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| 1 (i) | Carry out method for solving quadratic equation in $3^{x}$ <br> Obtain at least $3^{x}=7$ <br> Use logarithms to solve an equation of the form $3^{x}=k$ where $k>0$ Obtain 1.77 | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | [4] |
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| (ii) | State $\pm 1.77$, following positive answer from part (i) | B1 ${ }^{\wedge}$ | [1] |
| 2 | State or imply $\ln y=\ln A+p x$ <br> Equate gradient of line to $p$ <br> Obtain $p=0.32$ <br> Substitute to find $A$ <br> Obtain $A=4.81$ <br> OR 1: <br> $3.17=\ln A+5 p$ or $4.77=\ln A+10 p$ <br> Correct attempt to obtain $\ln A$ or $p$ <br> Correct attempt to obtain the other unknown <br> Obtain $\quad A=4.81$ <br> Obtain $\quad p=0.32$ <br> OR 2: $\mathrm{e}^{3.17}=A \mathrm{e}^{5 p} \text { or } \mathrm{e}^{4.77}=A \mathrm{e}^{10 p}$ <br> Correct attempt to obtain p <br> Correct attempt to get A <br> Obtain $\quad A=4.81$ <br> Obtain $p=0.32$ | B1 <br> M1 <br> A1 <br> M1 <br> A1 <br> B1 <br> M1 <br> M1 <br> A1 <br> A1 <br> B1 <br> M1 <br> M1 <br> A1 <br> A1 | [5] |
| 3 | Differentiate to obtain $4 \cos 2 x+10 \sin 2 x$ <br> Equate first derivative to zero and arrange to $\tan 2 x=\ldots$ <br> Obtain $\tan 2 x=-0.4$ <br> Carry out correct method for finding at least one value of $x$, dependent *M <br> Obtain $x=1.38$ <br> Obtain $x=2.95$ and no others between 0 and $\pi$ | $\begin{array}{\|l} \text { B1 } \\ { }^{*} \text { M1 } \\ \text { A1 } \\ \text { DM1 } \\ \text { A1 } \\ \text { A1 } \end{array}$ | [6] |
| $4 \quad$ (i) | Integrate to obtain $2 \mathrm{e}^{2 x}+5 x$ <br> Apply limits correctly and equate to 100 <br> Rearrange and apply logarithms correctly to reach $a=\ldots$ <br> Confirm given result $a=\frac{1}{2} \ln \left(50+\mathrm{e}^{-2 a}-5 a\right)$ | $\begin{array}{\|l\|l} \hline \text { B1 } \\ \text { M1 } \\ \text { M1 } \\ \text { A1 } \end{array}$ | [4] |
| (ii) | Use the iterative formula correctly at least once <br> Obtain final answer 1.854 <br> Show sufficient iterations to justify accuracy to 3 dp or show sign change in interval ( $1.8535,1.8545$ ) | $\begin{array}{\|l\|} \text { M1 } \\ \text { A1 } \\ \text { B1 } \end{array}$ | [3] |


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| 5 (i) | Use $\cos 2 x=2 \cos ^{2} x-1$ and attempt factorisation of numerator Obtain $(2 \cos x+1)(\cos x+4)$ <br> Confirm given result $2 \cos x+1$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | [3] |
| :---: | :---: | :---: | :---: |
| (ii) | Express integrand as $2 \cos 2 x+1$ <br> Integrate to obtain $\sin 2 x+x$ <br> Apply limits correctly to integral of form $k_{1} \sin 2 x+k_{2} x$ <br> Obtain $2 \pi$ | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | [4] |
| 6 | Differentiate $4 x y$ to obtain $4 y+4 x \frac{\mathrm{~d} y}{\mathrm{~d} x}$ <br> Differentiate $y^{2}$ to obtain $2 y \frac{\mathrm{~d} y}{\mathrm{~d} x}$ <br> Equate attempt of derivative of left-hand side to zero <br> Substitute $(1,3)$ to find numerical value of derivative <br> Obtain $-\frac{18}{10}$ or $-\frac{9}{5}$ <br> Obtain $\frac{10}{18}$ or $\frac{5}{9}$ as gradient of normal, following their numerical value of derivative <br> Form equation of normal at $(1,3)$ <br> Obtain $5 x-9 y+22=0$ or equivalent of requested form | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { A1§ } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | [8] |
| $7 \quad$ (i) | Substitute $x=-3$, equate to zero and obtain $27 a+3 b=39$ or equivalent <br> Substitute $x=-2$ and equate to 18 <br> Obtain $8 a+2 b=6$ or equivalent <br> Solve a relevant pair of linear equations for $a$ and $b$ <br> Obtain $a=2$ and $b=-5$ | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | [5] |
| (ii) (a) | Attempt division by $x+3$ at least as far as $2 x^{2}+k x$ <br> Obtain quotient $2 x^{2}-3 x+4$ <br> Calculate discriminant of 3 -term quadratic expression, or equivalent Obtain -23 and conclude appropriately | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | [4] |
| (b) | State $\cos y=-\frac{1}{3}$ <br> Obtain 109.5, dependent *B <br> Obtain -109.5 and no others between - 180 and 180, dependent *B | $\begin{aligned} & \text { *B1 } \\ & \text { B1 } \\ & \text { DB1 } \end{aligned}$ | [3] |

