

2 Solve the inequality $|3x - a| > 2|x + 2a|$, where a is a positive constant.

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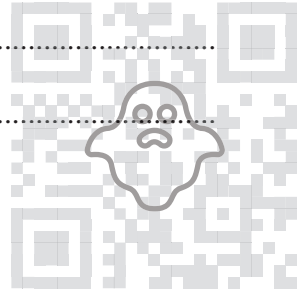
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- 3 (a) Given the complex numbers $u = a + ib$ and $w = c + id$, where a, b, c and d are real, prove that $(u + w)^* = u^* + w^*$. [2]

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- (b) Solve the equation $(z + 2 + i)^* + (2 + i)z = 0$, giving your answer in the form $x + iy$ where x and y are real. [4]

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- 5 (a) On a sketch of an Argand diagram, shade the region whose points represent complex numbers z satisfying the inequalities $|z - 3 - 2i| \leq 1$ and $\text{Im } z \geq 2$. [4]

- (b) Find the greatest value of $\arg z$ for points in the shaded region, giving your answer in degrees. [3]

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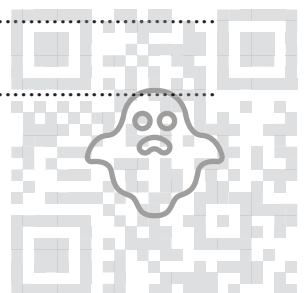
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10 With respect to the origin O , the position vectors of the points A and B are given by $\vec{OA} = \begin{pmatrix} 1 \\ 2 \\ -1 \end{pmatrix}$ and $\vec{OB} = \begin{pmatrix} 0 \\ 3 \\ 1 \end{pmatrix}$.

(a) Find a vector equation for the line l through A and B . [3]

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(b) The point C lies on l and is such that $\vec{AC} = 3\vec{AB}$.
Find the position vector of C . [2]

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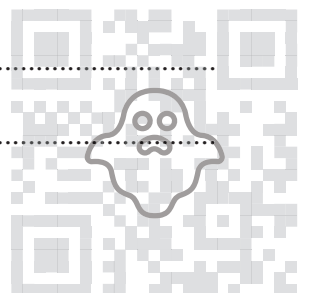
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(c) Find the possible position vectors of the point P on l such that $OP = \sqrt{14}$. [5]

Dotted lines for writing the answer.



11 The equation of a curve is $y = \sqrt{\tan x}$, for $0 \leq x < \frac{1}{2}\pi$.

(a) Express $\frac{dy}{dx}$ in terms of $\tan x$, and verify that $\frac{dy}{dx} = 1$ when $x = \frac{1}{4}\pi$. [4]

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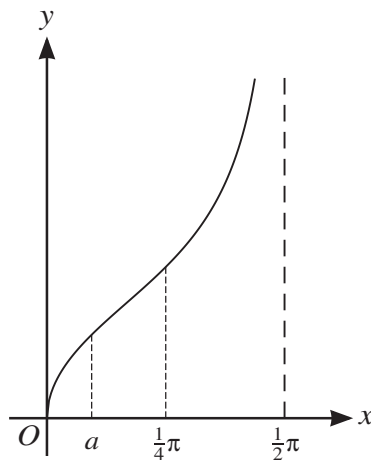
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The value of $\frac{dy}{dx}$ is also 1 at another point on the curve where $x = a$, as shown in the diagram.



(b) Show that $t^3 + t^2 + 3t - 1 = 0$, where $t = \tan a$. [4]

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(c) Use the iterative formula

$$a_{n+1} = \tan^{-1} \left(\frac{1}{3}(1 - \tan^2 a_n - \tan^3 a_n) \right)$$

to determine a correct to 2 decimal places, giving the result of each iteration to 4 decimal places. [3]

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