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1	(i)	$(x+3)^2 - 7$	B1B1	[2]	For $a = 3, b = -7$
	(ii)	1, -7 seen $x > 1, x < -7$ oe	B1 B1	[2]	$x > 1$ or $x < -7$ Allow $x \leq -7, x \geq 1$ oe
2		$8C6(2x)^6 \left(\frac{1}{2x^3}\right)^2$ soi $28 \times 64 \times \frac{1}{4}$ oe (powers and factorials evaluated) 448	B1 B2,1,0 B1	[4]	May be seen within a number of terms May be seen within a number of terms Identified as answer
3	(i)	$2r\alpha + r\alpha + 2r = 4.4r$ $\alpha = 0.8$	M1 A1	[2]	At least 3 of the 4 terms required
	(ii)	$\frac{1}{2}(2r)^2 0.8 - \frac{1}{2}(r^2)0.8 = 30$ $(3/2)r^2 \times 0.8 = 30 \rightarrow r = 5$	M1A1 ^{ft} A1	[3]	Ft through on <i>their</i> α
4	(i)	$C = (4, -2)$ $m_{AB} = -1/2 \rightarrow m_{CD} = 2$ Equation of CD is $y + 2 = 2(x - 4)$ oe $y = 2x - 10$	B1 M1 M1 A1	[4]	Use of $m_1 m_2 = -1$ on their m_{AB} Use of <i>their</i> C and m_{CD} in a line equation
	(ii)	$AD^2 = (14 - 0)^2 + (-7 - (-10))^2$ $AD = 14.3$ or $\sqrt{205}$	M1 A1	[2]	Use <i>their</i> D in a correct method
5		$a(1+r) = 50$ or $\frac{a(1-r^2)}{1-r} = 50$ $ar(1+r) = 30$ or $\frac{a(1-r^3)}{1-r} = 30 + a$ Eliminating a or r $r = 3/5$ $a = 125/4$ oe $S = 625/8$ oe	B1 B1 M1 A1 A1 A1 ^{ft}	[6]	Or otherwise attempt to solve for r Any correct method Ft through on <i>their</i> r and a ($-1 < r < 1$)

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6	(i)	$\cos^4 x = (1 - \sin^2 x)^2 = 1 - 2\sin^2 x + \sin^4 x$ AG	B1	[1]	Could be LHS to RHS or vice versa
	(ii)	$8\sin^4 x + 1 - 2\sin^2 x + \sin^4 x = 2(1 - \sin^2 x)$ $9\sin^4 x = 1$ $x = 35.3^\circ$ (or any correct solution) Any correct second solution from $144.7^\circ, 215.3^\circ, 324.7^\circ$ The remaining 2 solutions	M1 A1 A1 A1 [✓] A1	[5]	Substitute for $\cos^4 x$ and $\cos^2 x$ or OR sub for $\sin^4 x \rightarrow 3\cos^2 x = 2$ $\rightarrow \cos x = (\pm)\sqrt{2/3}$ Allow the first 2 A1 marks for radians (0.616, 2.53, 3.76, 5.67)
7	(i)	$A = (1/2, 0)$	B1	[1]	Accept $x = 0$ at $y = 0$
	(ii)	$\int (1 - 2x)^{1/2} dx = \left[\frac{(1 - 2x)^{3/2}}{3/2} \right] [\div (-2)]$ $\int (2x - 1)^2 dx = \left[\frac{(2x - 1)^3}{3} \right] [\div 2]$ $[0 - (-1/3)] - [0 - (-1/6)]$ 1/6	B1B1 B1B1 M1 A1	[6]	May be seen in a single expression May use $\int_a^1 x dy$, may expand $(2x - 1)^2$ Correct use of <i>their</i> limits
8	(i)	$fg(x) = 5x$ Range of fg is $y \geq 0$ oe	M1A1 B1	[3]	only Accept $y > 0$
