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1	State non-modulus equation $(0.4x - 0.8)^2 = 4$ or equivalent or corresponding pair of linear equations	B1	SR One solution only – B1 Must see some evidence of attempt to solve the quadratic for M1 for at least one value of x For a pair of linear equations, there must be a sign difference If extra solutions are given then A0
	Solve 3-term quadratic equation or pair of linear equations	M1	
	Obtain -3 and 7	A1	
			[3]
2	(i) Use $4^y = 2^{2y}$	B1	
	Attempt solution of quadratic equation in 2^y	M1	
	Obtain finally $2^y = 7$ only	A1	[3]
	(ii) Apply logarithms to solve equation of form $2^y = k$ where $k > 0$	M1	Must be using their positive answer for (i)
	Obtain 2.81	A1	
			[2]
3	(i) Obtain integral of form $k_1 e^{\frac{1}{2}x} + k_2 x$	M1	Allow $k_1 = 4$
	Obtain correct $8e^{\frac{1}{2}x} + 3x$ oe	A1	
	Use limits correctly to confirm $8e - 2$	A1	[3]
	(ii) Draw increasing curve in first quadrant	M1	If incorrect y intercept used then M1 A0 Allow if no intercept stated
	Draw more or less accurate sketch with correct curvature, gradient at $x = 0$ must be > 0	A1	
			[2]
	(iii) State more and refer to top(s) of trapezium(s) above curve	B1	Can be shown using a diagram. Reference to a trapezium must be made
			[1]

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4	(i)	Substitute $x = -1$ and simplify Obtain $-4 + a - a + 4 = 0$ and conclude appropriately	M1 A1	Allow attempt at long division, must get down to a remainder Allow M1 if at least 2 numerical values of a are used May equate to $(x+1)(Ax^2 + Bx + C) + R$ - allow M1 if they get as far as finding R Must have a conclusion - allow 'hence shown', or made a statement of intent at the start of the question	[2]
	(ii)	Substitute $x = 2$ and equate to -42 and attempt to solve Obtain $a = -13$	M1 A1	May equate to $(x-2)(Ax^2 + Bx + C)$, must have a complete method to get as far as $a = \dots$ to obtain M1	[2]
	(iii)	Divide $p(x)$ with their a at least as far as $4x^2 + kx$ Obtain $4x^2 - 17x + 4$ Obtain $(x+1)(4x-1)(x-4)$ or equivalent if x^2 already involved Obtain $(x^2 + 1)(2x-1)(2x+1)(x-2)(x+2)$	M1 A1 A1 A1	If $(x+1)(4x-1)(x-4)$ seen with no evidence of long division then allow the marks	[4]
5	(i)	Use quotient rule (or product rule) to find first derivative Obtain $\frac{\frac{4}{x}(x^2 + 1) - 8x \ln x}{(x^2 + 1)^2}$ or equivalent State $\frac{4}{x}(x^2 + 1) - 8x \ln x = 0$ or equivalent Carry out correct process to produce equation without \ln , without any incorrect working Confirm $m = e^{0.5(1+m^{-2})}$ or $x = e^{0.5(1+x^{-2})}$	M1 A1 A1 M1 A1	Quotient: Must have a difference in the numerator and $(x^2 + 1)^2$ in the denominator Product: Must see an application of the chain rule. Condone missing brackets if correct use is implied by correct work later	[5]

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(ii)	<p>Use iterative formula correctly at least once</p> <p>Obtain final answer 1.895</p> <p>Show sufficient iterations to 6 sf to justify answer or show sign change in interval (1.8945, 1.8955)</p>	<p>M1</p> <p>A1</p> <p>A1</p>	[3]	<p>Should not be attempting to use $x_0 = 0$, but if used and ‘recovered’ then SC M1 A1- usually see $m_1 = 1.6487$</p>
6 (i)	<p>Use $\cos 2\theta = 2\cos^2 \theta - 1$ appropriately twice</p> <p>Simplify to confirm $1 - \frac{1}{2}\sec^2 \theta$</p>	<p>B1</p> <p>B1</p>	[2]	<p>Alternative method</p> $\frac{1 - 2\sin^2 \theta}{2\cos^2 \theta} = \frac{1}{2}\sec^2 \theta - \tan^2 \theta \text{ or}$ $\frac{1}{2\cos^2 \theta} - \tan^2 \theta \quad \text{B1}$ <p>then as for 2nd B1</p>
(ii)	<p>Use $\sec^2 \alpha = 1 + \tan^2 \alpha$</p> <p>Obtain equation $\tan^2 \alpha + 10 \tan \alpha + 25 = 0$ or equivalent</p> <p>Attempt solution of 3-term quadratic equation for $\tan \alpha$ and use correct process for finding value of α from negative value of $\tan \alpha$</p> <p>Obtain 1.77</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	[4]	<p>If quadratic is incorrect, need to see evidence of attempt to solve as required to obtain M1</p> <p>Allow better or in terms of $\pi \left(\frac{1013\pi}{1800} \right)$</p>
(iii)	<p>State or imply integrand $1 - \frac{1}{2}\sec^2 \frac{1}{2}x$</p> <p>Obtain integral of form $k_1 x - k_2 \tan \frac{1}{2}x$</p> <p>Obtain correct $x - \tan \frac{1}{2}x$</p> <p>Apply limits correctly to obtain $\pi - 2$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	[4]	

7	(i)	<p>Use correct addition formula for either $\cos(\theta + \frac{1}{6}\pi)$ or, after diffn, $\sin(\theta + \frac{1}{6}\pi)$</p> <p>Differentiate to obtain $\frac{dy}{d\theta}$ of form $k_1 \sin \theta + k_2 \cos \theta$ or $k \sin(\theta + \frac{1}{6}\pi)$</p> <p>Divide attempt at $\frac{dy}{d\theta}$ by attempt at $\frac{dx}{d\theta}$</p> <p>Obtain $\frac{-\frac{3\sqrt{3}}{2} \sin \theta - \frac{3}{2} \cos \theta}{4 \cos \theta}$ or equivalent</p> <p>Simplify to obtain $-\frac{3}{8}(1 + \sqrt{3} \tan \theta)$</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>Condone ‘missing brackets’</p> <p>[5]</p>
	(ii)	<p>Identify $\theta = 0$</p> <p>Substitute 0 into formula for $\frac{dy}{dx}$ and take negative reciprocal</p> <p>Obtain gradient of normal $\frac{8}{3}$</p> <p>Form equation of normal through point $(0, 1 + \frac{3\sqrt{3}}{2})$</p> <p>Obtain $y = \frac{8}{3}x + 1 + \frac{3\sqrt{3}}{2}$ or equivalent</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>soi</p> <p>be implied by $y = 1 + \frac{3\sqrt{3}}{2}$ or 3.6</p> <p>Must be from correct (i)</p> <p>[5]</p>