

Question	Answer	Marks	Guidance
1(a)(i)	Po(2.54)	M1	seen or implied Po(2540 × 0.001)
	$1 - e^{-2.54}(1 + 2.54)$	M1	any $\lambda$ Allow 1 end error
	= 0.721 (3 sf)	A1	
		3	
1(a)(ii)	$n$ large and $p$ small (or $np (= 2.54) < 5$ )	B1	$n > 50, p < 0.1$
		1	
1(b)	$\mu = 5.6$	B1	
	$\sigma = 2.37$ (3 sf)	B1	Accept $\sqrt{5.6}$
		2	

Question	Answer	Marks	Guidance
2(i)	$4820 \pm z \times \frac{1420}{\sqrt{125}}$	M1	Must be a $z$ value
	$z = 2.326$	B1	Accept 2.326 - 2.329
	4524/4525 to 5115/5116 or 4520 to 5120 (3 sf)	A1	Must be an interval
		3	

Question	Answer	Marks	Guidance
2(ii)	$\bar{x} = 4840$	<b>B1</b>	or width = 280 or half width = 140
	$4840 + 1.96 \times \frac{1420}{\sqrt{n}} = 4980$ OE	<b>M1</b>	or $140 = 1.96 \times \frac{1420}{\sqrt{n}}$ OE
	$n = 395$	<b>A1</b>	CAO must be an integer
		<b>3</b>	

Question	Answer	Marks	Guidance
3(i)	$\bar{m} = \frac{98.2}{100} = 0.982$	<b>B1</b>	Accept either
	$s = \sqrt{\frac{100}{99} \times \sqrt{\frac{104.52}{100} - 0.982^2}}$ (= 0.28582) or var = 0.08169	<b>M1</b>	
	$H_0$ : Pop mean mass = 1.01 $H_1$ : Pop mean mass < 1.01	<b>B1</b>	not just 'mean', but allow just ' $\mu$ '
	$\pm \frac{0.982 - 1.01}{\frac{0.28582}{\sqrt{100}}}$	<b>M1</b>	$\pm \frac{0.982 - 1.01}{\frac{0.284387}{\sqrt{100}}}$ <b>M1</b>
	= -0.980 (3 sf) accept $\pm$	<b>A1</b>	= -0.985 (3 sfs) accept $\pm$ <b>A1</b>
	Comp with $z = -1.645$ (or areas $0.1635 > 0.05$ )	<b>M1</b>	Valid comparison of $z$ 's or area's
	No evidence that (mean) mass is less than 1.01	<b>A1 FT</b>	Correct conclusion FT their $z$
		<b>7</b>	

Question	Answer	Marks	Guidance
3(ii)	Distr of $X$ normal (so distr of $\bar{X}$ normal) Must state or imply No	<b>B1</b>	X/parent population
		<b>1</b>	

Question	Answer	Marks	Guidance
4(i)	$k \int_0^a \frac{1}{\sqrt{x}} dx = 1$	<b>M1</b>	Attempt int $f(x)$ and = 1 ignore limits
	$(2k[x^{0.5}]_0^a = 1)$ $2ka^{0.5} = 1$ or $a = \frac{1}{4k^2}$	<b>A1</b>	OE; a correct eqn in $k$ & $a$ after sub limits
	$k \int_0^a \frac{x}{\sqrt{x}} dx = 3$	<b>M1</b>	Attempt int $xf(x)$ and = 3
	e.g. $\frac{2}{3}ka^{1.5} = 3$ or $a^3 = \frac{81}{4k^2}$	<b>A1</b>	OE; a correct eqn in $k$ and $a$ after sub limits
	e.g. $a^2 = 81$ or e.g. $k^2 = \frac{81}{4 \times 9^3}$	<b>M1</b>	Attempt eliminate one letter
	$a = 9$	<b>A1</b>	Convincingly obtained
	e.g. $k = \frac{9}{54}$ $k = \frac{1}{6}$ AG	<b>A1</b>	
		<b>7</b>	

Question	Answer	Marks	Guidance
4(ii)	$\frac{1}{6} \int_0^m \frac{1}{\sqrt{x}} dx = 0.5$ OE	M1	Attempt int f(x), unknown limit and = 0.5
	$\frac{1}{3} m^{0.5} = 0.5$	A1	a correct equn in $m$ after sub limits
	$m = 2.25$	A1	
		3	

Question	Answer	Marks	Guidance
5(i)	$E(X - Y) = 56 - 43$ (= 13)	B1	
	$\text{Var}(X - Y) = 6^2 + 5^2$ (= 61)	M1	
	$\frac{0 - 13}{\sqrt{61}}$ (= -1.664)	M1	Ignore any attempted cc/no SD/var mixes. var must be attempt at a combination
	$1 - \phi(-1.664) = \phi(1.664)$	M1	For area consistent with their working
	= 0.952 (3 sf)	A1	Similar scheme for use of $Y - X$
		5	

Question	Answer	Marks	Guidance
5(ii)	$E(M) = 56 + 1.5(43)$ (= 120.5)	<b>B1</b>	
	$\text{Var}(M) = 6^2 + 1.5^2 \times 5^2$ (= 92.25)	<b>M1</b>	
	$\frac{135 - 120.5}{\sqrt{92.25}}$ (= 1.510)	<b>M1</b>	Ignore any attempted cc/no SD/var mixes. var must be attempt at a combination
	$1 - \phi(1.510)$	<b>M1</b>	For area consistent with their working
	= 0.0655 or 0.0656 or 6.55% or 6.56% (3 sf) As final answer	<b>A1</b>	Allow 6.6% or 6.5% or 7% if correct working seen
		<b>5</b>	

Question	Answer	Marks	Guidance
6(i)	$H_0$ : Pop mean no. defectives = 5.15 $H_1$ : Pop mean no. defectives < 5.15	<b>B1</b>	or '= 1.03 (per day)' not just 'mean', but allow just ' $\lambda$ ' or ' $\mu$ '
	$P(X \leq 2)$	<b>M1</b>	Attempted. Any one term error/end error/incorrect $\lambda$ /expression 1-...
	$= e^{-5.15} (1 + 5.15 + \frac{5.15^2}{2})$	<b>M1</b>	Correct expression attempted
	= 0.113	<b>A1</b>	
	Comp with 0.1	<b>M1</b>	Valid comparison
	No evidence to believe mean no. of defectives has decreased	<b>A1 FT</b>	Correct conclusion (FT their value) No contradictions
		<b>6</b>	

Question	Answer	Marks	Guidance
6(ii)	BOTH $P(X \leq 1) = e^{-5.15} (1 + 5.15) (= 0.0357)$ AND $P(X \leq 2) = e^{-5.15} (1 + 5.15 + \frac{5.15^2}{2}) = (0.113)$	<b>B1*</b>	(Could be seen in (i))
	Comp either with 0.1	<b>DB1</b>	One comparison with 0.01 (could be seen in (i))
	$P(\text{Type I error}) = 0.0357$ (3 sf)	<b>B1</b>	
		<b>3</b>	
6(iii)	Actually mean = 1.03 but conclude that mean < 1.03	<b>B1</b>	Mean no. of defectives not reduced, but conclude that it is reduced.
		<b>1</b>	