

| Question | Answer | Marks | Guidance |
|----------|---|-------|---|
| 1 | $0.2dv/dt = te^{-v}$ | M1 | Uses Newton's Second Law to set up a differential equation. Allow a for dv/dt . |
| | $\int e^v dv = 5 \int t dt$ leading to $e^v = 5t^2/2 (+ c)$ | M1 | Separates the variables and integrates. |
| | $e^v - 1 = 2.5t^2$ | A1 | Substitutes $t = 0, v = 0$. |
| | $v(2) = \ln 11 = 2.4$ | A1 | |
| | | 4 | |

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| 2 | $0.15W + 0.3(60 - W) = 0.25 \times 60$ | M1A1 | Attempts to take moments about the base of the cone. W = weight of the cone. |
| | $W = 20 \text{ N}$ | A1 | |
| | | 3 | |

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|----------|--|-------|---|
| 3(i) | $0.4v dv/dx = 0.4g \sin 30 - 0.2v^2$ | M1 | Uses Newton's Second Law down the plane. Allow a for vdv/dx . |
| | $v dv/dx = 5 - 0.5v^2$ | A1 | AG |
| | | 2 | |
| 3(ii) | $\int v / (5 - 0.5v^2) dv = \int x dx$ | M1 | Separates the variables and attempts to integrate. |
| | $-\ln(5 - 0.5v^2) = x (+ c)$ | A1 | |
| | $c = -\ln 5 [5 - 0.5v^2 = 5e^{-x}]$ | M1 | Puts $x = 0, v = 0$ to find c and attempts to solve for v . |
| | $v = \sqrt{(10 - 10e^{-x})}$ | A1 | |
| | | 4 | |

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| 4(i) | $e = \sqrt{(0.5^2 + 1.2^2)} - 1 = 0.3$ | B1 | |
| | $T = 39 \times 0.3/1$ | M1 | Uses $T = \lambda x/L$. |
| | $mg = 2 \times (39 \times 0.3/1) \times 0.5/1.3$ | M1 | Resolves vertically. |
| | $m = 0.9$ | A1 | AG |
| | | 4 | |
| 4(ii) | $E = \sqrt{(1.6^2 + 1.2^2)} - 1 = 1 \text{ m}$ | B1 | E = extension when the particle comes to instantaneous rest. |
| | $EE = 39 \times 1^2/(2 \times 1)$ or $39 \times 0.3^2/(2 \times 1)$ | B1 | |
| | $0.9v^2/2 + 0.9g(1.6 - 0.5)$ $= 2[39 \times 1^2/(2 \times 1) - 39 \times 0.3^2/(2 \times 1)]$ | M1A1 | Set up a 4 term energy equation involving EE , KE and PE . |
| | $v = 7.54 \text{ m s}^{-1}$ | A1 | |
| | | 5 | |

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| 5(i) | $OG = 2 \times 0.8\sin(\pi/4)/(3\pi/4)$ (0.48016...m) | B1 | |
| | $AG^2 = (0.8\sin45)^2 + (0.8\cos45 - OG)^2$ OR $AG^2 = 0.8^2 + OG^2 - 2 \times 0.8 \times OG\cos45$ | M1 | Uses Pythagoras's Theorem OR the cosine formula. |
| | $AG = 0.572(11...) \text{ m}$ | A1 | |
| | | 3 | |
| 5(ii) | $\tan B A G = (0.8\cos45 - OG)/(0.8\sin45)$ | M1 | Uses trigonometry to find angle BAG . |
| | $BAG = 8.5965^\circ = 8.6(0)^\circ$ | A1 | |
| | $W \times AG = 12 \times 2 \times 0.8\sin45 \times \sin B A G$ | M1 | Takes moments about A . |
| | $0.572W = 12 \times 2 \times 0.8\sin45 \times \sin 8.6$ | A1FT | |
| | $W = 3.55 \text{ N}$ | A1 | |
| | | 5 | |

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| 6(i) | $T = 0.2 \times 2.5^2 / (0.4 + e)$ | B1 | Uses Newton's Second Law towards the centre of the circle. |
| | $T = 8e/0.4$ | B1 | Uses $T = \lambda x/L$. |
| | $1.25/(0.4 + e) = 20e \rightarrow 20e^2 + 8e - 1.25 = 0$ | M1 | Eliminates T to find e . |
| | $e = 0.12(0) \text{ m}$ | A1 | |
| | | 4 | |
| 6(ii) | $0.2v^2/2 = 2[8x^2/(2 \times 0.4)]$ | B1 | Uses $KE = 2EE$. |
| | $0.2v^2/(0.4 + x) = 8x/0.4$ | B1 | Uses $T = \lambda x/L$ and $T = mv^2/r$. |
| | | M1 | Attempts to solve the 2 equations to find v or x . |
| | $x = 0.4$ and $v = 5.66$ or $4\sqrt{2}$ | A1A1 | |
| | | 5 | |

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| 7(i) | $U_H = 18\cos 30$ and $U_V = 18\sin 30 + 2g (=29)$ | B1 | |
| | $U = \sqrt{[(18\cos 30)^2 + 29^2]}$ or $\tan\theta = 29/(18\cos 30)$ | M1 | Uses Pythagoras's Theorem and trigonometry. |
| | $U = 32.9(24..) \text{ m s}^{-1}$ | A1 | |
| | $\theta = 61.7^\circ$ | A1 | |
| | | 4 | |
| 7(ii) | $v^2 = 38^2 - (18\cos 30)^2 = (+/-29)^2 + 2gh$ | M1 | Uses 2 ways to find v , the vertical velocity at the ground and equates. |
| | $h = 18$ | A1 | |
| | OR $mgh + m \times 32.924^2/2 = m \times 38^2/2$ | M1 | |
| | $h = 18$ | A1 | |
| | | 2 | |

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| 7(iii) | $-\sqrt{[(38^2 - (18 \cos 30)^2]} = 29 - gt$ | M1 | Uses $v = u + at$ for first part of flight. |
| | $t = 6.36(6)$ | A1 | |
| | $v = \sqrt{[20^2 - (18 \cos 30)^2]} = 12.5(3)$ $-12.5(3) = 12.5(3) - gt'$ | M1 | Uses $v = u + at$ for second part of flight. |
| | $t' = 2.50(6)$ | A1 | |
| | $T (= 6.366 + 2.506) = 8.87$ | A1 | |
| | | | 5 |