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- 1 EITHER: State or imply non-modular inequality $(2x-5)^2 > (3(2x+1))^2$, or corresponding quadratic equation, or pair of linear equations $(2x-5) = \pm 3(2x+1)$ **B1**
 Make reasonable solution attempt at a 3-term quadratic, or solve two linear equations for x **M1**
 Obtain critical values -2 and $\frac{1}{4}$ **A1**
 State final answer $-2 < x < \frac{1}{4}$ **A1**
 OR: Obtain critical value $x = -2$ from a graphical method, or by inspection, or by solving a linear equation or inequality **B1**
 Obtain critical value $x = \frac{1}{4}$ similarly **B2**
 State final answer $-2 < x < \frac{1}{4}$ **B1** [4]
 [Do not condone \leq for $<$]
- 2 State or imply $1+u=u^2$ **B1**
 Solve for u **M1**
 Obtain root $\frac{1}{2}(1+\sqrt{5})$, or decimal in $[1.61, 1.62]$ **A1**
 Use correct method for finding x from a positive root **M1**
 Obtain $x = 0.438$ and no other answer **A1** [5]
- 3 Use $\tan(A \pm B)$ and obtain an equation in $\tan \theta$ and $\tan \phi$ **M1***
 Substitute throughout for $\tan \theta$ or for $\tan \phi$ **dep M1***
 Obtain $3 \tan^2 \theta - \tan \theta - 4 = 0$ or $3 \tan^2 \phi - 5 \tan \phi - 2 = 0$, or 3-term equivalent **A1**
 Solve a 3-term quadratic and find an angle **M1**
 Obtain answer $\theta = 135^\circ$, $\phi = 63.4^\circ$ **A1**
 Obtain answer $\theta = 53.1^\circ$, $\phi = 161.6^\circ$ **A1** [6]
 [Treat answers in radians as a misread. Ignore answers outside the given interval.]
 [SR: Two correct values of θ (or ϕ) score A1; then A1 for both correct θ , ϕ pairs.]
- 4 (i) Evaluate, or consider the sign of, $x^3 - x^2 - 6$ for two integer values of x , or equivalent **M1**
 Obtain the pair $x = 2$ and $x = 3$, with no errors seen **A1** [2]
- (ii) State a suitable equation, e.g. $x = \sqrt{(x + (6/x))}$ **B1**
 Rearrange this as $x^3 - x^2 - 6 = 0$, or work *vice versa* **B1** [2]
- (iii) Use the iterative formula correctly at least once **M1**
 Obtain final answer 2.219 **A1**
 Show sufficient iterates to 5 d.p. to justify 2.219 to 3 d.p., or show there is a sign change in the interval (2.2185, 2.2195) **A1** [3]

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- 5 (i) State or imply that the derivative of e^{-2x} is $-2e^{-2x}$ **B1**
 Use product or quotient rule **M1**
 Obtain correct derivative in any form **A1**
 Use Pythagoras **M1**
 Justify the given form **A1** [5]
- (ii) Fully justify the given statement **B1** [1]
- (iii) State answer $x = \frac{1}{4}\pi$ **B1** [1]
- 6 (i) Substitute $x = -1$, equate to zero and simplify at least as far as $-8 + a - b - 1 = 0$ **B1**
 Substitute $x = -\frac{1}{2}$ and equate the result to 1 **M1**
 Obtain a correct equation in any form, e.g. $-1 + \frac{1}{4}a - \frac{1}{2}b - 1 = 1$ **A1**
 Solve for a or for b **M1**
 Obtain $a = 6$ and $b = -3$ **A1** [5]
- (ii) Commence division by $(x + 1)$ reaching a partial quotient $8x^2 + kx$ **M1**
 Obtain quadratic factor $8x^2 - 2x - 1$ **A1**
 Obtain factorisation $(x + 1)(4x + 1)(2x - 1)$ **A1** [3]
 [The M1 is earned if inspection reaches an unknown factor $8x^2 + Bx + C$ and an equation in B and/or C , or an unknown factor $Ax^2 + Bx - 1$ and an equation in A and/or B .]
 [If linear factors are found by the factor theorem, give B1B1 for $(2x - 1)$ and $(4x + 1)$, and B1 for the complete factorisation.]
