| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(i) | $1+6 y+15 y^{2}$ | B1 | CAO |
|  |  | 1 |  |
| 1(ii) | $1+6\left(p x-2 x^{2}\right)+15\left(p x-2 x^{2}\right)^{2}$ | M1 | SOI. Allow $6 \mathrm{C} 1 \times 1^{5}\left(p x-2 x^{2}\right), 6 \mathrm{C} 2 \times 1^{4}\left(p x-2 x^{2}\right)^{2}$ |
|  | $\left(15 p^{2}-12\right)\left(x^{2}\right)=48\left(x^{2}\right)$ | A1 | 1 term from each bracket and equate to 48 |
|  | $p=2$ | A1 | SC: A1 $p=4$ from $15 p-12=48$ |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 2 | $(y=)\left[(x-3)^{2}\right][-2]$ | $\begin{gathered} \text { *B1 } \\ \text { DB1 } \end{gathered}$ | DB1 dependent on 3 in 1st bracket |
|  | $x-3=( \pm) \sqrt{y+2}$ or $y-3=( \pm) \sqrt{x+2}$ | M1 | Correct order of operations |
|  | $\left(\mathrm{g}^{-1}(x)\right)=3+\sqrt{x+2}$ | A1 | Must be in terms of $x$ |
|  | Domain (of $\mathrm{g}^{-1}$ ) is $(x)>-1$ | B1 | Allow $(-1, \infty)$. Do not allow $y>-1$ or $\mathrm{g}(x)>-1$ or $\mathrm{g}^{-1}(x)>-1$ |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 3 | $\frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}+2 x-8$ | B1 |  |
|  | Set to zero (SOI) and solve | M1 |  |
|  | (Min) $a=-2,($ Max $) ~ b=4 / 3 .-$ in terms of $a$ and $b$. | $\begin{aligned} & \mathbf{A 1} \\ & \mathbf{A 1} \end{aligned}$ | Accept $a \geqslant-2, \quad b \leqslant \frac{4}{3}$ <br> SC: A1 for $a>-2, \quad b<\frac{4}{3}$ or for $-2<x<\frac{4}{3}$ |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(i) | Angle $C A O=\frac{\pi}{3}$ | B1 |  |
|  |  | 1 |  |
| 4(ii) | $(\text { Sector } A O C)=\frac{1}{2} r^{2} \times \text { their } \frac{\pi}{3}$ | M1 | SOI |
|  | $(\triangle A B C)=\frac{1}{2}(r)(2 r) \sin \left(\text { their } \frac{\pi}{3}\right) \text { or } \frac{1}{2}(2 r)(r) \frac{\sqrt{3}}{2} \text { or } \frac{1}{2}(r)(r) \sqrt{3}$ | M1 | For M1M1, their $\frac{\pi}{3}$ must be of the form $k \pi$ where $0<k<1 / 2$ |
|  | $(\triangle A B C)=\frac{1}{2}(r)(2 r) \sin \left(\frac{\pi}{3}\right) \text { or } \frac{1}{2}(2 r)(r) \frac{\sqrt{3}}{2} \text { or } \frac{1}{2}(r)(r) \sqrt{3}$ | A1 | All correct |
|  | $r^{2}\left(\frac{\sqrt{3}}{2}\right)-\frac{1}{2} r^{2}\left(\frac{\pi}{3}\right)$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | $S=28 x^{2}, V=8 x^{3}$ | B1B1 | SOI |
|  | $7 V^{\frac{2}{3}}=7 \times 4 x^{2}=S$ | B1 | AG, WWW |
|  |  | 3 |  |
| 5(ii) | $\left(\frac{\mathrm{d} S}{\mathrm{~d} V}\right)=\frac{14 V^{-\frac{1}{3}}}{3}=\frac{14}{30}$ SOI when $V=1000$ | $\begin{array}{r} \text { *M1 } \\ \mathbf{A 1} \end{array}$ | Attempt to differentiate <br> For M mark $\left(\frac{\mathrm{d} S}{\mathrm{~d} V}\right)$ to be of form $k V^{-\frac{1}{3}}$ |
|  | $\left(\frac{\mathrm{d} V}{\mathrm{~d} t}=\frac{\mathrm{d} S}{\mathrm{~d} t} \times \frac{\mathrm{d} V}{\mathrm{~d} S}\right)$ OE used with $\frac{\mathrm{d} S}{\mathrm{~d} t}=2$ and $\frac{1}{\text { their } \frac{14}{30}}$ | DM1 |  |
|  | $\frac{30}{7}$ or 4.29 | A1 | OE |
|  | Alternative method for question 5(ii) |  |  |
|  | $V=\frac{S^{\frac{3}{2}}}{7 \sqrt{7}} \rightarrow\left(\frac{\mathrm{~d} V}{\mathrm{~d} S}\right)=\frac{3}{2} \times S^{\frac{1}{2}} \times \frac{1}{7 \sqrt{7}}=\frac{30}{14}$ SOI when $S=700$ | $\begin{array}{r} \text { *M1 } \\ \mathbf{A 1} \end{array}$ | Attempt to differentiate <br> For M mark $\left(\frac{\mathrm{d} V}{\mathrm{~d} S}\right)$ to be of form $k S^{\frac{1}{2}}$ |
