}$ .	[4]
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