	(ii)	$y = 4 / (5x + 2) \Rightarrow x = (4 - 2y) / 5y$ oe $g^{-1}(x) = (4 - 2x) / 5x$ oe 0, 2 with no incorrect inequality $0 < x \leq 2$ oe, c.a.o.	M1 A1 B1, B1 B1	[5]	Must be a function of x
9	(i)	$\mathbf{XP} = -4\mathbf{i} + (p - 5)\mathbf{j} + 2\mathbf{k}$ $[-4\mathbf{i} + (p - 5)\mathbf{j} + 2\mathbf{k}] \cdot (p\mathbf{j} + 2\mathbf{k}) = 0$ $p^2 - 5p + 4 = 0$ $p = 1$ or 4	B1 M1 A1 A1	[4]	Or \mathbf{PX} Attempt scalar prod with $\mathbf{OP/PO}$ and set = 0 (= 0 could be implied)
	(ii)	$\mathbf{XP} = -4\mathbf{i} + 4\mathbf{j} + 2\mathbf{k} \rightarrow \mathbf{XP} = \sqrt{16 + 16 + 4}$ Unit vector = $1/6(-4\mathbf{i} + 4\mathbf{j} + 2\mathbf{k})$ oe	M1 A1	[2]	Expect 6
	(iii)	$\mathbf{AG} = -4\mathbf{i} + 15\mathbf{j} + 2\mathbf{k}$ $\mathbf{XQ} = \lambda\mathbf{AG}$ soi $\lambda = 2/3 \rightarrow \mathbf{XQ} = -\frac{8}{3}\mathbf{i} + 10\mathbf{j} + \frac{4}{3}\mathbf{k}$	B1 M1 A1	[3]	

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<p>10 (i)</p>	$3z - \frac{2}{z} = -1 \Rightarrow 3z^2 + z - 2 = 0$ $x^{1/2} \text{ (or } z) = 2/3 \text{ or } -1$ $x = 4/9 \text{ only}$	<p>M1</p> <p>A1</p> <p>A1</p>	<p>[3]</p>	<p>Express as 3-term quad. Accept $x^{1/2}$ for z</p> <p>(OR</p> $3x - 1 = -\sqrt{x}, 9x^2 - 13x + 4 = 0$ <p>M1, A1, A1 $x = 4/9$)</p>
<p>(ii)</p>	$f(x) = \frac{3x^{3/2}}{3/2} - \frac{2x^{1/2}}{1/2} \quad (+c)$ <p>Sub $x=4, y=10 \quad 10 = 16 - 8 + c \Rightarrow c = 2$</p> <p>When $x = \frac{4}{9}, y = 2\left(\frac{4}{9}\right)^{3/2} - 4\left(\frac{4}{9}\right)^{1/2} + 2$</p> $-2/27$	<p>B1B1</p> <p>M1A1</p> <p>M1</p> <p>A1</p>	<p>[6]</p>	<p>c must be present</p> <p>Substituting x value from part (i)</p>
<p>11 (i)</p>	$\frac{dy}{dx} = -(x-1)^{-2} + 9(x-5)^{-2}$ $m_{\text{tangent}} = -\frac{1}{4} + \frac{9}{4} = 2$ <p>Equation of normal is $y - 5 = -\frac{1}{2}(x - 3)$</p> $x = 13$	<p>M1A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>[5]</p>	<p>May be seen in part (ii)</p> <p>Through (3, 5) and with $m = -1 / m_{\text{tangent}}$</p>
<p>(ii)</p>	$(x-5)^2 = 9(x-1)^2$ $x-5 = (\pm)3(x-1) \text{ or } (8)(x^2 - x - 2) = 0$ $x = -1 \text{ or } 2$ $\frac{d^2y}{dx^2} = 2(x-1)^{-3} - 18(x-5)^{-3}$ <p>When $x = -1, \frac{d^2y}{dx^2} = -\frac{1}{6} < 0$ MAX</p> <p>When $x = 2, \frac{d^2y}{dx^2} = \frac{8}{3} > 0$ MIN</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>[6]</p>	<p>Set $\frac{dy}{dx} = 0$ and simplify</p> <p>Simplify further and attempt solution</p> <p>If change of sign used, x values close to the roots must be used and all must be correct</p>