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<p><b>1</b> <math>\lambda = \frac{1}{30}</math>  <math>1 - e^{-\frac{1}{30}}</math>  <math>= 0.0328</math> (3 s.f.)</p>	<p>B1  M1  M1  A1    [4]</p>	<p>o.e  <math>1 - P(X = 0)</math> by Poisson, any <math>\lambda</math> allow 1 end error  <math>1 - P(X = 0)</math> by Poisson, correct <math>\lambda</math> no end errors    S.R. Binomial with final answer 0.0328 B2  Correct answer, no working scores B2</p>
<p><b>2</b> <math>z = 2.576</math>  <math>2 \times z \times \frac{0.17}{\sqrt{n}} = 0.2</math> oe  <math>n = \left(\frac{2 \times 0.17 \times 2.576}{0.2}\right)^2</math> oe (= 19.2)  Smallest <math>n</math> is 20</p>	<p>B1  M1  M1  A1 [4]</p>	<p>Seen (accept 2.574 to 2.579)    Allow without '2 ×' OR with incorrect <math>z</math>    Attempt to arrange equ of correct form (with correct <math>z</math> and '2 ×' into the form <math>n =</math> or <math>\sqrt{n} =</math></p>
<p><b>3 (i)</b> est (<math>\mu</math>) = 2866 or 2870 (3 s.f.)  est (<math>\sigma^2</math>) = <math>\frac{1}{49} (410900000 - \frac{143300^2}{50})</math>  (= 4126.53)  = 4130 (3 sf)</p>	<p>B1  M1    A1 [3]</p>	<p>Accept 143300/50 o.e.  Correct subst in correct formula</p>
<p><b>(ii)</b> <math>H_0</math>: Pop mean (or <math>\mu</math>) = 2850  <math>H_1</math>: Pop mean (or <math>\mu</math>) <math>\neq</math> 2850  <math>\frac{\frac{143300}{50} - 2850}{\frac{\sqrt{4126.53}}{\sqrt{50}}}</math>    = 1.761  '1.761' &lt; 1.96  No evidence mean distance changed</p>	<p>B1  M1    A1  M1  A1f    [5]</p>	<p>Both. Not just 'mean'  Allow '4126.53' without <math>\sqrt{\quad}</math>, but must have all <math>\sqrt{50}</math>    Or correct c.v. (2867.81) for alt method  For valid comparison of <math>z</math> values, areas or c.v.  Dep 1.96; ft their 1.761  If <math>H_1</math>: <math>\mu &gt; 2850</math> and c.f. 1.645,  max B0M1A1M1A0  (c.v. for 1 tail test 2864.94)</p>
<p><b>4 (i)</b> <math>\lambda = 2.8</math>  <math>e^{-2.8} (1 + 2.8 + \frac{2.8^2}{2})</math>  = 0.469 (3 s.f.) or 0.47(0)</p>	<p>B1    M1  A1 [3]</p>	<p>seen    any <math>\lambda</math> allow one end error    As final answer</p>
<p><b>(ii)</b> <math>e^{-0.7n} \geq 0.99</math> or <math>e^{-\lambda} \geq 0.99</math>  <math>-0.7n \geq \ln 0.99</math> or <math>-\lambda \geq \ln 0.99</math>  <math>n \leq 0.01436</math> or <math>\lambda \leq 0.01005</math>  '0.01436' <math>\times</math> 150  or '0.01005' <math>\times</math> 150 <math>\div</math> 0.7  Max period is 2.15 mins (3 sf)</p>	<p>M1  M1  A1    M1  A1 [5]</p>	<p>Allow '=' throughout  Attempt ln both sides  Can be implied. Accept 3 s.f.    Note <math>e^{-(0.7/150)n} \geq 0.99</math> scores 1<sup>st</sup> and 3<sup>rd</sup> M1  T &amp; I leading to ans 2.2 mins, SC: B2</p>

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<p><b>5 (i)</b> <math>\int_0^2 k(x-2)^2 dx = 1</math>  <math>\left(\frac{k(x-2)^3}{3}\right)_0^2 = 1</math>  <math>k\left[0 - \left(-\frac{8}{3}\right)\right] = 1</math>  <math>k = \frac{3}{8}</math> <b>AG</b></p>	<p>M1  A1  [2]</p>	<p>Attempt to integrate <math>f(x)</math> with correct limits and = 1  Must see this line or better, e.g. <math>k \times \frac{8}{3} = 1</math></p>
