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1	coded mean = 0.3 oe $sd = \sqrt{\frac{96.1}{250} - (0.3)^2}$ $= 0.543$ Alt: $\Sigma(t-2.5)^2$ expanded $\Sigma t^2 = 2033.6$ $sd = \sqrt{\frac{2033.6}{250} - 2.8^2}$ $= 0.543$	B1	$\Sigma(t - 2.5) = 75$ B0 until $\div 250$
		M1	Subst in variance formula both terms coded
		A1 3	Correct answer
		Or B1	
		M1	Substituting their Σt^2 from expanded 3-term expression, 250 and 2.8 in variance formula
		A1 3	
2	(i) $P(X) = \frac{20}{28} \left(\frac{5}{7} \right) (0.714), 71.4\%$	B1 1	oe
	(ii) $P(F) = \frac{20}{28} \times \frac{1}{4} \times \frac{8}{28} \times \frac{6}{10} = \frac{7}{20}$	M1	Summing two 2-factor probs created by One of $\frac{1}{4}$ or $\frac{3}{4}$ multiplied by $\frac{20}{28}$ or $\frac{8}{28}$
		A1 2	Added to $\frac{4}{10}$ or $\frac{6}{10} \times$ altn population prob Correct answer
	(iii) $P(X F) = \frac{5/28}{7/20} = \frac{25}{49} (0.510)$	M1	Their unsimplified country X probability ($\frac{5}{28}$) as num or denom of a fraction Or (their fair hair population) \div (total fair hair pop)
		A1 2	Correct answer
3	(i) $P(S) = \frac{3}{16}$ $P(T) = \frac{4}{16}$ $P(S \cap T) = \frac{2}{16}$ $P(S) \times P(T) = \frac{3}{64} \neq \frac{2}{16}$ Not independent	M1	Sensible attempt at $P(S)$
		M1	Sensible attempt at $P(T)$
		B1	Correct $P(S \cap T)$
		M1	comp $P(S) \times P(T)$ with $P(S \cap T)$ (their values), evaluated
		A1 5	Correct conclusion following all correct working
	(ii) not exclusive since $P(S \cap T) \neq 0$ Or counter example e.g. 1 and 3 Or $P(S \cup T) \neq P(S) + P(T)$ with values	B1 ^h 1	FT their $P(S \cap T)$, not obtained from $P(S) \times P(T)$, with value and statement.
4	(i) $z = 1.127$ $1.127 = \frac{136 - 125}{\sigma}$ $\sigma = 9.76$	B1	± 1.127 seen accept rounding to ± 1.13
		M1	Standardising no cc no sq rt, with attempt at z
		A1 3	(not $\pm 0.8078, \pm 0.5517, \pm 0.13, \pm 0.87$) Correct ans

(ii)	$P(131 < x < 141) = P\left(\frac{131-125}{9.76} < z < \frac{141-125}{9.76}\right)$ $= \Phi(1.639) - \Phi(0.6147)$ $= 0.9493 - 0.7307$ $= 0.2186$ <p>Number = $0.2186 \times 170 = 37$ or 38 or awrt 37.2</p>	M1 M1 M1 A1	Standardising once with their sd, no $\sqrt{}$, ² , allow cc Correct area $\Phi 2 - \Phi 1$ Mult by 170, $P < 1$ Correct answer, nfw																												
5 (a)	e.g. ** (AAOOOI) ***** $\frac{8!}{2!2!} \times \frac{6!}{2!3!} = 604800$	B1 M1 A1	8! ($8 \times 7!$) or 6! seen anywhere, either alone or in numerator) Dividing by at least 3 of 2!2!2!3! (may be fractions added) Correct answer																												
(b)	<table border="0"> <tr> <td>C(7)</td> <td>E(6)</td> <td>A(4)</td> <td></td> </tr> <tr> <td>1</td> <td>1</td> <td>2</td> <td>$= 7 \times 6 \times {}^4C_2 = 252$</td> </tr> <tr> <td>1</td> <td>2</td> <td>1</td> <td>$= 7 \times {}^6C_2 \times 4 = 420$</td> </tr> <tr> <td>1</td> <td>3</td> <td>0</td> <td>$= 7 \times {}^6C_3 \times 1 = 140$</td> </tr> <tr> <td>2</td> <td>1</td> <td>1</td> <td>$= {}^7C_2 \times 6 \times 4 = 504$</td> </tr> <tr> <td>2</td> <td>2</td> <td>0</td> <td>$= {}^7C_2 \times {}^6C_2 \times 1 = 