| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(i) | Binomial | B1 |  |
|  | $n=500$ and $p=\frac{1}{150}$ or 0.00667 | B1 | Or B $\left(500, \frac{1}{150}\right)$ for B1B1 |
|  |  | 2 |  |
| 1(ii) | Poisson | B1 |  |
|  | $n$ large and mean $=\frac{10}{3}$ or 3.3 or better, which is $<5$ | B1 | Accept $n>50$ |
|  |  | 2 |  |
| 1 (iii) | $1-e^{-\frac{10}{3}} \times\left(1+\frac{10}{3}+\frac{\left(\frac{10}{3}\right)^{2}}{2}\right)$ | M1 | $1-\mathrm{P}(X=0,1,2)$ |
|  | $=1-0.353$ | A1 | Correct expression with $\lambda=3.3$ or better |
|  | $=0.647$ (3 sf) | A1 | SC Use of Binomial scores B1 for 0.648. Use of Normal scores B1 for $0.67(0)$ to 0.677 |
|  |  | 3 |  |


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| :---: | :---: | :---: | :---: |
| 2(i)(a) | Assume standard deviation for the region is 7.1 | B1 | Or standard deviation is same as for whole population OE |
|  | $\frac{63.2-65.2}{\frac{7.1}{\sqrt{n}}}=-2.182$ | M1 | Attempt to find correct equation (accept +2.182 ) |
|  | $n=\{-2.182 \times 7.1 \div(-2)\}^{2}$ | A1 | Any correct expression for $n$ or $\sqrt{n}$. SOI |
|  | $n=60$ | A1 | CWO. Must be an integer |
|  |  | 4 |  |
| 2(i)(b) | $\mathrm{H}_{0}$ : population mean $($ or $\mu)=65.2$ <br> $\mathrm{H}_{1}$ : population mean $($ or $\mu)<65.2$ | B1 | Not just 'mean' |
|  | $2.182>1.751$ | M1 | Or valid area comparison. |
|  | There is evidence that animals are shorter in this region | A1 | CWO. No contradictions |
|  |  | 3 |  |
| 2(ii) | Population unknown or population not given as normal | B1 | Allow population not normal. Accept distribution of X unknown. |
|  |  | 1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3(i) | $\operatorname{est}(\mu)=\frac{25110}{50} \quad(=502.2)$ | B1 |  |
|  | $\operatorname{est}\left(\sigma^{2}\right)=\frac{50}{49}\left(\frac{12610300}{50}-\frac{25110}{50}\right)^{2}\left(=\frac{50}{49} \times \frac{58}{50}=1.1836\right)$ | M1 | OE |
|  | $1.18(3 \mathrm{sf}) \text { or } \frac{58}{49}$ | A1 | Accept SD $=1.0879$ |
|  | $z=2.054$ or 2.055 | B1 |  |
|  | $502.2 \pm z \times \frac{\sqrt{1.1836^{\prime}}}{\sqrt{50}}$ | M1 | Must be of correct form. |
|  | 501.9 to 502.5 (1dp) | A1 | CWO. Must be in interval. <br> SC accept use of biased variance (1.16) for M1 A1 |
|  |  | 6 |  |
| 3(ii) | More confident or $z$ would be greater, Hence wider. | B1 | OE <br> Reason needed |
|  |  | 1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | $\begin{aligned} & \frac{1}{2} \times a \times \frac{a}{2}=1 \text { or } \frac{1}{2} \int_{0}^{a} x \mathrm{~d} x=1 \\ & \frac{a^{2}}{4}=1 \mathrm{OE} \end{aligned}$ | M1 | Attempt at triangle area or integral $\mathrm{f}(x)$ and $=1$, |
|  | $a=2$ | A1 |  |
|  |  | 2 |  |
| 4(ii) | $\frac{1}{2} \int_{0}^{2} x^{2} \mathrm{~d} x$ | M1 | Attempt integral $x \mathrm{f}(x)$ |