|  | $\left(\frac{\mathrm{d} V}{\mathrm{~d} t}=\frac{\mathrm{d} S}{\mathrm{~d} t} \times \frac{\mathrm{d} V}{\mathrm{~d} S}\right)$ OE used with $\frac{\mathrm{d} S}{\mathrm{~d} t}=2$ and $\frac{1}{\text { their } \frac{14}{30}}$ | DM1 |  |
|  | $\frac{30}{7}$ or 4.29 | A1 | OE |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(ii) | Alternative method for question 5(ii) |  |  |
|  | Attempt to find either $\frac{\mathrm{d} V}{\mathrm{~d} x}$ or $\left(\frac{\mathrm{d} S}{\mathrm{~d} x}\right.$ and $\left.\frac{\mathrm{d} V}{\mathrm{~d} S}\right)$ together with either $\frac{\mathrm{d} x}{\mathrm{~d} t}$ or $x$ | *M1 |  |
|  | $\frac{\mathrm{d} V}{\mathrm{~d} x}=24 x^{2}$ or $\left(\frac{\mathrm{d} S}{\mathrm{~d} x}=56 x\right.$ and $\left.\frac{\mathrm{d} V}{\mathrm{~d} S}=\frac{3 x}{7}\right), \frac{\mathrm{d} x}{\mathrm{~d} t}=\frac{1}{140}$ or $x=5(\mathrm{~A} 1)$ | A1 |  |
|  | Correct method for $\frac{\mathrm{d} V}{\mathrm{~d} t}$ | DM1 |  |
|  | $\frac{30}{7}$ or 4.29 | A1 | OE |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(i) | $3 k x-2 k=x^{2}-k x+2 \rightarrow x^{2}-4 k x+2 k+2(=0)$ | B1 | $k x$ terms combined correctly-implied by correct $b^{2}-4 a c$ |
|  | Attempt to find $b^{2}-4 a c$ | M1 | Form a quadratic equation in $k$ |
|  | 1 and $-\frac{1}{2}$ | A1 | SOI |
|  | $k>1, k<-\frac{1}{2}$ | A1 | Allow $x>1, x<-1 / 2$ |
|  |  | 4 |  |
| 6(ii) | $y=3 x-2, \quad y=-\frac{3}{2} x+1$ | M1 | Use of their $k$ values (twice) in $y=3 k x-2 k$ |
|  | $3 x-2=-\frac{3}{2} x+1$ OR $y+2=2-2 y$ | M1 | Equate their tangent equations OR substitute $y=0$ into both lines |
|  | $x=\frac{2}{3}, \rightarrow y=0$ in one or both lines | A1 | Substitute $x=\frac{2}{3}$ in one or both lines |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | $3 \cos ^{4} \theta+4\left(1-\cos ^{2} \theta\right)-3(=0)$ | M1 | Use $s^{2}=1-c^{2}$ |
|  | $3 x^{2}+4(1-x)-3(=0) \rightarrow 3 x^{2}-4 x+1(=0)$ | A1 | AG |
|  |  | 2 |  |
| 7(ii) | Attempt to solve for $x$ | M1 | Expect $x=1,1 / 3$ |
|  | $\cos \theta=( \pm) 1,( \pm) 0.5774$ | A1 | Accept $( \pm)\left(\frac{1}{\sqrt{3}}\right)$ SOI |
|  | $(\theta=) 0^{\circ}, 180^{\circ}, 54.7^{\circ}, 125.3^{\circ}$ | A3,2,1,0 | A2,1,0 if more than 4 solutions in range |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| $8(\mathrm{i})$ | $(2 x-1)^{\frac{1}{2}}<2$ or $3(2 x-1)^{\frac{1}{2}}<6$ | M1 | SOI |
|  | $2 x-1<4$ | A1 | SOI |
|  | $\frac{1}{2}<x<\frac{5}{2}$ | A1 A1 | Allow 2 separate statements |
|  | $8($ ii) | $\mathrm{f}(x)=\left[3(2 x-1)^{3 / 2} \div\left(\frac{3}{2}\right) \div(2)\right][-6 x](+\mathrm{c})$ | B1 B1 |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 9(i) | $\frac{5 k-6}{3 k}=\frac{6 k-4}{5 k-6} \rightarrow(5 k-6)^{2}=3 k(6 k-4)$ | M1 | OR any valid relationship |
|  | $25 k^{2}-60 k+36=18 k^{2}-12 k \rightarrow 7 k^{2}-48 k+36$ | A1 | AG |
|  |  | 2 |  |
| 9(ii) | $k=\frac{6}{7}, 6$ | B1B1 | Allow $0.857(1)$ for $\frac{6}{7}$ |
|  | When $k=\frac{6}{7}, r=-\frac{2}{3}$ | B1 | Must be exact |
|  | When $k=6, r=\frac{4}{3}$ | B1 |  |
|  |  | 4 |  |