- 7 (i) Use correct method to form a vector equation for AB **M1**
 Obtain a correct equation, e.g. $\mathbf{r} = \mathbf{i} + 2\mathbf{j} + \lambda(2\mathbf{i} - 2\mathbf{j} + \mathbf{k})$ or $\mathbf{r} = 3\mathbf{i} + \mathbf{k} + \mu(2\mathbf{i} - 2\mathbf{j} + \mathbf{k})$ **A1** [2]
- (ii) Using a direction vector for AB and a relevant point, obtain an equation for m in any form **M1**
 Obtain answer $2x - 2y + z = 4$, or equivalent **A1** [2]
- (iii) Express general point of AB in component form, e.g. $(1 + 2\lambda, 2 - 2\lambda, \lambda)$ or $(3 + 2\mu, -2\mu, 1 + \mu)$ **B1**
 Substitute in equation of m and solve for λ or for μ **M1**
 Obtain final answer $\frac{7}{3}\mathbf{i} + \frac{2}{3}\mathbf{j} + \frac{2}{3}\mathbf{k}$ for the position vector of N , from $\lambda = \frac{2}{3}$ or $\mu = -\frac{1}{3}$ **A1**
 Carry out a correct method for finding CN **M1**
 Obtain the given answer $\sqrt{13}$ **A1** [5]
 [The f.t. is on the direction vector for AB .]

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8	Separate variables and integrate one side	B1	
	Obtain term $\ln(x + 2)$	B1	
	Use $\cos 2A$ formula to express $\sin^2 2\theta$ in the form $a + b \cos 4\theta$	M1	
	Obtain correct form $(1 - \cos 4\theta)/2$, or equivalent	A1	
	Integrate and obtain term $\frac{1}{2}\theta - \frac{1}{8}\sin 4\theta$, or equivalent	A1	
	Evaluate a constant, or use $\theta = 0, x = 0$ as limits in a solution containing terms $c \ln(x + 2), d \sin(4\theta), e\theta$	M1	
	Obtain correct solution in any form, e.g. $\ln(x + 2) = \frac{1}{2}\theta - \frac{1}{8}\sin 4\theta + \ln 2$	A1	
	Use correct method for solving an equation of the form $\ln(x + 2) = f$	M1	
Obtain answer $x = 0.962$	A1	[9]	
9	(i) Show u in a relatively correct position	B1	
	Show u^* in a relatively correct position	B1	
	Show $u^* - u$ in a relatively correct position	B1	
	State or imply that $OABC$ is a parallelogram	B1	[4]
	(ii) <i>EITHER</i> : Substitute for u and multiply numerator and denominator by $3 + i$, or equivalent	M1	
	Simplify the numerator to $8 + 6i$ or the denominator to 10	A1	
	Obtain final answer $\frac{4}{5} + \frac{3}{5}i$, or equivalent	A1	
	<i>OR</i> : Substitute for u , obtain two equations in x and y and solve for x or for y	M1	
	Obtain $x = \frac{4}{5}$ or $y = \frac{3}{5}$, or equivalent	A1	
	Obtain final answer $\frac{4}{5} + \frac{3}{5}i$, or equivalent	A1	[3]
(iii)	State or imply $\arg(u^*/u) = \tan^{-1}(\frac{3}{4})$	B1	
	Substitute exact arguments in $\arg(u^*/u) = \arg u^* - \arg u$	M1	
	Fully justify the given statement using exact values	A1	[3]
10	(i) Use the quotient rule	M1	
	Obtain correct derivative in any form	A1	
	Equate derivative to zero and solve for x	M1	
	Obtain answer $x = \sqrt[3]{2}$, or exact equivalent	A1	[4]
	(ii) State or imply indefinite integral is of the form $k \ln(1 + x^3)$	M1	
	State indefinite integral $\frac{1}{3} \ln(1 + x^3)$	A1	
	Substitute limits correctly in an integral of the form $k \ln(1 + x^3)$	M1	
	State or imply that the area of R is equal to $\frac{1}{3} \ln(1 + p^3) - \frac{1}{3} \ln 2$, or equivalent	A1	
	Use a correct method for finding p from an equation of the form $\ln(1 + p^3) = a$ or $\ln((1 + p^3)/2) = b$	M1	
	Obtain answer $p = 3.40$	A1	[2]