|  | $=\left[\frac{x^{3}}{6}\right]_{0}^{2}$ | M1 | Correct integral and limits 0 to their ' $a$ ' |
|  | $\left(=\frac{8}{6}\right)=\frac{4}{3}$ | A1 | $\begin{aligned} & \text { AG } \\ & \text { CWO } \end{aligned}$ |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(iii) | $P\left(X<\frac{4}{3}\right)=\frac{1}{2} \int_{0}^{\frac{4}{3}} x \mathrm{~d} x$ | M1 | Attempt integral $\mathrm{f}(x)$ between correct limits |
|  | $=\frac{4}{9}$ | A1 | or $\frac{5}{9}$ |
|  | $P(E(X)<X<m)=\frac{1}{2}-\frac{4}{4}^{\prime}$ | M1 | or $\frac{5}{9}-\frac{1}{2}$ |
|  | $\frac{1}{18}$ | A1 |  |
|  | Alternative method for question 4(iii) |  |  |
|  | Attempt to find $m$ | M1 |  |
|  | $m=\sqrt{2}$ | A1 |  |
|  | Integrate $\mathrm{f}(x)$ between $\frac{4}{3}$ and ' $\sqrt{2}$ ' | M1 |  |
|  | $\frac{1}{18}$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | mean $=3250$ var. $=61$ | B1 | Or mean $=325$ var. $=\frac{6.1}{10}$ |
|  | $\frac{3240-3250}{\sqrt{61}}(=-1.280)$ | M1 | Standardise with their values (no mixed methods) |
|  | $\phi('-1.280 ')=1-\phi(' 1.280)$ | M1 | Area consistent with their figures |
|  | 0.100 | A1 | Allow 0.1 |
|  |  | 4 |  |
| 5(ii) | $\mathrm{E}(\mathrm{D})=325-2 \times 167=-9$ | B1 | Accept $\pm 9$ |
|  | $\operatorname{Var}(\mathrm{D})=6.1+2^{2} \times 5.6(=28.5)$ | B1 |  |
|  | $\frac{0-(-9)}{\sqrt{28.5}}(=1.686)$ | M1 | Standardising with their values. Must have a combination attempt on denominator and $\sqrt{ }$ |
|  | $1-\phi\left(' 1.686{ }^{\prime}\right)$ | M1 | Area consistent with their figures |
|  | 0.0459 | A1 |  |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6 (i) | $\mathrm{H}_{0}$ : Pop mean ( or $\lambda$ or $\mu$ ) is 1.1 <br> $\mathrm{H}_{1}$ : Pop mean (or $\lambda$ or $\mu$ ) is more than 1.1 | B1 |  |
|  | $\mathrm{P}(X \geqslant 4)=1-\mathrm{e}^{-1.1}\left(1+1.1+\frac{1.1^{2}}{2}+\frac{1.1^{3}}{3!}\right)$ | M1 | Correct expression for either $\mathrm{P}(X \geqslant 4)$ or $\mathrm{P}(X \geqslant 5)$ |
|  | 0.0257 | A1 | Correct value of either $\mathrm{P}(X \geqslant 4)$ or $\mathrm{P}(X \geqslant 5)$ |
|  | $\mathrm{P}(X \geqslant 5)=0.0257-\mathrm{e}^{-1.1} \times \frac{1.1^{4}}{4!}=0.00544$ | B1 | B1 for the other value <br> (Note use of $\mathrm{P}(X<4)=0.9743$ and $\mathrm{P}(X<5)=0.99456$ can score only if comparison with 0.99 seen) |
|  | $0.00544<0.01<0.0257$ | M1 | OE stated (valid comparison) |
|  | There is evidence mean has increased | B1 | SC P $(X \geqslant 6)=0.000968$ M1A1 <br> Conclusion |
|  |  | 6 |  |
| 6(ii) | Concluding mean has increased when it has not | B1 | In context |
|  | '0.00544' | B1FT | FT their $\mathrm{P}(X \geqslant 5)$, dep $<0.01$ |
|  |  | 2 |  |
| 6(iii) | $\mathrm{e}^{-7.0}\left(1+7+\frac{7^{2}}{2}+\frac{7^{3}}{3!}+\frac{7^{4}}{4!}\right)$ | M1 | Correct expression for $\mathrm{P}(X \leqslant 4 \mid \lambda=7.0)$ |
|  | 0.173 (3 sf) | A1 |  |
|  |  | 2 |  |