| 9 (iii) | Use of $S_{\infty}=\frac{a}{1-r}$ with $r=$ their $-\frac{2}{3}$ and $a=3 \times$ their $\frac{6}{7}$ | M1 | Provided $0<\mid$ their $-2 / 3 \mid<1$ |
|  | $\frac{18}{7} \div\left(1+\frac{2}{3}\right)=\frac{54}{35}$ or 1.54 | A1 | FT if $0.857(1)$ has been used in part (ii). |
|  |  | 2 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 10(i) | $\mathbf{A X}=\left(\begin{array}{l}6 \\ 2 \\ 3\end{array}\right)$, and one of $\mathbf{A B}=\left(\begin{array}{c}18 \\ 6 \\ 9\end{array}\right), \mathbf{X B}=\left(\begin{array}{c}12 \\ 4 \\ 6\end{array}\right), \mathbf{B} \mathbf{X}=\left(\begin{array}{c}-12 \\ -4 \\ -6\end{array}\right)$ | B1B1 |  |
|  | State $\mathbf{A B}=3 \mathbf{A X}\left(\right.$ or $\mathbf{X B}=2 \mathbf{A X}$ or $\mathbf{A B}=\frac{3}{2} \mathbf{X B}$ etc $)$ hence straight line OR $\frac{\mathbf{A X} \cdot \mathbf{A B}}{\|\mathbf{A X}\|\|\mathbf{A B}\|}=1(\rightarrow \theta=0) \text { or } \frac{\mathbf{A X} \cdot \mathbf{B X}}{\|\mathbf{A X}\|\|\mathbf{B X}\|}=-1(\rightarrow \theta=180)$ <br> hence straight line | B1 | WWW <br> A conclusion (i.e. a straight line) is required. |
|  |  | 3 |  |
| 10(ii) | $\mathbf{C X}=\left(\begin{array}{c}-3 \\ 6 \\ 2\end{array}\right)$ | B1 |  |
|  | CX.AX $=-18+12+6$ | M1 |  |
|  | $=0$ (hence $C X$ is perpendicular to $A X$ ) | A1 |  |
|  |  | 3 |  |
| 10(iii) | $\|\mathbf{C X}\|=\sqrt{3^{2}+6^{2}+2^{2}},\|\mathbf{A B}\|=\sqrt{18^{2}+6^{2}+9^{2}}$ <br> Both attempted | M1 |  |
|  | Area $\triangle A B C=\frac{1}{2} \times$ their $21 \times$ their $7=73 \frac{1}{2}$ | M1A1 | Accept answers which round to 73.5 |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 11(i) | $\frac{\mathrm{d} y}{\mathrm{~d} x}=-2(x-1)^{-3}$ | B1 |  |
|  | When $x=2, m=-2 \rightarrow$ gradient of normal $=-\frac{1}{m}$ | M1 | $m$ must come from differentiation |
|  | Equation of normal is $y-3=1 / 2(x-2) \rightarrow y=1 / 2 x+2$ | A1 | AG Through $(2,3)$ with gradient $-\frac{1}{m}$. Simplify to AG |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 11(ii) | $(\pi) \int y_{1}{ }^{2}(\mathrm{~d} x),(\pi) \int y_{2}{ }^{2}(\mathrm{~d} x)$ | *M1 | Attempt to integrate $y^{2}$ for at least one of the functions |
|  | $\begin{aligned} & (\pi) \int\left(\frac{1}{2} x+2\right)^{2} \text { or }\left(\frac{1}{4} x^{2}+2 x+4\right) \\ & (\pi) \int\left((x-1)^{-4}+4(x-1)^{-2}+4\right) \end{aligned}$ | A1A1 | A1 for $\left(\frac{1}{2} x+2\right)^{2}$ depends on an attempt to integrate this form later |
|  | $\begin{aligned} & (\pi)\left[\frac{2}{3}\left(\frac{1}{2} x+2\right)^{3} \text { or } \frac{1}{12} x^{3}+x^{2}+4 x\right] \\ & (\pi)\left[\frac{(x-1)^{-3}}{-3}+\frac{4(x-1)^{-1}}{-1}+4 x\right] \end{aligned}$ | A1A1 | Must have at least 2 terms correct for each integral |
|  | ( $\pi$ ) $\left\{18-\frac{125}{12}\right.$ or $\left.\frac{2}{3}+4+8-\left(\frac{1}{12}+1+4\right)\right\}\left\{\frac{-1}{24}-2+12-\left(\frac{-1}{3}-4+8\right)\right\}$ | DM1 | Apply limits to at least 1 integrated expansion |
|  | Attempt to add 2 volume integrals (or 1 volume integral + frustum) $\pi\left\{7 \frac{7}{12}+6 \frac{7}{24}\right\}$ | DM1 |  |
|  | $13 \frac{7}{8} \pi \text { or } \frac{111}{8} \pi \text { or } 13.9 \pi \text { or } 43.6$ | A1 | $\frac{2}{3}+4+8-\left(\frac{1}{12}+1+4\right) \frac{-1}{24}-2+12-\left(\frac{-1}{3}-4+8\right)$ |
|  |  | 8 |  |

