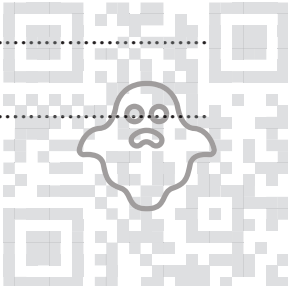


- 2 (a) Find the first three terms, in ascending powers of x , in the expansion of $(1 + ax)^6$. [1]

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- (b) Given that the coefficient of x^2 in the expansion of $(1 - 3x)(1 + ax)^6$ is -3 , find the possible values of the constant a . [4]

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3 (a) Express $5y^2 - 30y + 50$ in the form $5(y + a)^2 + b$, where a and b are constants. [2]

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(b) The function f is defined by $f(x) = x^5 - 10x^3 + 50x$ for $x \in \mathbb{R}$.
Determine whether f is an increasing function, a decreasing function or neither. [3]

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4 The first term of an arithmetic progression is 84 and the common difference is -3 .

(a) Find the smallest value of n for which the n th term is negative. [2]

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It is given that the sum of the first $2k$ terms of this progression is equal to the sum of the first k terms.

(b) Find the value of k . [3]

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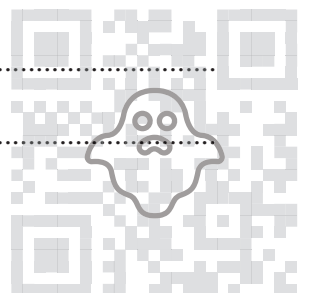
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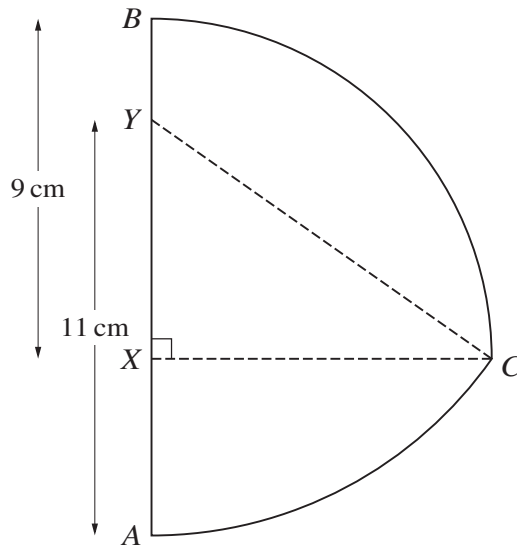
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In the diagram, X and Y are points on the line AB such that $BX = 9\text{ cm}$ and $AY = 11\text{ cm}$. Arc BC is part of a circle with centre X and radius 9 cm , where CX is perpendicular to AB . Arc AC is part of a circle with centre Y and radius 11 cm .

- (a) Show that angle $XYC = 0.9582$ radians, correct to 4 significant figures. [1]

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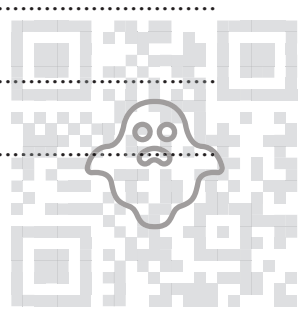
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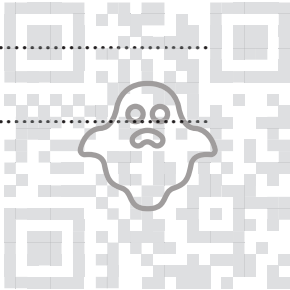
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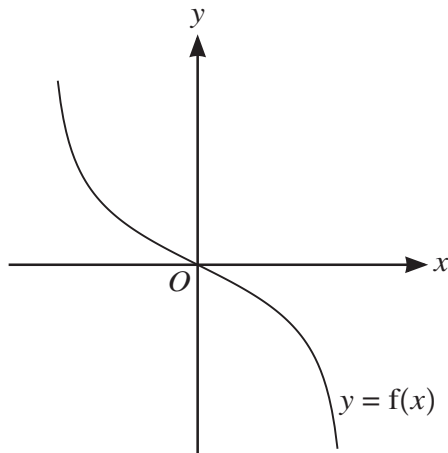
(b) Find the perimeter of ABC .

