

<b>Page 4</b>	<b>Mark Scheme</b>	<b>Syllabus</b>	<b>Paper</b>
	<b>Cambridge International AS/A Level – October/November 2016</b>	<b>9709</b>	<b>61</b>

<b>1</b>	$z = 0.674$ $0.674 = \frac{k - 20}{7}$ $k = 24.7$	<b>M1</b> <b>M1</b> <b>A1</b>	[3]	$\pm 0.674$ seen Standardising no cc, no sq, no sq rt														
<b>2</b>	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>diff</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>prob</td> <td>6/36</td> <td>10/36</td> <td>8/36</td> <td>6/36</td> <td>4/36</td> <td>2/36</td> </tr> </table> Expectation = $(0+10+16+18+16+10)/36$ = $70/36$ = $1.94$	diff	0	1	2	3	4	5	prob	6/36	10/36	8/36	6/36	4/36	2/36	<b>B1</b> <b>M1</b> <b>A1</b> <b>M1</b> <b>A1</b>	[5]	0, 1, 2, 3, 4, 5 seen in table heading or considering all different differences Attempt at finding prob of any difference 1 correct prob Probs summing to 1
diff	0	1	2	3	4	5												
prob	6/36	10/36	8/36	6/36	4/36	2/36												
<b>3 (i)</b>	$0.9 \times 0.95 \times 0.85 \times 0.1 = 0.0727$	<b>B1</b>	[1]															
<b>(ii)</b>	$P(0, 1, 2)$ = $(0.9)^{12} + {}^{12}C_1 (0.1)(0.9)^{11} + {}^{12}C_2 (0.1)^2(0.9)^{10}$ = $0.889$	<b>M1</b> <b>M1</b> <b>A1</b>	[3]	Bin term ${}^{12}C_x (p)^x (1-p)^{12-x}$ $p < 1, x \neq 0$ Bin expression $p = 0.1$ or $0.9, n = 12, 2$ or $3$ terms														
<b>(iii)</b>	$X \sim B(50, 0.85)$ Expectation = $50 \times 0.85 (= 42.5)$ Var = $50 \times 0.85 \times 0.15 (= 6.375)$	<b>M1</b> <b>A1</b>	[2]	$50 \times 0.85$ seen oe can be implied Correct unsimplified mean and var														
<b>4 (i)</b>	$P(< 1) = P\left(z < \frac{1-1.04}{0.017}\right) = P(z < -2.353)$ = $1 - 0.9907$ = $0.0093$	<b>M1</b> <b>M1</b> <b>A1</b>	[3]	Standardising no cc, no $\sqrt$ or sq $1 - \Phi$ (final process)														
<b>(ii)</b>	expected number $1000 \div 1.04 = 961$ or $962$	<b>B1</b>	[1]	Or anything in between														
<b>(iii)</b>	$z = -1.765$ $-1.765 = \frac{1 - \mu}{0.017}$ = $1.03$	<b>B1</b> <b>M1</b> <b>A1</b>	[3]	$\pm 1.76$ to $1.77$ Standardising must have a z-value, allow $\sqrt$ or sq														
<b>(iv)</b>	expected number = $1000 \div 1.03 = 971$ or $970$	<b>B1</b> <sup>ft</sup>	[1]	Or anything in between, ft their (iii)														

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5	(a)	e.g. P*N*P*P*L $= \frac{5!}{3!} \times \frac{{}^6P_4}{2!}$ $= 3600$	M1 M1 M1 A1	[4]	Mult by 5! in num Dividing by 3! or 2! Mult by ${}^6P_4$ oe
	(b) (i)	${}^7C_5 \times {}^5C_4 \times {}^2C_1 \times {}^2C_1$ $= 420$	M1 A1	[2]	Mult 4 combs of which three are correct
	(ii)	both in team ${}^6C_4 \times {}^4C_3 \times 2 \times 2 = 240$ $420 - 240 = 180$ ways  <b>OR</b> Bat in bowl out + bowl in bat out + both out $= {}^6C_4 \times {}^4C_3 \times 2 \times 2 + {}^6C_5 \times {}^4C_3 \times 2 \times 2 + {}^6C_5 \times {}^4C_4 \times 2 \times 2$ $= 60 + 96 + 24 = 180$ ways  <b>OR</b> Bat in bowl out + bat out $= 60 + {}^6C_5 \times {}^5C_4 \times 2 \times 2 = 60 + 120 = 180$ ways	M1 M1 A1 M1 A1 A1 M1 A1 A1	[3]	Evaluating both in team and subtracting from (i) 240 seen can be unsimplified ft their 420, their 240  summing 2 or 3 options not both in team 2 or 3 options correct unsimplified Correct ans from correct working  As above, or bowl in bat out + bowl out
6	(i)	$P(B, B) = 1/4 \times 2/5$ $= 1/10$	M1 A1	[2]	Multiplying two different probs
	(ii)	$P(X = 1) = P(R, R) + P(B, B)$ $= 3/4 \times 4/5 + 1/10$ $= 14/20$ (7/10)	M1 M1 A1	[3]	Finding P(R, R) (=3/5) Summing two options
	(iii)	$P(B \cap B)$ $= \frac{P(B \cap B)}{P(B)} = \frac{1/10}{3/4 \times 1/5 + 1/4 \times 2/5}$  $= 2/5$	M1 M1 A1 A1	[4]	their (i) seen as num or denom of a fraction  $3/4 \times p_1 + 1/4 \times p_2$ seen anywhere  1/4 (unsimplified) seen as num or denom of a fraction, www

<b>7 (i)</b>	<table border="1"> <thead> <tr> <th>Factory <i>A</i></th> <th></th> <th>Factory <i>B</i></th> </tr> </thead> <tbody> <tr> <td></td> <td>3</td> <td>1 5 8</td> </tr> <tr> <td>9</td> <td>4</td> <td>2 4 7 8 9</td> </tr> <tr> <td>9 8 8 7 4 3 0</td> <td>5</td> <td>1 4 6 8</td> </tr> <tr> <td>5 3 1 1 1</td> <td>6</td> <td>4</td> </tr> </tbody> </table>	Factory <i>A</i>		Factory <i>B</i>		3	1 5 8	9	4	2 4 7 8 9	9 8 8 7 4 3 0	5	1 4 6 8	5 3 1 1 1	6	4	<b>M1</b>		Attempt at ordering factory <i>B</i>
	Factory <i>A</i>		Factory <i>B</i>																
		3	1 5 8																
9	4	2 4 7 8 9																	
9 8 8 7 4 3 0	5	1 4 6 8																	
5 3 1 1 1	6	4																	
	Key: 9   4   2 represents 0.049g for factory <i>A</i> and 0.042 g for factory <i>B</i>	<b>B1</b>		Correct stem															
		<b>B1</b>		Correct leaves factory <i>A</i>															
		<b>B1</b>		Correct leaves factory <i>B</i>															
		<b>B1</b>	[5]	Correct key need factory <i>A</i> and factory <i>B</i> and units															
<b>(ii)</b>	<p>median factory <i>B</i> = 0.048 g</p> <p>IQR = UQ – LQ = 0.055 – 0.04</p> <p>= 0.015</p>	<b>B1</b>		using their key i.e. 48, 0.48 etc or correct															
		<b>M1</b>		Subt their LQ from their UQ for factory <i>B</i>															
		<b>A1</b>	[3]																
<b>(iii)</b>	<p>generally heavier in factory <i>A</i></p> <p>Masses more spread out in factory <i>B</i></p>	<b>B1</b>		oe															
		<b>B1</b>	[2]	must refer to context, e.g. mass															