

Question	Answer	Marks	Guidance
1	Introduce logarithms to both sides and use power law	<b>*M1</b>	
	Obtain $(3x-1)\log 5 = 4x\log 2$ or equivalent	<b>A1</b>	Allow <b>A1</b> for poor use of brackets if recovered later
	Solve linear equation for $x$	<b>DM1</b>	dep *M
	Obtain 0.783	<b>A1</b>	Allow 3 sf or better
		<b>4</b>	

Question	Answer	Marks	Guidance
2	Solve 3-term quadratic equation or a pair of linear equations	<b>M1</b>	For <b>M1</b> , must square both sides when attempting a quadratic equation
	Obtain $x = -5$ and $x = 3$	<b>A1</b>	
	Substitute (at least) one value of $x$ (less than 4) into $ x+4  -  x-4 $ , showing correct evaluation of modulus and producing only one answer in each case	<b>M1</b>	
	Obtain $-8$ and $6$ and no others	<b>A1</b>	
		<b>4</b>	

Question	Answer	Marks	Guidance
3	Differentiate to obtain form $k_1 \sec^2 \frac{1}{2}x + k_2 \cos \frac{1}{2}x$	<b>M1</b>	If a factor of 0.5 is missed, can still get 5/6, penalise at first <b>A1</b>
	Obtain $\frac{1}{2}\sec^2 \frac{1}{2}x + \frac{3}{2}\cos \frac{1}{2}x$	<b>A1</b>	
	Equate first derivative to zero and produce $\cos^3 \frac{1}{2}x = k_3$	<b>*M1</b>	
	Use correct process to find one value of $x$	<b>DM1</b>	Dep on *M, allow for obtaining 1.609....., 92.2° or 268°
	Obtain $x = 4.67$	<b>A1</b>	Allow $x = 4.67$ or better for <b>A1</b>
	Obtain $y = 1.12$	<b>A1</b>	Allow $y = 1.12$ from $x = 4.66$ but nothing else
		<b>6</b>	

Question	Answer	Marks	Guidance
4(i)	Substitute $x = -3$ into either $p(x)$ or $q(x)$ and equate to zero ( may be implied)	<b>M1</b>	Allow long division, but the remainder needs to be independent of $x$
	Obtain $a = -11$	<b>A1</b>	
	Obtain $b = -8$	<b>A1</b>	
		<b>3</b>	
4(ii)	Divide $x + 3$ into expression for $q(x) - p(x)$ ( may be a four term cubic equation), or Obtain a 3 term cubic equation by subtraction	<b>*M1</b>	Allow *M1 for their $x^3 + 3x + 36$ , but must have integer values for $a$ and $b$
	Obtain $x^2 - 3x + 12$ or $x^2 - 2x - 5$ and $2x^2 - 5x + 7$	<b>A1</b>	
	Apply discriminant to quadratic factor of $q(x) - p(x)$ or equivalent	<b>DM1</b>	dep on *M
	Obtain $-39$ or equivalent and conclude appropriately	<b>A1</b>	
		<b>4</b>	

Question	Answer	Marks	Guidance
5(i)	Obtain derivative of the form $ke^{-2x}$	<b>*M1</b>	Condone $k = 4$ for <b>M1</b>
	State or imply gradient of curve at $P$ is $-8$	<b>A1</b>	
	Form equation of straight line through $(0, 9)$ with negative gradient	<b>*DM1</b>	dep on *M
	Obtain $y = -8x + 9$ or equivalent	<b>A1</b>	
	Equate equation of curve and equation of straight line	<b>DM1</b>	dep on both *M
	Rearrange to confirm $x = \frac{9}{8} - \frac{1}{2}e^{-2x}$	<b>A1</b>	
		<b>6</b>	

Question	Answer	Marks	Guidance
5(ii)	Use iterative process correctly at least once	<b>M1</b>	
	Obtain final answer 1.07	<b>A1</b>	
	Show sufficient iterations to 5 sf to justify answer or show sign change in interval (1.065, 1.075)	<b>A1</b>	
		<b>6</b>	

Question	Answer	Marks	Guidance
6(a)	Obtain $2 - 2\cos 2x$ as part of integrand	<b>B1</b>	
	Obtain $3\sin 2x$ as part of integrand	<b>B1</b>	Allow second <b>B1</b> for writing
	Integrate to obtain form $k_1x + k_2\sin 2x + k_3\cos 2x$	<b>M1</b>	$\int 6\sin x \cos x \, dx = 6\left(\frac{1}{2}\sin^2 x\right)$ , <b>M1</b> may then be implied by subsequent work
	Obtain $2x - \sin 2x - \frac{3}{2}\cos 2x$ or $2x - \sin 2x + 3\sin^2 x$	<b>A1</b>	
	Apply limits to obtain $\frac{1}{2}\pi + \frac{1}{2}$	<b>A1</b>	
		<b>5</b>	
6(b)	Integrate to obtain $2\ln(3x+2)$	<b>B1</b>	Allow $\frac{6}{3}\ln(3x+2)$ for <b>B1</b>
	Use at least one relevant logarithm property	<b>*M1</b>	
	Obtain $\frac{3a+2}{2} = 7$ or $\frac{(3a+2)^2}{4} = 49$ or equivalent without $\ln$	<b>A1</b>	
	Solve relevant equation to find $a$	<b>DM1</b>	Dep on <b>*M1</b> , allow for $49 = (3a+2)^2$ OE or correct working involving $(3a+2)$
	Obtain $a = 4$ only	<b>A1</b>	
		<b>5</b>	

Question	Answer	Marks	Guidance
7(i)	Obtain $4y + 4x \frac{dy}{dx}$ as derivative of $4xy$	<b>B1</b>	
	Obtain $4y \frac{dy}{dx}$ as derivative of $2y^2$	<b>B1</b>	
	State $2x + 4y + 4x \frac{dy}{dx} + 4y \frac{dy}{dx} = 0$	<b>B1</b>	3rd <b>B1</b> may be implied by later work
	Substitute $x = -1, y = 3$ to find gradient of line	<b>*M1</b>	dep at least one <b>B1</b>
	Form equation of tangent through $(-1, 3)$ with numerical gradient	<b>DM1</b>	dep *M
	Obtain $5x + 4y - 7 = 0$ or equivalent of required form	<b>A1</b>	Allow any 3 term integer form for <b>A1</b>
		<b>6</b>	
7(ii)	Substitute $\frac{dy}{dx} = \frac{1}{2}$ to find relation between $x$ and $y$	<b>*M1</b>	dep at least one <b>B1</b> in part (i), must be linear
	Obtain $4x + 6y = 0$ or equivalent	<b>A1</b>	
	Substitute for $x$ or $y$ in equation of curve	<b>DM1</b>	dep on *M
	Obtain $-\frac{7}{4}y^2 = 7$ or $-\frac{7}{9}x^2 = 7$ or equivalent and conclude appropriately	<b>A1</b>	
		<b>4</b>	