[6]

A series of horizontal dotted lines for writing the answer.



6



The diagram shows the graph of $y = f(x)$.

(a) On this diagram sketch the graph of $y = f^{-1}(x)$. [1]

It is now given that $f(x) = -\frac{x}{\sqrt{4-x^2}}$ where $-2 < x < 2$.

(b) Find an expression for $f^{-1}(x)$. [4]

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The function g is defined by $g(x) = 2x$ for $-a < x < a$, where a is a constant.

- (c) State the maximum possible value of a for which fg can be formed. [1]

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- (d) Assuming that fg can be formed, find and simplify an expression for $fg(x)$. [2]

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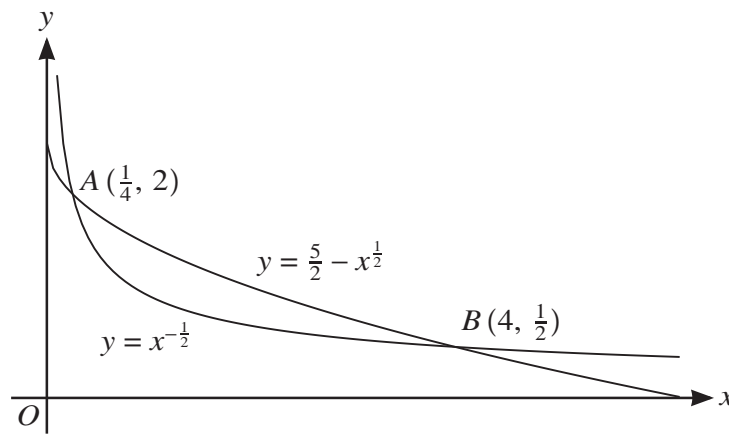
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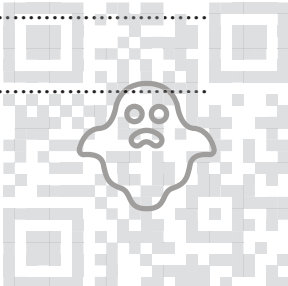
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The diagram shows the curves with equations $y = x^{-\frac{1}{2}}$ and $y = \frac{5}{2} - x^{\frac{1}{2}}$. The curves intersect at the points $A(\frac{1}{4}, 2)$ and $B(4, \frac{1}{2})$.

- (a) Find the area of the region between the two curves. [6]

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9 The line $y = 2x + 5$ intersects the circle with equation $x^2 + y^2 = 20$ at A and B .

(a) Find the coordinates of A and B in surd form and hence find the exact length of the chord AB . [7]

Dotted lines for writing the answer.



A straight line through the point $(10, 0)$ with gradient m is a tangent to the circle.

(b) Find the two possible values of m . [5]

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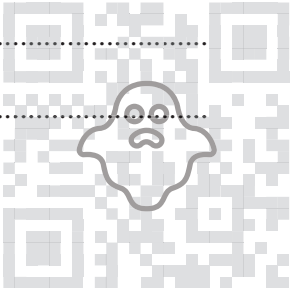
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10 A curve has equation $y = f(x)$ and it is given that

$$f'(x) = \left(\frac{1}{2}x + k\right)^{-2} - (1 + k)^{-2},$$

where k is a constant. The curve has a minimum point at $x = 2$.

(a) Find $f''(x)$ in terms of k and x , and hence find the set of possible values of k . [3]

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It is now given that $k = -3$ and the minimum point is at $(2, 3\frac{1}{2})$.

(b) Find $f(x)$. [4]

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(c) Find the coordinates of the other stationary point and determine its nature. [4]

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