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1	(i)	N(352, ...) Variance = 2.9	B1 B1	[2]	no recovery in (ii) for each B mark accept $sd = \sqrt{2.9} = 1.70(29)$ stated
	(ii)	$\frac{354 - 352}{\sqrt{2.9}} \quad (= 1.174)$ $1 - \Phi('1.174')$ $= 0.120$ (3 sf)	M1 M1 A1	[3]	with their mean and var Or $\frac{354.05 - 352}{\sqrt{2.9}}$ or correct restart $(= 1.204)$ (accept sd/var mix)1 $-\Phi('1.204')$ $= 0.114$ (3 sf) Incorrect cc can score M1M1A0
Total				[5]	
2		$(\Phi^{-1}(0.99) =) 2.326$ seen N(λ, λ) seen or implied $\frac{55.5 - \lambda}{\sqrt{\lambda}} = + "2.326"$ $\lambda + "2.326" \sqrt{\lambda} - 55.5 = 0$ $\sqrt{\lambda} = \frac{-"2.326" \pm \sqrt{"2.326"}^2 + 4 \times 55.5}}{2}$ $(= 6.377.. \text{ or } - 8.703..)$ $\lambda = 40.7$ (3 sf)	B1 M1 M1 M1 A1	[5]	must be Φ^{-1} , not Φ allow with wrong or no cc & $\Phi(0.99)$ (= 0.8389) must = "z" or attempt at z (0.99 / 0.01 M0) for correct method of solving their quad in $\sqrt{\lambda}$ and squaring to find λ cao, one ans only Without cc, $\lambda = 40.2$: lose final A1
Total				[5]	
3	(i)	0.4 or 2/5 or 26/65	B1	[1]	no recovery in (ii) for the B mark
	(ii)	"0.4" + $z \times \sqrt{\frac{0.4 \times 0.6}{65}} = 0.516$ oe $z = \left(0.116 \times \sqrt{\frac{65}{0.4 \times 0.6}} \right) = 1.909$ $(\Phi('1.909') = 0.97(18))$ $2 ('0.97' - 1)$ $\alpha = 94$	M1 A1 M1 A1	[4]	or "0.4" - $z \times \sqrt{\frac{0.4 \times 0.6}{65}} = 0.284$ or $z \times \sqrt{\frac{0.4 \times 0.6}{65}} = 0.116$ oe for fully correct method to find α from their z allow 94.36 or 94.4 or 94.374
Total				[5]	

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4	(i)	$k \int_{-2}^2 (4 - x^2) dx = 1$	M1		attempt Integral $f(x) = 1$, ignore limits
		$k \left[4x - \frac{x^3}{3} \right]_{-2}^2 = 1$	A1		correct integration & limits
		$\left(k \left(8 - \frac{8}{3} - \left(-8 - \left(-\frac{8}{3} \right) \right) \right) \right)$			
		$k \times \frac{32}{3} = 1$ oe Not e.g. $k \times 10.7 = k$			
		$k = \frac{3}{32}$ AG	A1	[3]	exact answer correctly found
	(ii)	Inverted parabola, vertex on y axis	B1		parabola must finish on x axis at ± 2 , labelled (ignore markings on y axis)
		$E(X) = 0$	B1	[2]	
	(iii)	$\frac{3}{32} \int_{-2}^1 (4 - x^2) dx$	M1		or $1 - \frac{3}{32} \int_1^2 (4 - x^2) dx$ ignore limits
		$\frac{3}{32} \left[4x - \frac{x^3}{3} \right]_{-2}^1$	A1		or $1 - \frac{3}{32} \left[4x - \frac{x^3}{3} \right]_1^2$
		$\frac{3}{32} \left(4 - \frac{1}{3} - \left(-8 - \left(-\frac{8}{3} \right) \right) \right)$			correct integration and correct limits
		$= \frac{27}{32}$ or 0.844 (3 sf)	A1	[3]	$= 1 - \frac{3}{32} \left(8 - \frac{8}{3} - \left(4 - \frac{1}{3} \right) \right)$
Total				[8]	

