| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(i) | $\frac{120}{300}=0.4$ | B1 | OE |
|  |  | 1 |  |
| 1(ii) | $\mathrm{P}($ male $) \times \mathrm{P}($ not piano $)=\frac{160}{300} \times \frac{225}{300}\left(\frac{8}{15} \times \frac{3}{4}\right)=\frac{2}{5}$ | M1 | $\mathrm{P}(\mathrm{M}) \times \mathrm{P}\left(\mathrm{P}^{\prime}\right)$ seen Can be unsimplified but the events must be named in a product |
|  | As $\mathrm{P}($ male $\cap$ not piano $)$ also $=\frac{120}{300}=\frac{2}{5}$ The events are Independent | A1 | Numerical comparison and correct conclusion |
|  | Alternative method for question 1(ii) |  |  |
|  | $\mathrm{P}(\text { male } \cap \text { not piano })=\frac{120}{300} ; \mathrm{P}(\text { not piano })=\frac{225}{300}$ | M1 | $\mathrm{P}\left(\mathrm{M} \mid \mathrm{P}^{\prime}\right)$ or $\mathrm{P}\left(\mathrm{P}^{\prime} \mid \mathrm{M}\right)$ unsimplified seen with their probs with correctly named events |
|  | $\mathrm{P}(\mathrm{M} \mid$ not piano $)=\frac{\frac{120}{300}}{\frac{225}{300}}=\frac{120}{225}=\frac{8}{15}=\mathrm{P}($ male $)$ <br> or <br> $\mathrm{P}($ not piano $\mid \mathrm{M})=\frac{\frac{120}{300}}{\frac{160}{300}}=\frac{120}{160}=\frac{3}{4}=\mathrm{P}($ not piano $)$ <br> Therefore the events are Independent | A1 | Numerical comparison with $\mathrm{P}(\mathrm{M})$ or $\mathrm{P}\left(\mathrm{P}^{\prime}\right)$ and correct conclusion |
|  |  | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2(i) | $\frac{9!}{2!3!}=30240$ | B1 | 9 ! Divided by at least one of 2 ! or 3! |
|  |  | B1 | Exact value |
|  |  | 2 |  |
| 2(ii) | $\begin{aligned} & D_{-------} \text {R: } \frac{7!}{2!2!}=1260 \\ & D_{-------} \text {O: } \frac{7!}{3!}=840 \end{aligned}$ | B1 | 7! Seen alone or as numerator in a term, can be multiplied not + or - |
|  |  | B1 | One term correct, unsimplified |
|  | Total $=2100$ | B1 | Final answer |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3(i) | $\begin{aligned} & 3 A 2 D 2 M:{ }^{6} \mathrm{C}_{3} \times{ }^{5} \mathrm{C}_{2} \times{ }^{4} \mathrm{C}_{2}(=1200) \\ & 4 A 2 D 1 M:{ }^{6} \mathrm{C}_{4} \times{ }^{5} \mathrm{C}_{2} \times{ }^{4} \mathrm{C}_{1}(=600) \\ & 3 A 3 D 1 M:{ }^{6} \mathrm{C}_{3} \times{ }^{5} \mathrm{C}_{3} \times{ }^{4} \mathrm{C}_{1}(=800) \end{aligned}$ | M1 | ${ }^{6} \mathrm{C}_{x} \times{ }^{5} \mathrm{C}_{y} \times{ }^{4} \mathrm{C}_{z}, x+y+z=7$ |
|  |  | A1 | 2 correct products, allow unsimplified |
|  |  | M1 | Summing their totals for 3 correct scenarios only |
|  | Total $=2600$ | A1 | Correct answer SC1 ${ }^{6} \mathrm{C}_{3} \times{ }^{5} \mathrm{C}_{2} \times{ }^{4} \mathrm{C}_{1} \times{ }^{9} \mathrm{C}_{1}=7200$ |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: | ---: |
| 3 (ii) | ${ }^{7} \mathrm{C}_{4} \times 1$ | $\mathbf{B 1}$ | ${ }^{7} \mathrm{C}_{3}$ or ${ }^{7} \mathrm{C}_{4}$ seen anywhere |
|  | 35 | $\mathbf{B 1}$ |  |
|  |  | $\mathbf{2}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | $\mathrm{P}(h<148)=0.67$ | B1 | $z= \pm 0.44$ seen |
|  | $\frac{h-148}{8}=0.44$ | M1 | $z \text {-value }= \pm \frac{(h-148)}{8}$ |
|  | $151.52 \approx 152$ | A1 | CAO |
|  |  | 3 |  |
| 4(ii) | $\mathrm{P}(144<X<152)=\mathrm{P}\left(\frac{144-148}{8}<Z<\frac{152-148}{8}\right)$ | M1 | Using $\pm$ standardisation formula for either 144 or 152, $\mu=148, \sigma=8$ and no continuity correction, allow $\sigma^{2}$ or $\sqrt{ } \sigma$ |
|  | $=\mathrm{P}\left(-\frac{1}{2}<Z<\frac{1}{2}\right)=0.6915-(1-0.6915)=2 \times 0.6915-1$ | M1 | Correct final area legitimately obtained from phi $\left(\right.$ their $\left.z_{2}\right)-\operatorname{phi}\left(\right.$ their $\left.z_{1}\right)$ |
|  | $=0.383$ | A1 | Final probability answer |
|  | $0.383 \times 120=45.96$ <br> Accept 45 or 46 only | B1FT | Their prob (to 3 or 4 sf ) $\times 120$, rounded to a whole number or truncated |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | Correct labels and scales | B1 | Axes labelled 'cumulative frequency' (or cf) and 'time (ort) [in] min(utes)', linear scales from 0 to 90 and 0 to 200 with at least 3 values marked on each axis. |