<p><b>(ii)</b> <math>\frac{3}{8} \int_d^2 (x-2)^2 dx = 0.2</math>  <math>\left(\frac{3}{8} \left[\frac{(x-2)^3}{3}\right]_d^2 = 0.2\right)</math>  <math>\frac{3}{8} \left[0 - \frac{(d-2)^3}{3}\right] = 0.2</math> oe  <math>((d-2)^3 = -1.6)</math>  <math>d = 0.83(0)</math> (3 s.f.)</p>	<p>M1  M1  A1 [3]</p>	<p><math>\int f(x)dx</math> with limits <math>d</math> and 2 or 0 and <math>d</math>, and = 0.2 or =0.8  Condone missing 'k'  Reasonable attempt to integrate from a correct expression, with limits substituted to give expression in <math>d^3</math>.  Condone missing 'k'</p>
<p><b>(iii)</b> <math>\frac{3}{8} \int_0^2 x(x-2)^2 dx</math>  <math>(= \frac{3}{8} \int_0^2 x^3 - 4x^2 + 4xdx)</math>  <math>= \frac{3}{8} \left[\frac{x^4}{4} - \frac{4x^3}{3} + 2x^2\right]_0^2</math>  <math>= \frac{1}{2}</math></p>	<p>M1  A1  A1 [3]</p>	<p>Attempt integ <math>xf(x)</math>; ignore limits, condone missing <math>k</math>  <math>\left(\frac{3}{8} \left[x \times \frac{(x-2)^3}{3} - \int \frac{(x-2)^3}{3} dx\right]_0^2\right)</math>  <math>= \frac{3}{8} \left[x \times \frac{(x-2)^3}{3} - \frac{(x-2)^4}{12}\right]_0^2</math>  Correct integration &amp; limits, condone missing <math>k</math></p>
<p><b>6 (i)</b> <math>P(\text{Type I}) = 1 - P(\geq 4 \text{ assuming } p = 0.7)</math>  <math>1 - ({}^6C_4 \times 0.7^4 \times 0.3^2 + {}^6C_5 \times 0.7^5 \times 0.3 + 0.7^6)</math>  <math>(= 1 - 0.744)</math>  <math>= 0.256</math> (3 s.f.)</p>	<p>M1 M1 A1 [3]</p>	<p>or <math>P(\leq 3 \text{ assuming } p = 0.7)</math> May be implied  <math>{}^6C_3 \times 0.7^3 \times 0.3^3 + {}^6C_2 \times 0.7^2 \times 0.3^4 + {}^6C_1 \times 0.7 \times 0.3^5 + 0.3^6</math>  Allow one end error  <math>= 0.256</math> (3 s.f.)  SR if zero scored allow B1 for use of <math>B(6, 0.7)</math> in any two or more terms</p>
<p><b>(ii)</b> <math>P(\text{Type II}) = P(\geq 4 \text{ assuming } p = 0.35)</math>  <math>= {}^6C_4 \times 0.35^4 \times 0.65^2 + {}^6C_5 \times 0.35^5 \times 0.65 + 0.35^6</math>  <math>= 0.117</math></p>	<p>M1 M1 A1 [3]</p>	<p>May be implied  Allow one end error  SR if zero scored allow B1 for use of <math>B(6, 0.35)</math> in any two or more terms</p>
<p><b>(iii)</b> Type 1  They will reject Luigi's belief, although it might be true.</p>	<p>B1 B1 [2]</p>	<p>In context</p>

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<p><b>7 (i)</b> <math>N(10.61, 0.1017)</math>  <math>\frac{11-10.61}{\sqrt{0.1017}}</math> (= 1.223)  <math>\Phi(1.223)</math>  = 0.889 (3 s.f.)</p>	<p>B1  M1 M1  A1 [4]</p>	<p>o.e. Stated or implied (accept in un-simplified form)  Allow without <math>\sqrt{\quad}</math> For attempt to find correct area consistent with their working</p>
<p><b>(ii)</b> <math>P(K - 1.2A &gt; 0)</math>  <math>\text{Var} = 0.0576 + 1.2^2 \times 0.0441</math>  (= 0.121104)  <math>N(-0.324, 0.121104)</math>  <math>\frac{0 - (-0.324)}{\sqrt{0.121104}}</math> (= 0.931)  <math>1 - \Phi(0.931)</math>  = 0.176 (3 s.f.)</p>	<p>M1  B1 B1  M1 M1  A1 [6]</p>	<p>Or similar stated or implied  o.e. May be implied (accept in un-simplified form)  Allow without <math>\sqrt{\quad}</math> For attempt to find correct area consistent with their working</p>