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- 1 Use law of the logarithm of a power M1
 Obtain a correct linear equation in any form, e.g. $x = (x - 2) \ln 3$ A1
 Obtain answer $x = 22.281$ A1 [3]
- 2 (i) State or imply ordinates 2, 1.1547..., 1, 1.1547... B1
 Use correct formula, or equivalent, with $h = \frac{1}{6}\pi$ and four ordinates M1
 Obtain answer 1.95 A1 [3]
- (ii) Make recognisable sketch of $y = \operatorname{cosec} x$ for the given interval B1
 Justify a statement that the estimate will be an overestimate B1 [2]
- 3 Substitute $x = -\frac{1}{3}$, equate result to zero or divide by $3x + 1$ and equate the remainder to zero
 and obtain a correct equation, e.g. $-\frac{1}{27}a + \frac{1}{9}b - \frac{1}{3} + 3 = 0$ B1
 Substitute $x = 2$ and equate result to 21 or divide by $x - 2$ and equate constant remainder to 21 M1
 Obtain a correct equation, e.g. $8a + 4b + 5 = 21$ A1
 Solve for a or for b M1
 Obtain $a = 12$ and $b = -20$ A1 [5]
- 4 (i) Use chain rule correctly at least once M1
 Obtain either $\frac{dx}{dt} = \frac{3\sin t}{\cos^4 t}$ or $\frac{dy}{dt} = 3\tan^2 t \sec^2 t$, or equivalent A1
 Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$ M1
 Obtain the given answer A1 [4]
- (ii) State a correct equation for the tangent in any form B1
 Use Pythagoras M1
 Obtain the given answer A1 [3]
- 5 (i) Substitute $z = 1 + i$ and obtain $w = \frac{1 + 2i}{1 + i}$ B1
EITHER: Multiply numerator and denominator by the conjugate of the denominator, M1
 or equivalent A1
 Simplify numerator to $3 + i$ or denominator to 2 A1
 Obtain final answer $\frac{3}{2} + \frac{1}{2}i$, or equivalent A1
- OR:* Obtain two equations in x and y , and solve for x or for y M1
 Obtain $x = \frac{3}{2}$ or $y = \frac{1}{2}$, or equivalent A1
 Obtain final answer $\frac{3}{2} + \frac{1}{2}i$, or equivalent A1 [4]

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- (ii) *EITHER*: Substitute $w = z$ and obtain a 3-term quadratic equation in z ,
 e.g. $iz^2 + z - i = 0$ B1
 Solve a 3-term quadratic for z or substitute $z = x + iy$ and use a correct
 method to solve for x and y M1
OR: Substitute $w = x + iy$ and obtain two correct equations in x and y by equating
 real and imaginary parts B1
 Solve for x and y M1
- Obtain a correct solution in any form, e.g. $z = \frac{-1 \pm \sqrt{3} i}{2i}$ A1
- Obtain final answer $-\frac{\sqrt{3}}{2} + \frac{1}{2}i$ A1 [4]
- 6 (i) Integrate and reach $b \ln 2x - c \int x \cdot \frac{1}{x} dx$, or equivalent M1*
- Obtain $x \ln 2x - \int x \cdot \frac{1}{x} dx$, or equivalent A1
- Obtain integral $x \ln 2x - x$, or equivalent A1
- Substitute limits correctly and equate to 1, having integrated twice M1(dep*)
- Obtain a correct equation in any form, e.g. $a \ln 2a - a + 1 - \ln 2 = 1$ A1
- Obtain the given answer A1 [6]
- (ii) Use the iterative formula correctly at least once M1
- Obtain final answer 1.94 A1
- Show sufficient iterations to 4 d.p. to justify 1.94 to 2d.p. or show that there is a sign
 change in the interval (1.935, 1.945). A1 [3]
- 7 (i) Separate variables correctly and attempt to integrate at least one side B1
- Obtain term $\ln R$ B1
- Obtain $\ln x - 0.57x$ B1
- Evaluate a constant or use limits $x = 0.5$, $R = 16.8$, in a solution containing terms of the form
 $a \ln R$ and $b \ln x$ M1
- Obtain correct solution in any form A1
- Obtain a correct expression for R , e.g. $R = xe^{(3.80 - 0.57x)}$, $R = 44.7xe^{-0.57x}$ or
 $R = 33.6xe^{(0.285 - 0.57x)}$ A1 [6]
- (ii) Equate $\frac{dR}{dx}$ to zero and solve for x M1
- State or imply $x = 0.57^{-1}$, or equivalent, e.g. 1.75 A1
- Obtain $R = 28.8$ (allow 28.9) A1 [3]
- 8 (i) Use $\sin(A + B)$ formula to express $\sin 3\theta$ in terms of trig. functions of 2θ and θ M1
- Use correct double angle formulae and Pythagoras to express $\sin 3\theta$ in terms of $\sin \theta$ M1
- Obtain a correct expression in terms of $\sin \theta$ in any form A1
- Obtain the given identity A1 [4]
- [SR: Give M1 for using correct formulae to express RHS in terms of $\sin \theta$ and $\cos 2\theta$,
 then M1A1 for expressing in terms of $\sin \theta$ and $\sin 3\theta$ only, or in terms
 of $\cos \theta$, $\sin \theta$, $\cos 2\theta$ and $\sin 2\theta$, then A1 for obtaining the given identity.]

