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<b>1</b>	$\lambda = (1.2 + 2.3) \div 2$ $= 1.75$ $e^{-1.75} \left( \frac{1.75^2}{2} + \frac{1.75^3}{3!} \right)$ $= 0.421$ (3 sf)	<b>M1</b> <b>A1</b>  <b>M1</b>  <b>A1</b> [4]	Attempt combined mean, allow 1.2 + 2.3 Correct mean  Allow incorrect mean. Allow end errors (1 and/or 4)
		<b>Total: 4</b>	
<b>2 (i)</b>	$\frac{6}{\sqrt{120}}$ oe seen  $\frac{30-29}{\left(\frac{6}{\sqrt{120}}\right)}$ (= 1.826)  $P(z > '1.826') = 1 - \Phi('1.826')$ $= 0.034$ (2 sf)	<b>B1</b>   <b>M1</b>   <b>M1</b> <b>A1</b> [4]	Or 6 <sup>2</sup> /120 oe seen  ± Allow without $\sqrt{120}$ . No sd/var mix  Correct tail consistent with their working 0.0339
<b>(ii)</b>	No <i>n</i> is large ( $\geq 30$ )  Sample mean is (appr) normally distrib or The CLT applies oe	B1    B1 [2]	1 <sup>st</sup> B1 for either comment  2 <sup>nd</sup> B1 for 'No' with 2 <sup>nd</sup> comment (No mark for 'No' alone)
		<b>Total: 6</b>	
<b>3 (i)</b>	$\frac{3420}{60}$ (= 57)  $\frac{60}{59} \left( \frac{195200}{60} - 57^2 \right)$ (= 4.40678) $= 4.41$ (3 sf)	<b>B1</b>   <b>M1</b>   <b>A1</b> [3]	  Oe  As final answer
<b>(ii)</b>	$'57' \pm z \sqrt{\frac{4.40678}{60}}$  $z = 2.326$  [56.4 to 57.6] (3 sf)	<b>M1</b>   <b>B1</b>  <b>A1</b> [3]	  2.326 – 2.329 (accept 2.33 if no better seen) NB: use of biased variance in (ii) can score in full
		<b>Total: 6</b>	

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<p>4 (i)</p>	$k \int_1^2 (3-x) dx = 1$ $k \left[ 3x - \frac{x^2}{2} \right]_1^2 = 1$ $(k(6 - 2 - (3 - 0.5))) = 1$ $k \times 1.5 = 1 \text{ or } k \times \frac{3}{2} = 1 \text{ or } k = \frac{1}{1.5} \text{ oe}$ $k = \frac{2}{3} \text{ AG}$	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>A1</b> [3]</p>	<p>Attempt <math>\int f(x) = 1</math>, ignore limits or <math>\frac{k}{2}(h_1 + h_2) = 1</math></p> <p>Correct integration &amp; limits or <math>\frac{k}{2}(2 + 1) = 1</math></p> <p>No errors seen</p>
<p>(ii)</p>	$\frac{2}{3} \int_1^m (3-x) dx = 0.5 \text{ oe } \int \text{from } m \text{ to } 2$ $\left( \frac{2}{3} \left[ 3x - \frac{x^2}{2} \right]_1^m = 0.5 \right)$ $\frac{2}{3} \left[ 3m - \frac{m^2}{2} - 2.5 \right] = 0.5$ $m^2 - 6m + 6.5 = 0 \text{ oe}$ $\left( m = \frac{6 \pm \sqrt{36 - 4 \times 6.5}}{2} = 1.42 \text{ or } 4.58 \right)$ $m = 1.42 \text{ (3 sf)}$	<p><b>M1*</b></p> <p><b>dep M1*</b></p> <p><b>A1</b></p> <p><b>A1</b> [4]</p>	<p>Attempt <math>\text{Int } f(x) = 0.5</math>, ignore limits oe</p> <p>Or use of area of trapezium</p> <p>Sub of correct limits into their integral. Or trapezium using 1 and m/m and 2</p> <p>Any correct 3-term QE = 0 or <math>(m-3)^2 = 2.5</math></p> <p>or <math>\frac{6 - \sqrt{10}}{2}</math> oe; single correct ans</p>
		<p><b>Total: 7</b></p>	

