| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 1(i) | State or imply non-modular equation $(9 x-2)^{2}=(3 x+2)^{2}$ or pair of linear equations | B1 |  |
|  | Attempt solution of quadratic equation or of 2 linear equations | M1 |  |
|  | Obtain 0 and $\frac{2}{3}$ | A1 | SC: B1 for one correct solution |
|  |  | 3 |  |
| 1(ii) | Apply logarithms and use power law for $3^{y}=k$ where $k>0$ | M1 | Must be using their answers to part (i) |
|  | Obtain -0.369 | A1 |  |
|  |  | 2 |  |


| Question | Answer | Marks |  |
| :---: | :--- | ---: | ---: |
| 2 | Integrate to obtain form $k \ln (2 x+1)$ | M1 |  |
|  | Obtain correct $3 \ln (2 x+1)$ | A1 |  |
|  | Use subtraction law of logarithms correctly | M1 | Dependent on first M1 |
|  | Use power law of logarithms correctly | M1 | Dependent on first M1 |
|  | Confirm $\ln 125$ | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 3 | State $\frac{1}{\cos ^{2} \theta}=\frac{3}{\sin \theta}$ or $1+\tan ^{2} \theta=\frac{3}{\sin \theta}$ | $\mathbf{B 1}$ |  |
|  | Produce quadratic equation in $\sin \theta$ | M1 | Dependent on B1 |
|  | Solve 3-term quadratic equation to find value between -1 and 1 for $\sin \theta$ | M1 | Dependent on first M1 |
|  | Obtain $\sin \theta=\frac{1}{6}(-1+\sqrt{37})$ and hence 57.9 | $\mathbf{A 1}$ |  |
|  | Obtain 122.1 and no others between 0 and 180 | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{5}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 4 (i) | Substitute -2 and simplify | M1 |  |
|  | Obtain $16-16+8+24-32$ and hence zero and conclude | A1 | AG; necessary detail needed |
|  | 4(ii) | Attempt division by $x+2$ to reach at least partial quotient $x^{3}+k x$ or use of <br> identity or inspection | $\mathbf{2}$ |
|  | Obtain $x^{3}+2 x-16$ | A1 |  |
|  | Equate to zero and obtain $x=\sqrt[3]{16-2 x}$ | A1 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 4 (iii) | Use iteration process correctly at least once | M1 |  |
|  | Obtain final answer 2.256 | $\mathbf{A 1}$ |  |
|  | Show sufficient iterations to 6 sf to justify answer or show a sign change in the <br> interval (2.2555, 2.2565) | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $5(\mathrm{i})$ | Use product rule to differentiate $y$ obtaining $k_{1} \mathrm{e}^{2 t}+k_{2} t \mathrm{e}^{2 t}$ | M1 |  |
|  | Obtain correct $3 \mathrm{e}^{2 t}+6 \mathrm{e}^{2 t}$ | $\mathbf{A 1}$ |  |
|  | State derivative of $x$ is $1+\frac{1}{t+1}$ | B1 |  |
|  | Use $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{\mathrm{d} y}{\mathrm{~d} t} / \frac{\mathrm{d} x}{\mathrm{~d} t}$ with $t=0$ to find gradient | M1 |  |
|  | Obtain $y=\frac{3}{2} x$ or equivalent | $\mathbf{A 1}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(ii) | Equate $\frac{\mathrm{d} y}{\mathrm{~d} x}$ or $\frac{\mathrm{d} y}{\mathrm{dt}}$ to zero and solve for $t$ | M1 | Allow full marks if correct solution is obtained but $\frac{\mathrm{d} x}{\mathrm{~d} t}$ is incorrect |
|  | Obtain $t=-\frac{1}{2}$ | A1 |  |
|  | Obtain $x=-1.19$ | A1 |  |
|  | Obtain $y=-0.55$ | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 6 (i) | Use $y$ values $2, \sqrt{2.5}, 1$ or equivalents | B1 |  |
|  | Use correct formula, or equivalent, with $h=\frac{1}{2} \pi$ and three $y$ values | M1 |  |
|  | Obtain $\frac{1}{2} \times \frac{1}{2} \pi(2+2 \sqrt{2.5}+1)$ or equivalent and hence 4.84 | A1 |  |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 6(ii) | State or imply volume is $\int \pi\left(1+3 \cos ^{2} \frac{1}{2} x\right) \mathrm{d} x$ | B1 | Allow if $\pi$ appears later; condone omission of $\mathrm{d} x$ |
|  | Use appropriate identity to express integrand in form $k_{1}+k_{2} \cos x$ | M1 |  |
|  | Obtain $\int \pi\left(\frac{5}{2}+\frac{3}{2} \cos x\right) \mathrm{d} x$ or $\int\left(\frac{5}{2}+\frac{3}{2} \cos x\right) \mathrm{d} x$ | A1 | Condone omission of $\mathrm{d} x$ |
|  | Integrate to obtain $\pi\left(\frac{5}{2} x+\frac{3}{2} \sin x\right)$ or $\frac{5}{2} x+\frac{3}{2} \sin x$ | A1 |  |
|  | Obtain $\frac{5}{2} \pi^{2}$ with no errors seen | A1 |  |
|  |  | 5 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| $7(\mathrm{i})$ | State expression of form $k_{1} \cos 2 x+k_{2} \sin 2 x$ | M1 |  |
|  | State correct $2 \cos 2 x-6 \sin 2 x$ | A1 |  |
|  |  | $\mathbf{2}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(ii) | State $R=\sqrt{40}$ or $6.324 \ldots$ | B1 FT | Following their derivative |
|  | Use appropriate trigonometry to find $\alpha$ | M1 |  |
|  | Obtain 1.249... | A1 | Allow $\alpha$ in degrees at this point |
|  | Equate their $R \cos (2 x+\alpha)$ to 3 and find $\cos ^{-1}(3 \div R)$ | *M1 |  |
|  | Carry out correct process to find one value of $\alpha$ | M1 | Dependent on *M1, allow for $-0.086 \ldots$. |
|  | Obtain 1.979 | A1 |  |
|  | Carry out correct process to find second value of $\alpha$ within the range | M1 | Dependent on *M1 |
|  | Obtain 3.055 | A1 | Allow 3.056 |
|  |  | 8 |  |

