

- 3 A line with equation $y = mx - 6$ is a tangent to the curve with equation $y = x^2 - 4x + 3$.

Find the possible values of the constant m , and the corresponding coordinates of the points at which the line touches the curve. [6]

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4 (a) Show that the equation

$$\frac{\tan x + \sin x}{\tan x - \sin x} = k,$$

where k is a constant, may be expressed as

$$\frac{1 + \cos x}{1 - \cos x} = k. \quad [2]$$

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(b) Hence express $\cos x$ in terms of k . [2]

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(c) Hence solve the equation $\frac{\tan x + \sin x}{\tan x - \sin x} = 4$ for $-\pi < x < \pi$. [2]

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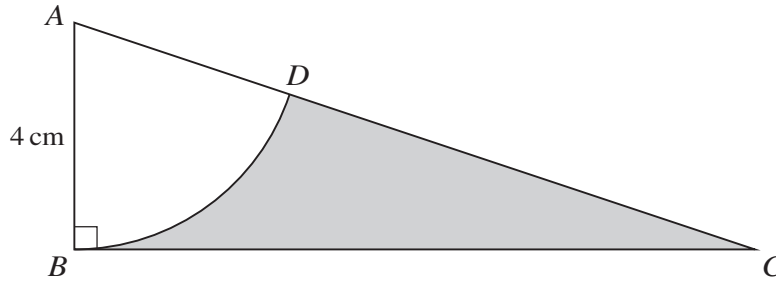
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The diagram shows a triangle ABC , in which angle $ABC = 90^\circ$ and $AB = 4$ cm. The sector ABD is part of a circle with centre A . The area of the sector is 10 cm^2 .

- (a) Find angle BAD in radians. [2]

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- (b) Find the perimeter of the shaded region. [4]

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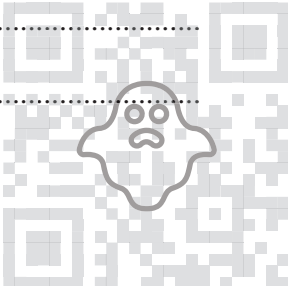
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6 Functions f and g are both defined for $x \in \mathbb{R}$ and are given by

$$f(x) = x^2 - 2x + 5,$$

$$g(x) = x^2 + 4x + 13.$$

- (a) By first expressing each of $f(x)$ and $g(x)$ in completed square form, express $g(x)$ in the form $f(x + p) + q$, where p and q are constants. [4]

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- (b) Describe fully the transformation which transforms the graph of $y = f(x)$ to the graph of $y = g(x)$. [2]

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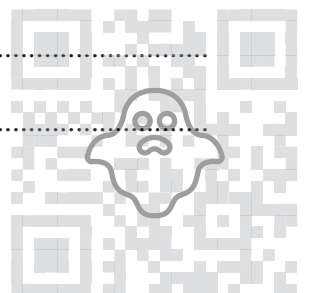
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8 Functions f and g are defined as follows:

$$f : x \mapsto x^2 - 1 \text{ for } x < 0,$$

$$g : x \mapsto \frac{1}{2x + 1} \text{ for } x < -\frac{1}{2}.$$

(a) Solve the equation $fg(x) = 3$.

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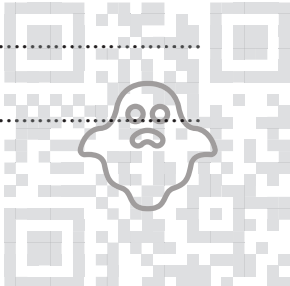
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(b) Find an expression for $(fg)^{-1}(x)$.

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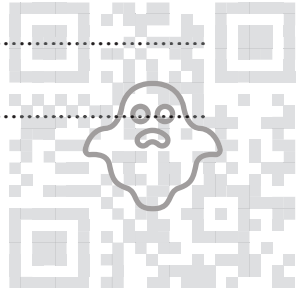


9 (a) A geometric progression is such that the second term is equal to 24% of the sum to infinity.

Find the possible values of the common ratio.

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10 Points $A(-2, 3)$, $B(3, 0)$ and $C(6, 5)$ lie on the circumference of a circle with centre D .

(a) Show that angle $ABC = 90^\circ$. [2]

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(b) Hence state the coordinates of D . [1]

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(c) Find an equation of the circle. [2]

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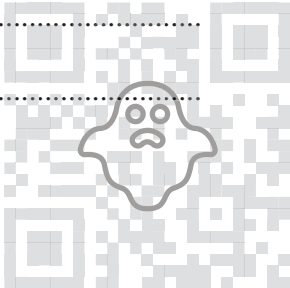
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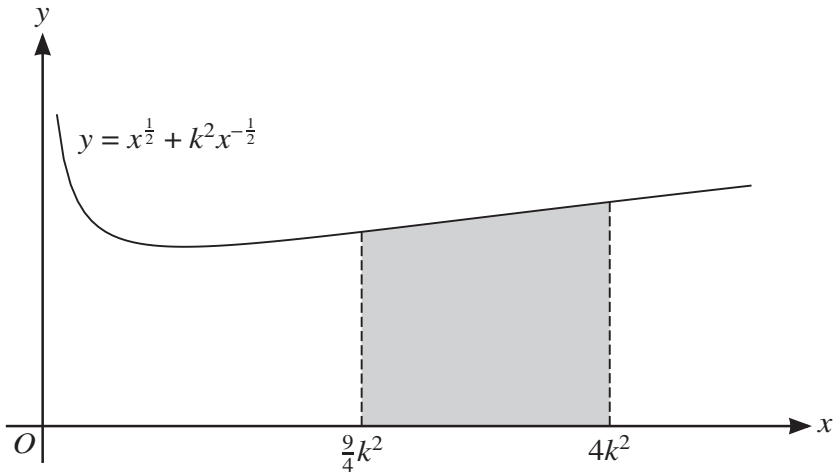
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The diagram shows part of the curve with equation $y = x^{\frac{1}{2}} + k^2x^{-\frac{1}{2}}$, where k is a positive constant.

- (a) Find the coordinates of the minimum point of the curve, giving your answer in terms of k . [4]

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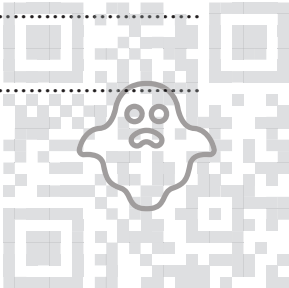
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The tangent at the point on the curve where $x = 4k^2$ intersects the y -axis at P .

- (b) Find the y -coordinate of P in terms of k . [4]

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The shaded region is bounded by the curve, the x -axis and the lines $x = \frac{9}{4}k^2$ and $x = 4k^2$.

- (c) Find the area of the shaded region in terms of k . [3]

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