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1	$\left(\frac{508}{8}\right) = 63.5$ $(\sum x^2 = 32360.12)$ $\frac{8}{7} \left(\frac{32360.12}{8} - 63.5^2 \right)$ $= 14.6 \text{ (3 sf) or } 2553/175$	B1 M1 A1	[3]	oe From correct working
2 (i)	$H_0: P(6) = \frac{1}{6} \quad H_1: P(6) < \frac{1}{6}$	B1	[1]	Allow $H_0: p = \frac{1}{6} \quad H_1: p < \frac{1}{6}$
(ii)	$\left(\frac{5}{6}\right)^{15}$ $= 0.065 > 0.05$	M1 A1	[2]	Correct result and comparison needed for A1 SR if 2 tail test followed allow A1 for $0.065 > 0.025$
(iii)	$\left(\frac{5}{6}\right)^{16} = 0.054 \text{ and } \left(\frac{5}{6}\right)^{17} = 0.045$ <p>Smallest n is 17</p> <p>OR</p> $\left(\frac{5}{6}\right)^n < 0.05 \text{ and attempt to solve}$ $n \ln\left(\frac{5}{6}\right) < \ln 0.05$ <p>smallest n is 17</p>	M1 A1 M1 A1	[2]	both No errors seen
3 (i)	$(\lambda) = 3.6 \div 3 = 1.2$ $1 - e^{-1.2} \left(1 + 1.2 + \frac{1.2^2}{2} + \frac{1.2^3}{3!} \right)$ $= 0.0338 \text{ (3 sf)}$	B1 M1 A1	[3]	1.2 seen Allow any λ As final answer
(ii)	$N(60 \times 3.6, 60 \times 3.6)$ $\frac{240.5 - 216}{\sqrt{216}} \quad (= 1.667)$ $1 - \Phi(1.667)$ $= 0.0478 \text{ (3 sf)}$	M1 M1 A1	[4]	Stated or implied Allow with no or wrong cc (no sd/var mixes) Area consistent with their working SR use of Poisson 0.0497 scores 4/4
4 (i)	6080 (litres) 106 (litres)	B1 B1	[2]	
(ii)	$E(21Y - 2X) = 635$ $\text{Var}(21Y - 2X) =$ $21^2 \times 12^2 + 2^2 \times 53^2$ $= 74740$ $\frac{0 - 635}{\sqrt{74740}} \quad (= -2.323)$ $1 - \Phi(-2.323) = \Phi(2.323)$ $= 0.99(0) \text{ (3 sf)}$	B1 B1 M1 M1 A1	[5]	correct expression or result or sd = 273 seen no sd/var mixes Area consistent with their working No errors seen
5 (a)	$63 \pm z \times \frac{9}{\sqrt{100}}$ $z = 1.645$ $61.5 \text{ to } 64.5 \text{ (3 sf)}$	M1 B1 A1	B1 [3]	Expression of correct form, any z Seen Must be an interval

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(b) (i)	$z = \frac{1.96}{2}$ (= 0.98)	M1	[3]	Allow $\frac{\text{any } z}{2}$
	$\Phi(\text{"0.98"})$ (= 0.8365) "0.8365" – (1 – "0.8365") (= 0.673)	M1		Allow 67 from correct working
	$\alpha = 67.3$ (3 sf)	A1		
(ii)	$4 = (2x'z'x'\sigma')/\sqrt{n}$ $n = 200$	M1 A1	[2]	Attempt to solve equ of correct form SR B1 for $n = 100$
6 (i)	m_x, m_y, m_z, m_w or X, Y, Z, W	B2	[2]	B1 if two adjacent means interchanged, i.e. m_y, m_x, m_z, m_w or m_x, m_z, m_y, m_w or m_x, m_y, m_w, m_z B1 for correct order reversed.
(ii) (a)	$\int_0^3 \frac{4}{81} x^4 dx$ $= \left[\frac{4}{81} \frac{x^5}{5} \right]_0^3$ $= \frac{4}{81} \times \frac{3^5}{5}$ or $\frac{4}{81} \times \frac{243}{5}$ or $\frac{972}{405}$ oe $= \frac{12}{5}$ or 2.4	M1 A1 A1	[3]	Attempt int $xf(x)$. Ignore limits Correct integration and limits (condone missing 4/81) Must see correct expression as well as $\frac{12}{5}$ or 2.4 No errors seen
(b)	$\int_{2.4}^3 \frac{4}{81} x^3 dx$ or $1 - \int_0^{2.4} \frac{4}{81} x^3 dx$ $= \left[\frac{4}{81} \frac{x^4}{4} \right]_{2.4}^3$ or $1 - \left[\frac{4}{81} \frac{x^4}{4} \right]_0^{2.4}$ $= 1 - \frac{4}{81} \times \frac{2.4^4}{4}$ oe $= \frac{369}{625}$ or 0.59(0) (3 sf)	M1 A1 A1	[3]	Attempt int $f(x)$ ignore limits Correct integration and limits (condone missing 4/81) As final answer
(c)	1	B1	[1]	

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7 (i)	H_0 : Pop mean time (or μ) = 20.5 H_1 : Pop mean time (or μ) < 20.5 $\frac{20.3-20.5}{1.2\div\sqrt{100}}$ = -1.667 or 0.0478/0.952 if areas compared ‘1.667’ < 1.751 (or ‘-1.667’ > -1.751) No evidence that (pop) mean time has decreased	B1 M1 A1 M1 A1ft	[5]	Not just “mean” Allow without \sqrt sign (accept $\pm 1.667/1.67$) Correct comparison of their z_{calc} with 1.751/1.75 oe valid comparison of areas (0.0478 > 0.04) No contradictions (ft their z)
(ii)	$\frac{cv-20.5}{1.2\div\sqrt{100}} = -1.751$ $cv = 20.29$ or 20.3 $\frac{20.29-20.1}{1.2\div\sqrt{100}} (= 1.583 \text{ or } 1.582)$ $1 - \Phi('1.583')$ = 0.0567 – 0.0569 (3 sf)	M1* A1 DM1 M1 A1	[5]	Allow $\frac{20.3-20.1}{1.2\div\sqrt{100}} (= 1.667)$ M1 $1 - \Phi('1.667')$ M1 = 0.0478 (3 sf) A1
(iii)	Concluding (mean) time not decreased when in fact it has.	B1	[1]	Must be in context oe