|  | 7 correctly plotted points above upper boundaries joined in a curve or line segments | B1 | $\begin{aligned} & (0,0) ;(10,16) ;(20,50) ;(30,106) ;(50,146) ;(70,176) \text {; } \\ & (90,200) \end{aligned}$ |
|  |  | 2 |  |
| 5(ii) | 29 | B1 | $28 \leqslant$ median $\leqslant 30$ |
|  |  | 1 |  |
| 5(iii) | 120 seen | M1 | For seeing 120 in a calculation or marked on the graph |
|  | 37 | A1FT | $36 \leqslant$ Ans $\leqslant 39$ or FT from their graph SC1 unsupported answer in range |
|  |  | 2 |  |
| 5(iv) | Frequencies 163456403024 | B1 | Seen. Allow unsimplified |
|  | $\text { Est. Mean }=\frac{5 \times 16+15 \times 34+25 \times 56+40 \times 40+60 \times 30+80 \times 24}{200}$ | M1 | At least 4 correct midpoints $(5,15,25,40,60,80)$ used in a calculation |
|  | $\frac{7310}{200}$ | M1 | Summing products of their 6 mid-points (not lower or upper bound or class width) $\times$ their frequencies / 200 (or their $\sum \mathrm{f}$ ), unsimplified |
|  | 36.55 | A1 | Accept 36.6 |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(i) | $\mathrm{P}(\mathrm{RR})=\frac{3}{8} \times \frac{2}{7}=\frac{3}{28}$ | B1 | OE |
|  |  | 1 |  |
| 6(ii) | $\begin{aligned} & \mathrm{P}(\mathrm{RW})+\mathrm{P}(\mathrm{WR}) \\ & \frac{3}{8} \times \frac{5}{7}+\frac{5}{8} \times \frac{3}{7} \end{aligned}$ | M1 | Method shown, numerical calculations identified, may include replacements |
|  | $=\frac{15}{28}$ | A1 | AG, Fully correct calculations |
|  | Alternative method for question 6(ii) |  |  |
|  | $\begin{aligned} & 1-(\mathrm{P}(\mathrm{RR})+\mathrm{P}(\mathrm{WW}) \\ & 1-\left(\frac{3}{28}+\frac{5}{8} \times \frac{4}{7}\right) \end{aligned}$ | M1 | Method shown, numerical calculations identified, may include replacements |
|  | $=\frac{15}{28}$ | A1 | AG, Fully correct calculations |
|  |  | 2 |  |
| 6(iii) | $\mathrm{P}(\text { first red } \mid \text { second red })=\frac{\text { their }(\mathbf{i})}{\text { their }(\mathbf{i})+\frac{5}{8} \times \frac{3}{7}}=\frac{\frac{3}{8} \times \frac{2}{7}}{\frac{3}{8} \times \frac{2}{7}+\frac{5}{8} \times \frac{3}{7}}=\frac{\frac{3}{28}}{\frac{21}{56}}$ | M1 | Conditional probability formula used consistent with their probabilities or correct |
|  | $=\frac{2}{7}$ | A1 | OE |
|  |  | 2 |  |



| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 7 7(i)(a) | $\mathrm{P}(0,1,2)={ }^{6} \mathrm{C}_{0} 0.3^{0} 0.7^{6}+{ }^{6} \mathrm{C}_{1} 0.3^{1} 0.7^{5}+{ }^{6} \mathrm{C}_{2} 0.3^{2} 0.7^{4}$ | $\mathbf{M 1}$ | Binomial term of form ${ }^{6} \mathrm{C}_{x} p^{x}(1-p)^{6-x} \quad 0<p<1$ <br> any $p, x \neq 6,0$ |
|  | $0.1176 \ldots+0.3025 \ldots+0.3241 \ldots$ | $\mathbf{A 1}$ | Correct unsimplified answer |
|  | 0.744 | $\mathbf{A 1}$ | Correct final answer |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i)(b) | $\mathrm{P}($ support neither choir $)=1-(0.3+0.45)=0.25$ | M1 | $0.25^{n}$ seen alone, $1<n \leqslant 6$ |
|  | $\begin{aligned} & P(6 \text { support neither choir })=0.25^{6} \\ & =0.000244 \text { or } \frac{1}{4096} \end{aligned}$ | A1 | Correct final answer |
|  |  | 2 |  |
| 7(ii) | $\begin{aligned} & \text { Mean }=240 \times 0.25=60 \\ & \text { Variance }=240 \times 0.25 \times 0.75=45 \end{aligned}$ | B1FT | Correct unsimplified 240p and 240pq where $\mathrm{p}=$ their P (support neither choir) or 0.25 |
|  | $\mathrm{P}(X<50)=\mathrm{P}\left(Z<\frac{49.5-60}{\sqrt{45}}\right)=\mathrm{P}(Z<-1.565)$ | M1 | Substituting their $\mu$ and $\sigma$ (condone $\sigma^{2}$ ) into the $\pm$ Standardisation Formula with a numerical value for ' 49.5 '. |
|  |  | M1 | Using continuity correction 49.5 or 50.5 within a standardisation expression |
|  | $1-0.9412$ | M1 | Appropriate area $\Phi$ from standardisation formula $\mathrm{P}(\mathrm{z}<\ldots)$ in final solution, $(<0.5$ if $z$ is $-\mathrm{ve},>0.5$ if $z$ is +ve$)$ |
|  | 0.0588 | A1 | Correct final answer |
|  |  | 5 |  |

