| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 1 | Use subtraction or addition property of <br> logarithms | *M1 |  |
|  | Obtain $\frac{3 x+1}{x+2}=\mathrm{e}$ or equivalent with no <br> presence of logarithm | A1 |  |
|  | Use correct process to solve equation | D11 |  |
|  | Obtain $\frac{2 \mathrm{e}-1}{3-\mathrm{e}}$ or exact equivalent | $\mathbf{4}$ |  |
|  |  |  |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 2 | Use $\cos 2 \theta=2 \cos ^{2} \theta-1$ | B1 |  |
|  | Obtain $10 \cos ^{3} \theta=4$ or equivalent | B1 |  |
|  | Use correct process to find at least one value of <br> $\theta$ from equation of form $k_{1} \cos ^{3} \theta=k_{2}$ | $\mathbf{M 1}$ |  |
|  | Obtain 42.5 | A1 |  |
|  | Obtain 317.5 and no others between 0 and 360 | $\mathbf{A 1}$ |  |
|  |  | $\mathbf{5}$ |  |


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| :---: | :---: | :---: | :---: |
| 3 | Take logarithms of both sides and apply power law | M1 | Condone incorrect inequality signs until final answer. The first 6 marks are for obtaining the correct critical values. |
|  | Obtain $2 x<\frac{\ln 80}{\ln 1.3}$ or equivalent using $\log _{10}$ | A1 |  |
|  | Obtain $x=8.35 \ldots$ | A1 |  |
|  | State or imply non-modulus inequality $(3 x-1)^{2}>(3 x-10)^{2}$ or corresponding equation or linear equation $3 x-1=-(3 x-10)$ | B1 |  |
|  | Attempt solution of inequality or equation (obtaining 3 terms when squaring each bracket or solving linear equation with signs of $3 x$ different) | M1 |  |
|  | Obtain $x=\frac{11}{6}$ or $x=1.83 \ldots$ | A1 |  |
|  | Conclude $1.83<x<8.35$ | A1 |  |
|  |  | 7 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 4(a) | Obtain integrand of form $a \sec ^{2} \theta+b$ | M1 |  |
|  | Obtain correct $5 \sec ^{2} \theta-1$ | A1 |  |
|  | Integrate to obtain form $a \tan \theta+b \theta$ | M1 |  |
|  | Obtain $5 \tan \theta-\theta+c$ | A1 |  |
|  |  | 4 |  |
| 4(b) | Obtain integral of form $k \ln (3 x+1)$ | *M1 |  |
|  | Apply limits and obtain $\frac{2}{3} \ln (3 a+1)=\ln 16$ | A1 |  |
|  | Obtain equation with no presence of $\ln$ | DM1 |  |
|  | Obtain 21 | A1 |  |
|  |  | 4 |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 5(i) | Substitute $x=-2$ and equate to zero | *M1 |  |
|  | Substitute $x=\frac{1}{2}$ and equate to 40 | *M1 |  |
|  | Obtain $-8 a+4 b-64=0$ and $\frac{1}{8} a+\frac{1}{4} b=\frac{23}{2}$ or equivalents | A1 |  |
|  | Solve a pair of simultaneous equations for $a$ or for $b$ | DM1 | Needs at least one of the two previous M marks |
|  | Obtain $a=12$ and $b=40$ | A1 |  |
|  |  | 5 |  |
| 5(ii) | Attempt division by $(x+2)$ or inspection at least as far as $k x^{2}+m x$ | M1 |  |
|  | Obtain $12 x^{2}+16 x+5$ | A1 |  |
|  | Conclude $(x+2)(2 x+1)(6 x+5)$ | A1 |  |
|  |  | 3 |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | :--- |
| 6(i) | Obtain $\frac{\mathrm{d} x}{\mathrm{~d} t}=4 \mathrm{e}^{2 t}+4 \mathrm{e}^{t}$ | $\mathbf{B 1}$ |  |
|  | Use product rule to find $\frac{\mathrm{d} y}{\mathrm{~d} t}$ | M1 |  |
|  | Obtain $\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{5 \mathrm{e}^{2 t}+10 t \mathrm{e}^{2 t}}{4 \mathrm{e}^{2 t}+4 \mathrm{e}^{t}}$ or equivalent | A1 |  |
|  | Equate first derivative of the form $\frac{a \mathrm{e}^{2 t}+b t \mathrm{e}^{2 t}}{c \mathrm{e}^{2 t}+d \mathrm{e}^{t}}$ <br> to zero and solve to find $t$ | M1 |  |
|  | Obtain $t=-\frac{1}{2}$ from completely correct work | A1 |  |
|  | Obtain $(3.16,-0.92)$ | $\mathbf{A 1}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :--- | ---: | ---: |
| 6(ii) | Identify $t=0$ | B1 |  |
|  | Substitute $t=0$ in expression for first derivative <br> and find negative reciprocal | M1 |  |
|  | Obtain $-\frac{8}{5}$ or equivalent | A1 |  |
|  |  | $\mathbf{3}$ |  |


| Question | Answer | Marks | Guidance |
| :---: | :---: | :---: | :---: |
| 7(i) | Differentiate to obtain form $k_{1} x+k_{2}+k_{3} \sin \frac{1}{2} x$ | *M1 |  |
|  | Obtain correct $2 x+3-\frac{5}{2} \sin \frac{1}{2} x$ and deduce or imply gradient at $P$ is 3 | A1 |  |
|  | Equate first derivative to their -3 and rearrange | DM1 |  |
|  | Obtain $x=\frac{5}{4} \sin \frac{1}{2} x-3$ | A1 |  |
|  |  | 4 |  |
| 7(ii) | Consider sign of their $2 x+6-\frac{5}{2} \sin \frac{1}{2} x$ at -4.5 and -4.0 or equivalent | M1 |  |
|  | Complete argument correctly for correct expression with appropriate calculations | A1 |  |
|  |  | 2 |  |
| 7(iii) | Use iteration formula correctly at least once | M1 |  |
|  | Obtain final answer -4.11 | A1 |  |
|  | Show sufficient iterations to justify accuracy to 3 sf or show sign change in interval $(-4.115,-4.105)$ | A1 |  |
|  |  | 3 |  |

