

1 (a) Express $x^2 + 6x + 5$ in the form $(x + a)^2 + b$, where a and b are constants. [2]

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(b) The curve with equation $y = x^2$ is transformed to the curve with equation $y = x^2 + 6x + 5$. Describe fully the transformation(s) involved. [2]

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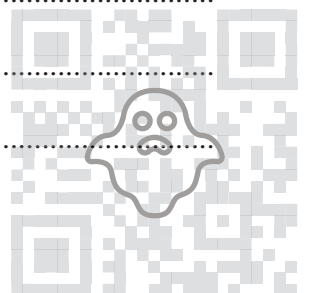
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2 The function f is defined by $f(x) = \frac{2}{(x+2)^2}$ for $x > -2$.

(a) Find $\int_1^{\infty} f(x) dx$. [3]

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(b) The equation of a curve is such that $\frac{dy}{dx} = f(x)$. It is given that the point $(-1, -1)$ lies on the curve.

Find the equation of the curve. [2]

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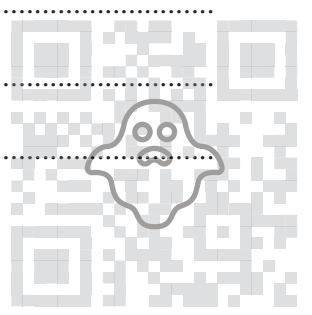
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3 Solve the equation $3 \tan^2 \theta + 1 = \frac{2}{\tan^2 \theta}$ for $0^\circ < \theta < 180^\circ$. [5]

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6 The function f is defined by $f(x) = \frac{2x}{3x-1}$ for $x > \frac{1}{3}$.

(a) Find an expression for $f^{-1}(x)$. [3]

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(b) Show that $\frac{2}{3} + \frac{2}{3(3x-1)}$ can be expressed as $\frac{2x}{3x-1}$. [2]

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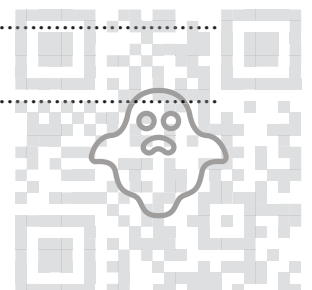
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(c) State the range of f . [1]

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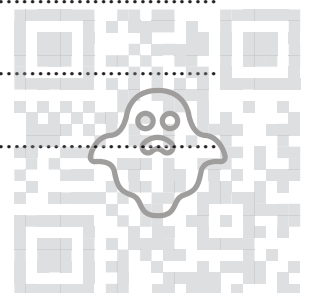
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7 The first and second terms of an arithmetic progression are $\frac{1}{\cos^2 \theta}$ and $-\frac{\tan^2 \theta}{\cos^2 \theta}$, respectively, where $0 < \theta < \frac{1}{2}\pi$.

(a) Show that the common difference is $-\frac{1}{\cos^4 \theta}$. [4]

Dotted lines for student answer.



(b) Find the exact value of the 13th term when $\theta = \frac{1}{6}\pi$.

[3]

A series of 25 horizontal dotted lines for writing the solution to the problem.

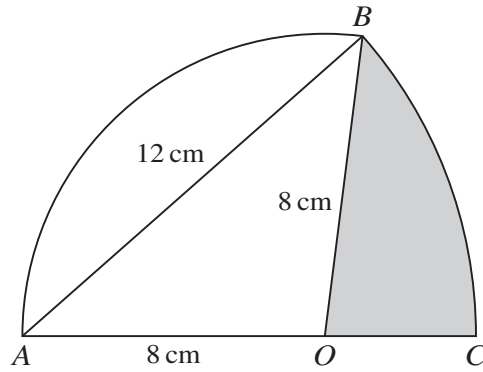


(b) Find the coordinates of the stationary point and determine the nature of the stationary point. [5]

A series of horizontal dotted lines provided for writing the answer.



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In the diagram, arc AB is part of a circle with centre O and radius 8 cm. Arc BC is part of a circle with centre A and radius 12 cm, where AOC is a straight line.

(a) Find angle BAO in radians. [2]

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(b) Find the area of the shaded region.

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(c) Find the perimeter of the shaded region.

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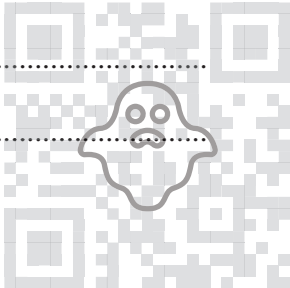
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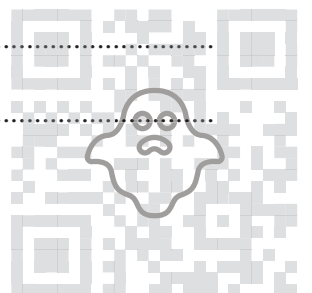


(b) It is given instead that $\int_{\frac{1}{4k^2}}^{k^2} \left(\frac{1}{k}x^{\frac{1}{2}} + x^{-\frac{1}{2}} + \frac{1}{k^2} \right) dx = \frac{13}{12}$.

Find the value of *k*.

[5]

Series of horizontal dotted lines for writing the solution.



11 A circle with centre C has equation $(x - 8)^2 + (y - 4)^2 = 100$.

(a) Show that the point $T(-6, 6)$ is outside the circle. [3]

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Two tangents from T to the circle are drawn.

(b) Show that the angle between one of the tangents and CT is exactly 45° . [2]

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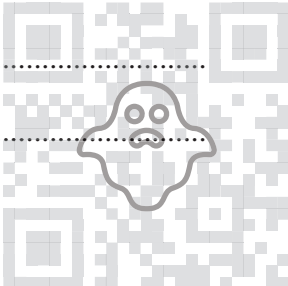
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The two tangents touch the circle at A and B .

- (c) Find the equation of the line AB , giving your answer in the form $y = mx + c$. [4]

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- (d) Find the x -coordinates of A and B . [3]

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