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- 1 (i) Either Square both sides to obtain three-term quadratic equation **M1**
Solve three-term quadratic equation to obtain two values **M1**
Obtain -1 and $\frac{7}{3}$ **A1**
- Or Obtain $\frac{7}{3}$ from graphical method, inspection or linear equation **B1**
Obtain -1 similarly **B2** [3]
- (ii) Use logarithmic method to solve an equation of the form $5^y = k$ where $k > 0$ **M1**
Obtain 0.526 and no others **A1** [2]
- 2 (i) Use the iterative formula correctly at least once **M1**
Obtain final answer 2.289 **A1**
Show sufficient iterations to justify accuracy to 3 d.p. or show sign change in interval (2.2885, 2.2895) **A1** [3]
- (ii) State $x = 2 + \frac{4}{x^2 + 2x + 4}$ or equivalent **B1**
Obtain $\sqrt[3]{12}$ **B1** [2]
- 3 State or imply that $\ln y = \ln K + m \ln x$ **B1**
Form a numerical expression for gradient of line **M1**
Obtain -1.39 or -1.4 **A1**
Use their gradient value and one point correctly to obtain intercept **M1**
Obtain value for $\ln K$ between 4.26 and 4.28 **A1**
Obtain $K = 71$ or $K = 72$ or value rounding to either with no error noted **A1** [6]
- 4 (i) Substitute $x = -2$ and equate to zero **M1**
Solve equation to confirm $a = -4$ **A1** [2]
- (ii) (a) Find quadratic factor by division, inspection, identity, ... **M1**
Obtain $6x^2 - x - 2$ **A1**
Conclude $(x + 2)(3x - 2)(2x + 1)$ **A1** [3]
- (b) State or imply at least $\sec \theta = -2$ and attempt solution **M1**
Obtain 120° and no others in range **A1** [2]
- 5 (i) Use product rule to obtain form $k_1 e^{-3x} + k_2 x e^{-3x}$ **M1**
Obtain correct $4e^{-3x} - 12xe^{-3x}$ **A1**
Obtain $x = \frac{1}{3}$ or 0.333 or better and no other **A1** [3]

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- (ii) Use quotient rule or equivalent M1*
 Obtain correct numerator $8x(x+1) - 4x^2$ or equivalent A1
 Equate numerator to zero and solve to find at least one value M1 dep
 Obtain $x = -2$ A1
 Obtain $x = 0$ A1 [5]
- 6 (i) Either Obtain $\frac{dx}{dt} = -3 \sin t$ B1
 Obtain $\frac{dy}{dt} = -2 \sin(t - \frac{1}{6}\pi)$ B1
 Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ M1
 Expand $-2 \sin(t - \frac{1}{6}\pi)$ to obtain $k_1 \sin t + k_2 \cos t$ M1
 Confirm given result $\frac{1}{3}(\sqrt{3} - \cot t)$ correctly A1
- Or Obtain $\frac{dx}{dt} = -3 \sin t$ B1
 Expand y to obtain $k_3 \cos t + k_4 \sin t$ M1
 Obtain $\frac{dy}{dt} = -\sqrt{3} \sin t + \cos t$ or equivalent A1
 Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ M1
 Confirm given result $\frac{1}{3}(\sqrt{3} - \cot t)$ correctly A1 [5]
- (ii) Identify value of t as $\frac{1}{2}\pi$ only B1
 Obtain gradient at relevant point as $\frac{1}{3}\sqrt{3}$ or 0.577 or better B1
 Form equation of tangent through (0, 1), using their gradient M1
 Obtain $y = \frac{1}{3}\sqrt{3}x + 1$ or equivalent A1 [4]
- 7 (i) Express $\cos^2 x$ in form $k_1 + k_2 \cos 2x$ M1
 Obtain correct $\frac{1}{2} + \frac{1}{2} \cos 2x$ A1
 Rewrite second term as $\sec^2 x$ B1
 Integrate to obtain at least terms $k_3 \sin 2x$ and $k_4 \tan x$ M1
 Obtain $\frac{1}{2}x + \frac{1}{4} \sin 2x + \tan x$ A1
 Confirm given result $\frac{1}{6}\pi + \frac{9}{8}\sqrt{3}$ A1 [6]
- (ii) State volume is $\pi \int (\cos x + \frac{1}{\cos x})^2$ (π maybe implied by later appearance) B1
 Expand to obtain $\pi \int (\cos^2 x + \frac{1}{\cos^2 x} + 2) dx$ or $\int (\cos^2 x + \frac{1}{\cos^2 x} + 2) dx$ B1
 Integrate integrand involving three terms (in part using part (i) or otherwise i.e. $k_3 \sin 2x + k_4 \tan x + k_5 x$) M1
 Obtain $\frac{5}{6}\pi^2 + \frac{9}{8}\sqrt{3}\pi$ or exact equivalent A1 [4]