

| Question | Answer | Marks | Guidance |
|----------|---|-----------|--|
| 1 | $e^{-2.3} \left(\frac{2.3^2}{2} + \frac{2.3^3}{3!} + \frac{2.3^4}{4!} \right)$ | M2 | M1 for one term wrong or one end error or $1 - P(2, 3, 4)$ |
| | = 0.585 (3 sf) | A1 | |
| | | 3 | |

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|----------|--|-----------|--|
| 2(i) | $z = 1.96$ | B1 | seen |
| | $330.1 \pm z \times \frac{4.8}{\sqrt{180}}$ | M1 | Must be of correct form. Any z |
| | = 329.4 to 330.8 (1 dp) | A1 | Must be to 1 dp. Must be an interval. |
| | | 3 | |
| 2(ii) | Yes, because vol of all cans not stated to be normal | B1 | Or Yes, population not stated to be normal |
| | | 1 | |

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| 3 | $E(T) = 2 \times 250 + 5 \times 160 (= 1300)$ | B1 | |
| | $\text{Var}(T) = 2 \times 10 + 5 \times 9 (= 65)$ | B1 | |
| | $\frac{1310 - 1300}{\sqrt{65}} (= 1.240)$ | M1 | Standardise using their values (must come from a combination attempt). Ignore cc |
| | $1 - \phi(1.240^2)$ | M1 | Correct area consistent with their working |
| | $= 0.1075$ | A1 | Allow 0.107 to 0.108 (no errors seen) |
| | | 5 | |

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| 4(i) | $\int_0^a \frac{k}{(x+1)^2} dx = 1$ | M1 | Any attempt integ f(x) and = 1. Ignore limits |
| | $-\left[\frac{k}{x+1}\right]_0^a = 1$ $-k\left(\frac{1}{a+1} - 1\right) = 1$ | M1 | Attempt subst correct limits into correct integral |
| | $k \times \frac{a}{a+1} = 1$ and $k = \frac{a+1}{a}$ AG | A1 | No errors seen |
| | | 3 | |

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| 4(ii) | Max time allowed by model (for runners to finish) | B1 | Allow: All runners finish in time a or less or Longest time (taken by any runner) oe |
| | | 1 | |
| 4(iii) | $\frac{a+1}{a} \int_0^{0.5} \frac{1}{(x+1)^2} dx = \frac{3}{4}$ | M1 | Attempt integ $f(x)$ and $= \frac{3}{4}$; ignore limits oe. Condone missing / incorrect k |
| | $-\frac{a+1}{a} \left[\frac{1}{(x+1)} \right]_0^{0.5} = \frac{3}{4}$ $-\frac{a+1}{a} \left(\frac{2}{3} - 1 \right) = \frac{3}{4}$ | M1 | Attempt subst correct limits into correct integral. Condone missing / incorrect k |
| | $a = 0.8$ oe | A1 | |
| | | 3 | |

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|----------|---|-----------|---|
| 5(i) | $\hat{\mu} = \frac{126}{70}$ or $\frac{9}{5}$ or 1.8 oe | B1 | |
| | $\Sigma x^2 f = 286$ | B1 | Seen or implied |
| | $\text{Est}(\sigma^2) = \frac{70}{69} \left(\frac{\Sigma x^2 f}{70} - '1.8'^2 \right)$ | M1 | oe attempted |
| | $= 0.858$ or $296 / 345$ | A1 | Note: Final answer for var 0.846 (biased) and no working implies B1 for 286 |
| | | 4 | |

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|----------|--|-------------|---|
| 5(ii) | $H_0: \mu = 1.9$ $H_1: \mu < 1.9$ | B1 | Or ‘pop mean’; not just ‘mean’ |
| | $\frac{1.8-1.9}{\sqrt{\frac{0.858}{70}}}$ | M1 | Standardise with their values from (i). Must have sqr 70. No SD / Var mix |
| | = -0.903 | A1 | Accept \pm |
| | $0.903 < 1.645$ | M1 | comp 1.645 allow comp 1.96 if $H_1: \mu \neq 1.9$ or comp $1 - \phi(0.903) = 0.182$ or 0.183 with 0.05 (or 0.025 if $H_1: \mu \neq 1.9$) |
| | No evidence that mean no courts in S is less than in N | A1ft | No contradictions. ft their 0.903, but not comp 1.96 i.e. no ft for a 2 tail test Accept cv method: cv = 1.718 M1A1 1.718 < 1.8 M1 conclusion A1 (cv centred on 1.8 gives 1.982 M1A1 and M1 for 1.982 > 1.9 A1 conclusion) |
| | | 5 | |
| 5(iii) | Type II because H_0 was not rejected | B1ft | ft their conclusion, i.e. if H_0 rejected, ‘Type I because H_0 rejected’ B1 Answer must be consistent with their conclusion. No conclusion in (ii) will score B0 |
| | | 1 | |