315$</td> </tr> <tr> <td>3</td> <td>1</td> <td>0</td> <td>$= {}^7C_3 \times 6 \times 1 = 210$</td> </tr> </table> <p>Total = 1841</p>	C(7)	E(6)	A(4)		1	1	2	$= 7 \times 6 \times {}^4C_2 = 252$	1	2	1	$= 7 \times {}^6C_2 \times 4 = 420$	1	3	0	$= 7 \times {}^6C_3 \times 1 = 140$	2	1	1	$= {}^7C_2 \times 6 \times 4 = 504$	2	2	0	$= {}^7C_2 \times {}^6C_2 \times 1 = 315$	3	1	0	$= {}^7C_3 \times 6 \times 1 = 210$	M1 A1 M1* DM1 A1	Mult 3 appropriate combinations together assume $6 = {}^6C_1$, $1 = {}^4C_0$ etc., $\sum r=4$, C&E both present At least 3 correct unsimplified products Listing at least 4 different correct options Summing at least 4 outcomes, involving 3 combs or perms, $\sum r=4$ Correct answer SC if CE removed, M1 available for listing at least 4 different correct options for remaining 2. DM1 for ${}^7C_1 \times {}^6C_1 \times (\text{sum of at least 4 outcomes})$
C(7)	E(6)	A(4)																													
1	1	2	$= 7 \times 6 \times {}^4C_2 = 252$																												
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6 (i)	fd 0.9, 3, 4.2, 5.2, 1.4 	M1 A1 B1 B1	Attempt at scaled freq [f/(attempt at cw)] Correct heights seen on diagram Scale no less than 1cm to 1 unit Correct bar widths visually no gaps Labels (ht/metres and fd or freq per 20m etc.) and end points at 20.5 etc. condone 2 end point errors, scale no less than 1cm to 5m for 20,30... unless clearly accurate, linear scale between 20.5 and 80																												

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	(ii) $(30.5 \times 18 + 43 \times 15 + 48 \times 21 + 55.5 \times 52 + 70.5 \times 28)/134$ $= \frac{7062}{134} = 52.701$ $\text{Var} = (30.5^2 \times 18 + 43^2 \times 15 + 48^2 \times 21 + 55.5^2 \times 52 + 70.5^2 \times 28)/134 - 52.701^2$ $= 392203.5/134 - 52.701^2 = 149.496$ $\text{sd} = 12.2$	M1	Attempt at unsimplified, mid points (at least 4 within 0.5)
		M1 A1	Attempt at Σfx their mid points $\div 134$ Correct mean rounding to 53
		M1	Attempts at Σfx^2 their mid points \div their $\Sigma f - \text{mean}^2$
		A1 5	Correct answer, nfw
7	(i) $P(0, 1, 2) = (0.92)^{19} + {}^{19}C_1(0.08)(0.92)^{18} + {}^{19}C_2(0.08)^2(0.92)^{17}$ $= 0.809$	M1 M1	Binomial term ${}^{19}C_x p^x (1-p)^{19-x}$ seen $0 < p < 1$ Correct unsimplified expression
		A1 3	Correct answer (no working SC B2)
	(ii) $P(\text{at least } 1) = 1 - P(0)$ $= 1 - P(0.92)^n > 0.90$ $0.1 > (0.92)^n$ $n > 27.6$ Ans 28	M1 M1	Eqn with their 0.92^n , 0.9 or 0.1, 1 not nec Solving attempt by logs or trial and error, power eqn with one unknown power
	(iii) $np = 1800 \times 0.08 = 144$ $npq = 132.48$ $P(\text{at least } 152) = P\left(z > \left(\frac{151.5 - 144}{\sqrt{132.48}}\right)\right)$ $= P(z > 0.6516)$ $= 1 - 0.7429$ $= 0.257$	B1 M1 M1 M1 A1	correct unsimplified np and npq seen accept 132.5, 132, 11.5, awrt 11.51 standardising, with $\sqrt{\quad}$ cont correction 151.5 or 152.5 seen correct area $1 - \Phi$ (probability) correct answer
	(iv) Use because 1800×0.08 (and 1800×0.92 are both) > 5	B1 1	$1800 \times 0.08 > 5$ is sufficient $np > 5$ is sufficient if clearly evaluated in (iii) If $npq > 5$ stated then award B0