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<b>5 (i)</b>	Po(1.6) stated or implied  $P(X > 3) = 1 - e^{-1.6} \left( 1 + 1.6 + \frac{1.6^2}{2} + \frac{1.6^3}{3!} \right)$ $= 0.0788 \text{ (3 sf)}$	<b>M1</b>  <b>M1</b>  <b>A1</b> [3]	Allow M1 for $1 - P(X \leq 3)$ , incorrect $\lambda$ and allow one end error  SR Use of Bin scores B1 only for 0.0788		
<b>(ii)</b>	$\lambda = \frac{n}{2500}$ $e^{-\frac{n}{2500}} < 0.05 \quad \text{Allow =}$ $\text{Allow incorrect } \lambda$ $-\frac{n}{2500} < \ln 0.05 \quad \text{Attempt ln bs}$ $n > 7489.3 \text{ (1 dp)}$ $\text{Smallest } n = 7490$	<b>B1</b>  <b>M1</b>  <b>M1</b>  <b>A1</b> [4]	<table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; vertical-align: top;"> or  <math>e^{-\mu} &lt; 0.05</math>    <b>M1</b> </td> <td style="width: 50%; vertical-align: top;"> or  <math>\frac{2499}{2500}</math>    <b>B1</b>  <math>\left(\frac{2499}{2500}\right)^n &lt; 0.05</math>    <b>M1</b>  <math>n \ln \frac{2499}{2500} &lt; \ln 0.05</math>    <b>M1</b>  Smallest <math>n = 7488</math>    <b>A1</b> </td> </tr> </table> $n = \mu \times 2500$ <b>B1</b> Smallest $n = 7490$ <b>A1</b>	or $e^{-\mu} < 0.05$ <b>M1</b>	or $\frac{2499}{2500}$ <b>B1</b> $\left(\frac{2499}{2500}\right)^n < 0.05$ <b>M1</b> $n \ln \frac{2499}{2500} < \ln 0.05$ <b>M1</b> Smallest $n = 7488$ <b>A1</b>
or $e^{-\mu} < 0.05$ <b>M1</b>	or $\frac{2499}{2500}$ <b>B1</b> $\left(\frac{2499}{2500}\right)^n < 0.05$ <b>M1</b> $n \ln \frac{2499}{2500} < \ln 0.05$ <b>M1</b> Smallest $n = 7488$ <b>A1</b>				
		<b>Total: 7</b>			
<b>6 (i)</b>	$E(T) = 9 \times 78 + 7 \times 66 \quad (= 1164)$  $\text{Var}(T) = 9 \times 7^2 + 7 \times 5^2 \quad (= 616)$  $\frac{1200 - '1164'}{\sqrt{'616'}} \quad (= 1.450)$  $P(z < 1.450) = \Phi(1.450)$ $= 0.927 \text{ (3 sf)}$	<b>B1</b>  <b>B1</b>  <b>M1</b>  <b>M1</b>  <b>A1</b> [5]	Or $9 \times 78 + 7 \times 66 - 1200$  $\pm$ Allow without $\sqrt{\quad}$  Correct tail consistent with their mean		
<b>(ii)</b>	$E(D) = 66 - 78 \quad (= -12)$  $\text{Var}(D) = 7^2 + 5^2 \quad (= 74)$  $\frac{0 - ('-12')}{\sqrt{74}} \quad (= 1.395)$  $P(D > 0) = 1 - \Phi('1.395')$ $0.0815 \text{ (3 sf)}$	<b>B1</b>  <b>M1</b>  <b>M1</b>  <b>A1</b> [4]	Both needed  $\pm$ Allow without $\sqrt{\quad}$  Correct tail consistent with their mean Similar scheme for $P(M - W) < 0$		
		<b>Total: 9</b>			

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7	(i)	Prob could be different later in day or on a different day oe	<b>B1</b> [1]	or any explanation why not random or “Not random” or “Not representative”
	(ii)	Looking for decrease (or improvement) $H_0: P(\text{not arrive}) = 0.2$ $H_1: P(\text{not arrive}) < 0.2$	<b>B1</b> <b>B1</b> [2]	oe Allow “ $p = 0.2$ ”
	(iii)	Concluding that prob has <u>decreased</u> (or publicity has worked) when it hasn't oe	<b>B1</b> [1]	In context
	(iv)	$P(X = 0)$ and $P(X = 1)$ attempted  $P(X \leq 2) = 0.8^{30} + 30 \times 0.8^{29} \times 0.2 +$ ${}^{30}C_2 \times 0.8^{28} \times 0.2^2$ $(= 0.0442)$  $P(X \leq 3) = 0.8^{30} + 30 \times 0.8^{29} \times 0.2 +$ ${}^{30}C_2 \times 0.8^{28} \times 0.2^2 + {}^{30}C_3 \times 0.8^{27} \times 0.2^3$ $= 0.123$  cr is $X \leq 2$ $P(\text{Type I}) = 0.0442$ (3 sf)	<b>M1</b>  <b>M1</b>  <b>B1</b>  <b>A1</b> <b>A1</b> [5]	B(30, 0.2) Not nec'y added May be implied by calc $P(X \leq 2)$ or $P(X \leq 3)$  Attempt $P(X \leq 2)$  Or ‘0.0442’ + ${}^{30}C_3 \times 0.8^{27} \times 0.2^3 = 0.123$
	(v)	3 is outside cr  No evidence that $p$ has decreased (or that publicity has worked)	<b>M1</b> <b>A1</b> ✓ [2]	Comparison of 3 with their cr or $P(X \leq 3) = 0.123$ which is $> 0.05$ Correct conclusion. No contradictions
			<b>Total: 11</b>	
			<b>Total for paper: 50</b>	