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5 (a)	$\lambda = 4.5$ $e^{-4.5} \quad (= 0.011109)$ $\left(\frac{99}{100}\right)^{450} \quad (= 0.010860)$ $\left(\frac{0.011109 - 0.010860}{0.010860} \times 100\right)$ $= 2.29\% \text{ (3 sf)}$	B1 M1 M1 A1	[4]	alone allow any λ
(b)	$H_0: P(6) = \frac{1}{6} \text{ or } p = \frac{1}{6}$ $H_1: P(6) < \frac{1}{6} \text{ or } p < \frac{1}{6}$ $\left(\frac{5}{6}\right)^{25} + 25\left(\frac{5}{6}\right)^{24} \times \frac{1}{6} + {}^{25}C_2 \left(\frac{5}{6}\right)^{23} \times \left(\frac{1}{6}\right)^2$ $= 0.189 \text{ (3 sf)}$ comp 0.1 No reason to believe die biased	B1 M1 A1 M1 A1	[5]	Both needed allow one error (extra term / missing term / incorrect term) CR method: attempt at least P(0) and P(0 and 1) (0.010... and 0.06... < 0.1) CR is 0,1 and must see 0.189 for A1 valid comp '0.189' with 0.1 oe valid comparison of 2 with CR correct conclusion, ✓ their 0.189 no contradictions
Total			[9]	
6 (i)	$H_0: \mu = 2.60$ $H_1: \mu > 2.60$ $\pm \frac{2.64 - 2.6}{0.2 \div \sqrt{75}}$ $= \pm 1.732$ $'1.732' > 1.645$ Reject H_0 . There is evidence that μ has increased	B1 M1 A1 B1 ✓	[4]	allow pop mean, not just 'mean' accept $\pm 1.73 \text{ (3 sf)}$ valid comparison with 1.645 (or 0.0416 < 0.05) and correct conclusion ✓ their 1.732 no contradictions (or CV method $x_{crit} = 2.638$ M1A1 comp $2.64 > 2.638$ and concln B1 ✓) SR two tail test, using 1.96 (or using 0.025) can score B0M1A1B1ft max 3/4

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(ii)	$\frac{x - 2.6}{0.2 \div \sqrt{75}} = 1.645 \quad (x = 2.638)$ $\pm \frac{2.638 - 2.68}{0.2 \div \sqrt{75}}$ $= \pm 1.819$ $\Phi(-1.819) = 1 - \Phi(1.819)$ $= 0.0345 \text{ or } 0.0344$	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	[5]	<p>for standardising with their “ 2.638 “ using 2.68 accept 1.82 (3 sf)</p> <p>indep M mark, calculate correct area/prob consistent with their working</p>
Total			[9]	
7 (i)	$\text{est } \mu = 2.087$ $\text{est } \sigma^2 = \frac{100}{99} \left(\frac{435.57}{100} - 2.087^2 \right)$ $= 0.000132(3232) \text{ or } 131/990000$	<p>B1</p> <p>M1</p> <p>A1</p>	[3]	<p>allow 2.09</p> <p>1/99 (435.57 – 208.7²/100)</p> <p>without $\frac{100}{99}$: 0.000131 M0A0</p>
(ii)	$E(Y - X) = 2.12 - 2.087 (= 0.033)$ $\text{Var}(Y - X) = 0.000144 + '0.00013232'$ $= 0.000276(32)$ $\frac{0.01 - '0.033'}{\sqrt{0.00027632}} \quad (= -1.384)$ $\Phi(-1.384) = 1 - \Phi(1.384)$ $= 0.0832$	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p>	[6]	<p>or 2.12 – 2.087 – 0.01 for Y – X – 0.01 < 0 allow 2.09 for 2.087 or $\sqrt{(0.012^2 + '0.00013232')}$ M1 = 0.016623 A1</p> <p>✓ their E(Y – X) & Var(Y – X) var must be a combination of the two vars</p> <p>correct area/prob consistent with their working SR use of biased var (0.000131) in (i) and (ii) scores in (ii) B1M1 A1 for 0.000275 and M1M1 A1 for 0.0827 (6/6 available)</p>
Total			[9]	
	Total for paper		[50]	