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| b) | Hence state the greatest and least possible values of $(5 \sin x - 3 \cos x)^2$. |
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| b) | Hence state the greatest and least possible values of $(5 \sin x - 3 \cos x)^2$. |

| (a) | Find the coordinates of this point. | [4 |
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| (b) | Determine whether the stationary point is a maximum or a minimum. | [2 |
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| $\int_3^\infty \frac{1}{(x+1)\sqrt{x}} \mathrm{d}x.$ | [6 |
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| 5 | (a) | Show that the equation |
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| | | $\cot 2\theta + \cot \theta = 2$ |
| | | can be expressed as a quadratic equation in $\tan \theta$. [3] |
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| | (b) | Hence solve the equation $\cot 2\theta + \cot \theta = 2$, for $0 < \theta < \pi$, giving your answers correct to 3 decimal places. [3] |
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| Find the values of a and b . | [6 |
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| | Given that $y = \ln(\ln x)$, show that | 1 4 | |
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| | <u>d</u> | $\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{x \ln x}.$ | [|
| | d | $ix x \ln x$ | |
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| The | variables x and t satisfy the differential | l equation | |
| | 1 | dx | |
| | $x \ln$ | $ax + t\frac{\mathrm{d}x}{\mathrm{d}t} = 0.$ | |
| It is | given that $x = e$ when $t = 2$. | | |
| 10 15 | given that $x = 0$ when $t = 2$. | | |
| (b) | answer. | | [|
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| Hence state what happens to the value of x as t tends to infinity. | [1] |
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(c)

8 The constant a is such that $\int_{1}^{a} \frac{\ln x}{\sqrt{x}} dx = 6.$

| (a) | Show that $a = \exp \left(\frac{1}{2} \right)$ | $\left(\frac{1}{\sqrt{a}}+2\right).$ | [5] |
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| $[\exp(x)$ is an alternative notation for e^x .] |
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| Us pl | Use an iterative formula based on the equation in part (a) to determine a correctlaces. Give the result of each iteration to 4 decimal places. | ct to 2 decima |
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| (a) | Show that l and m are perpendicular. |
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| (b) | Show that l and m intersect and state the position vector of the point of intersection. |
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| Show that the length of the perpendicular from the origin to the line m is $\frac{1}{3}\sqrt{5}$. [4] |
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| (a) | Find the values of a and b . | [4 |
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| (b) | State a second complex root of this equation. | [1] |
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| | the real factors of $p(x)$. | [|
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| (i) O | on a sketch of an Argand diagram, shade the region whose points represent combers z satisfying the inequalities $ z - u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | |
| (i) O | In a sketch of an Argand diagram, shade the region whose points represent columbers z satisfying the inequalities $ z - u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | |
| (i) O m | In a sketch of an Argand diagram, shade the region whose points represent columbers z satisfying the inequalities $ z - u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | omplo |
| (i) O | In a sketch of an Argand diagram, shade the region whose points represent columbers z satisfying the inequalities $ z - u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | |
| (i) O | In a sketch of an Argand diagram, shade the region whose points represent combers z satisfying the inequalities $ z - u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | |
| (i) O | In a sketch of an Argand diagram, shade the region whose points represent combers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | |
| (i) O | on a sketch of an Argand diagram, shade the region whose points represent combers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. | |
| nu (ii) Fi | on a sketch of an Argand diagram, shade the region whose points represent combers z satisfying the inequalities $ z - u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. The property of the least value of $\operatorname{Im} z$ for points in the shaded region. Give your answer in an arm. | [|
| nu (ii) Fi | umbers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. ind the least value of Im z for points in the shaded region. Give your answer in an | [|
| nu (ii) Fi | umbers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. ind the least value of Im z for points in the shaded region. Give your answer in an | [|
| nu (ii) Fi | umbers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. ind the least value of Im z for points in the shaded region. Give your answer in an | [|
| nu (ii) Fi | umbers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. ind the least value of Im z for points in the shaded region. Give your answer in an | [|
| nu (ii) Fi | umbers z satisfying the inequalities $ z-u \le \sqrt{5}$ and $\arg z \le \frac{1}{4}\pi$. ind the least value of Im z for points in the shaded region. Give your answer in an | [|