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- (ii) Substitute for x and obtain the given answer B1 [1]
- (iii) Carry out a correct method to find a value of x
Obtain answers 0.322, 0.799, -1.12 M1
[Solutions with more than 3 answers can only earn a maximum of A1 + A1.] A1 + A1 + A1 [4]
- 9 (i) State or imply the form $\frac{A}{1-x} + \frac{B}{2-x} + \frac{C}{(2-x)^2}$ B1
Use a correct method to determine a constant M1
Obtain one of $A = 2, B = -1, C = 3$ A1
Obtain a second value A1
Obtain a third value A1 [5]
- [The alternative form $\frac{A}{1-x} + \frac{Dx+E}{(2-x)^2}$, where $A = 2, D = 1, E = 1$ is marked B1M1A1A1A1 as above.]
- (ii) Use correct method to find the first two terms of the expansion of $(1-x)^{-1}, (2-x)^{-1}, (2-x)^{-2}, (1-\frac{1}{2}x)^{-1}$ or $(1-\frac{1}{2}x)^{-2}$ M1
Obtain correct unsimplified expansions up to the term in x^2 of each partial fraction A1✓ + A1✓ + A1✓
Obtain final answer $\frac{9}{4} + \frac{5}{2}x + \frac{39}{16}x^2$, or equivalent A1 [5]
- [Symbolic binomial coefficients, e.g. $\binom{-1}{1}$ are not sufficient for M1. The ✓ is on A,B,C.]
- [For the A,D,E form of partial fractions, give M1 A1✓ A1✓ for the expansions then, if $D \neq 0$, M1 for multiplying out fully and A1 for the final answer.]
[In the case of an attempt to expand $(x^2 - 8x + 9)(1-x)^{-1}(2-x)^{-2}$, give M1A1A1 for the expansions, M1 for multiplying out fully, and A1 for the final answer.]
- 10 (i) EITHER: Find \overrightarrow{AP} (or \overrightarrow{PA}) for a point P on l with parameter λ ,
e.g. $\mathbf{i} - 17\mathbf{j} + 4\mathbf{k} + \lambda(-2\mathbf{i} + \mathbf{j} - 2\mathbf{k})$ B1
Calculate scalar product of \overrightarrow{AP} and a direction vector for l and equate to zero M1
Solve and obtain $\lambda = 3$ A1
Carry out a complete method for finding the length of AP M1
Obtain the given answer 15 correctly A1
- OR1: Calling $(4, -9, 9)$ B , state \overrightarrow{BA} (or \overrightarrow{AB}) in component form, e.g. $-\mathbf{i} + 17\mathbf{j} - 4\mathbf{k}$ B1
Calculate vector product of \overrightarrow{BA} and a direction vector for l ,
e.g. $(-\mathbf{i} + 17\mathbf{j} - 4\mathbf{k}) \times (-2\mathbf{i} + \mathbf{j} - 2\mathbf{k})$ M1
Obtain correct answer, e.g. $-30\mathbf{i} + 6\mathbf{j} + 33\mathbf{k}$ A1
Divide the modulus of the product by that of the direction vector M1
Obtain the given answer correctly A1
- OR2: State \overrightarrow{BA} (or \overrightarrow{AB}) in component form B1
Use a scalar product to find the projection of BA (or AB) on l M1
Obtain correct answer in any form, e.g. $\frac{27}{\sqrt{9}}$ A1
Use Pythagoras to find the perpendicular M1

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	Obtain the given answer correctly	A1	
OR3:	State \overline{BA} (or \overline{AB}) in component form	B1	
	Use a scalar product to find the cosine of ABP	M1	
	Obtain correct answer in any form, e.g. $\frac{27}{\sqrt{9}\sqrt{306}}$	A1	
	Use trig. to find the perpendicular	M1	
	Obtain the given answer correctly	A1	
OR4:	State \overline{BA} (or \overline{AB}) in component form	B1	
	Find a second point C on l and use the cosine rule in triangle ABC to find the cosine of angle A , B , or C , or use a vector product to find the area of ABC	M1	
	Obtain correct answer in any form	A1	
	Use trig. or area formula to find the perpendicular	M1	
	Obtain the given answer correctly	A1	
OR5:	State correct \overline{AP} (or \overline{PA}) for a point P on l with parameter λ in any form	B1	
	Use correct method to express AP^2 (or AP) in terms of λ	M1	
	Obtain a correct expression in any form, e.g. $(1 - 2\lambda)^2 + (-17 + \lambda)^2 + (4 - 2\lambda)^2$	A1	
	Carry out a method for finding its minimum (using calculus, algebra or Pythagoras)	M1	
	Obtain the given answer correctly	A1	[5]
(ii) EITHER:	Substitute coordinates of a general point of l in equation of plane and either equate constant terms or equate the coefficient of λ to zero, obtaining an equation in a and b	M1*	
	Obtain a correct equation, e.g. $4a - 9b - 27 + 1 = 0$	A1	
	Obtain a second correct equation, e.g. $-2a + b + 6 = 0$	A1	
	Solve for a or for b	M1(dep*)	
	Obtain $a = 2$ and $b = -2$	A1	
OR:	Substitute coordinates of a point of l and obtain a correct equation, e.g. $4a - 9b = 26$	B1	
	EITHER: Find a second point on l and obtain an equation in a and b	M1*	
	Obtain a correct equation	A1	
	OR: Calculate scalar product of a direction vector for l and a vector normal to the plane and equate to zero	M1*	
	Obtain a correct equation, e.g. $-2a + b + 6 = 0$	A1	
	Solve for a or for b	M1(dep*)	
	Obtain $a = 2$ and $b = -2$	A1	[5]