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| 6(i) | $H_0: p = 0.15$ $H_1: p < 0.15$ ($N(60 \times 0.15, 60 \times 0.15 \times 0.85)$) $= N(9, 7.65)$ | B1 | Accept $H_0: \mu = 9$ $H_1: \mu < 9$ Use of Normal approximation: ($N(0.15, \frac{0.15 \times 0.85}{60})$) $= N(0.15, 0.002125)$ |
| | $\frac{6.5 - '9'}{\sqrt{7.65}}$ | M1 | For standardising (or $\frac{\frac{6.5 - 0.15}{60} - 0.15}{\sqrt{0.002125}} = -0.904$) Allow wrong or no cc |
| | $= -0.904$ | A1 | Accept \pm |
| | '0.904' < 1.282 | M1 | Valid comparison of z values or $\phi(' -0.904') = 0.183 > 0.1$ ft their 0.904 |
| | No evidence train late less often | A1ft | Use of Bin (60,0.15) to give $\Pr (<= 6) = 0.1848$ M1A1 Valid comparison with 0.1 M1 Conclusion A1ft |
| | | 5 | |
| 6(ii) | $0.1 + z \times \sqrt{\frac{0.1 \times 0.9}{60}} = 0.150$ | M1 | For $\sqrt{(0.1 \times 0.9 / 60)}$ seen |
| | | M1 | for $0.1 + z \times \dots = 0.150$ or $2z \dots = 0.1$ |
| | $z = 1.291$ | A1 | |
| | $\phi('1.291') (= 0.90(16))$ | M1 | for correct method to find α |
| | $\alpha = 80$ | A1ft | ft their z. Must be a +ve non-zero integer < 100 |
| | | 5 | |

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| 7(i) | $e^{-5.6} \times \frac{5.6^3}{3!}$ | M1 | Allow any λ |
| | = 0.108 (3 sf) | A1 | |
| | | 2 | |
| 7(ii) | $P(X=2 \text{ \& } Y=1) = e^{-2.1} \times \frac{2.1^2}{2} \times e^{-3.5} \times 3.5$ (0.2700 \times 0.10569 = 0.028538) | M1 | |
| | $\frac{P(X=2 \text{ \& } Y=1)}{P(X+Y=3)}$ attempted = $\frac{0.028538}{0.108234}$ | M1 | For attempt at fraction with their (i) as denominator or $\frac{2.1^2}{2} \times 3.5 \div \frac{5.6^3}{3}$ M2 |
| | = 0.264 (3 sf) | A1 | |
| | | 3 | |

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| 7(iii) | $\text{Var}(X) = 2.1$ | B1 | soi |
| | $\bar{X} \sim N(2.1, \frac{2.1}{100})$ or $N(210, 210)$ | B1 | soi B1 for $N(2.1, \dots)$ |
| | | B1 | B1 for $\frac{2.1}{100}$ oe Standardise with their values. Allow with or without cc or with incorrect cc |
| | $\frac{2.2-2.1}{\frac{\sqrt{2.1}}{\sqrt{100}}}$ oe $(220 - 210) / \sqrt{210}$ (= 0.690) | M1 | or $\frac{2.2+0.5+100-2.1}{\frac{\sqrt{2.1}}{\sqrt{100}}}$ or $(220.5 - 210) / \sqrt{210}$ (= 0.725) no mixed methods |
| | $1 - \phi('0.690')$ | M1 | Correct area consistent with their working or $1 - \phi('0.725')$ |
| | = 0.245 (3 sf) | A1 | = 0.234 (3 sf) |
| | | 6 | |