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<p>1 bars are not touching oe</p> <p>Area not rep by frequency, not used fd, not labelled fd</p>	<p>B1</p> <p>B1 2</p>	<p>Sensible reason involving not touching, no gaps, class boundaries, group data not continuous (may be the negative)</p> <p>Must be frequency density oe. Wrong height not sufficient. (Best 2 reasons awarded)</p>
<p>2</p> $P(13.6 < X < 14.8) = P\left(\frac{13.6 - 14}{0.52} < z < \frac{14.8 - 14}{0.52}\right)$ $= P(-0.7692 < z < 1.538)$ $= \Phi(1.538) - [1 - \Phi(0.7692)]$ $= 0.9380 - [1 - 0.7791]$ $= 0.7171$ $P(8) = (0.7171)^8 (0.2829)^2 {}_{10}C_8$ $= 0.252$	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1 5</p>	<p>Standardising 1 expression, no cc, no sq rt, no sq, ±, mean on num.</p> <p>$\Phi 1 + \Phi 2 - 1$ (indep) oe ($\Phi 2 - \Phi 1$ if cc used)</p> <p>Correct probability rounding to 0.72 here</p> <p>Binomial expression $10C_8 p^8 q^2$, $\Sigma p + q = 1$, any p</p> <p>Correct answer (rounding to 0.252)</p>
<p>3 (i) $(p =)0.85$</p> $P(< 12) = 1 - P(12, 13, 14)$ $= 1 - [(0.85)^{12} (0.15)^2 {}_{14}C_{12} + (0.85)^{13} (0.15) {}_{14}C_{13} + (0.85)^{14}]$ $= 1 - 0.6479$ $= 0.352$	<p>B1</p> <p>M1</p> <p>A1 3</p>	<p>$(p =)0.85$ oe seen anywhere</p> <p>Summing 2 or 3 consistent bin probs, any $p < 1$, $n = 14$ (or summing 12 or 13 consistent bin probs)</p> <p>Correct answer</p>
<p>(ii) $(0.85)^n \geq 0.1$</p> $n \leq 14.2$ $n = 14$	<p>M1</p> <p>M1</p> <p>A1 3</p>	<p>Eqn or inequality in 0.85(or 0.15), n, 0.1, n as a power</p> <p>Attempt to solve (can be implied) if n a power</p> <p>Correct answer – must be equals, not approx. MR allowed for 0.01, M1M1A0 max.</p>
<p>4 (i) $(220 \times 20 + 118 \times 25) / 45$</p> $= 163$	<p>M1</p> <p>A1 2</p>	<p>Mult by 20 and 25 and dividing their sum by 45</p> <p>Correct answer, 163.3 or $490/3$ oe acceptable</p>
<p>(ii) $\Sigma x_o^2 / 20 - 220^2 = 32^2$</p> $\Sigma x_o^2 = 988480$ $\Sigma x_i^2 / 25 - 118^2 = 12^2$ $\Sigma x_i^2 = 351700$ $\Sigma x_o^2 + \Sigma x_i^2 = 1340180$ $\text{New var} = 1340180 / 45 - (7350 / 45)^2$ $= 3100 - 3120$	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1 5</p>	<p>Subst in correct variance formula</p> <p>Correct Σx_o^2</p> <p>correct Σx_i^2</p> <p>Subst their combined results in correct var formula</p> <p>Correct answer</p>

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<p>5 (a) $P(X < q + 82) = 0.72$ $z = 0.583$ $\frac{\pm q}{7.4}$ or $\frac{\pm 2q}{7.4} = z$ or <i>probabilty</i> (o.e.) $q = 4.31$</p>	<p>M1 M1 A1</p>	<p>3 Rounding to ± 0.58 or ± 0.15 seen Standardising, no cc, no sq, no sq rt correct answer</p>
<p>(b) $\frac{0.5\mu - \mu}{\sigma} = \frac{\pm 0.5\mu}{\sigma}$ $\frac{0.2\sigma^2}{\sigma} = -0.2\sigma = -0.580$ $\sigma = 2.90$ $\mu = 3.36$</p>	<p>M1 B1 M1 A1</p>	<p>4 Standardising attempt some μ/σ allow cc, sq rt, sq Can be implied ± 0.580 seen (accept ± 0.58) substituting to eliminate μ or σ, arriving at numerical solution, any z value or probability – not dependent both answers correct, accept 2.9</p>
<p>6 (i) $\frac{8!}{3!2!2!}$ $= 1680$</p>	<p>M1 A1</p>	<p>2 8! Divided by at least one of 3!2!2! oe Correct answer</p>
<p>(ii) $5!$ $= 120$</p>	<p>M1 A1</p>	<p>2 5! Seen (not added, may be divided/multiplied) Correct answer</p>
<p>(iii) $\frac{5!4!}{3!2!2!}$ $= 120$</p>	<p>B1 M1 A1</p>	<p>3 5! Or 4! Seen in sum or product in numerator (denominator may be 1) $\frac{k5!4!}{3!2!2!}$ in a numerical expression Correct final answer</p>
<p>(iv) GG with AA, AE, EE, RA, RE, RT, TA, TE, $= 8$ ways GGG with A, E, R, T = 4 ways Total = 12 ways</p>	<p>M1 A1 A1</p>	<p>3 Summing 2 options (could be lists) 1 correct option Correct answer</p>

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<p>7 (i) $P(\text{same}) = P(1, 1) + P(3, 3) + P(5, 5)$ $= \frac{2}{9} \times \frac{1}{8} + \frac{4}{9} \times \frac{3}{8} + \frac{3}{9} \times \frac{2}{8}$ $= 5/18 (0.278)$ Alt. method: $\frac{2C_2 + 4C_2 + 3C_2}{9C_2}$ or $\frac{2 \times 1 + 3 \times 4 + 2 \times 3}{9C_2 \times 2}$ oe</p>	<p>M1 M1 A1 3</p>	<p>Summing 3 two-factor options Multiplying terms by one less in the numerator or denominator Correct answer M1 for numerator, M1 for denominator, A1 correct answer</p>								
<p>(ii) $P(5, \bar{5}) + P(\bar{5}, 5)$ $= \frac{3}{9} \times \frac{6}{8} + \frac{6}{9} \times \frac{3}{8} = \frac{36}{72} = \frac{1}{2}$ or 0.5 Alt. method: $\frac{6C_1 \times 3C_1 (\times 2)}{9C_2 (\times 2)}$ oe</p>	<p>M1 M1 A1 3</p>	<p>Mult 2 probs whose numerators sum to 9 o.e. Summing 2 options or mult by 2 (may be 4 options) Correct answer M1 for numerator, M1 for denominator, A1 correct answer</p>								
<p>(iii) $P(5 \cap \bar{5}) = \frac{3}{9} \times \frac{6}{8} = \frac{1}{4}$ $P(\bar{5}) = \frac{1}{4} + \frac{6}{9} \times \frac{5}{8} = 48/72 = 0.6666$ $P(5_1 \bar{5}_2) = \frac{1/4}{48/72} = 3/8 = 0.375$</p>	<p>M1 M1 A1 A1 4</p>	<p>Attempt at $P(5 \text{ and not } 5)$ seen as numerator or denominator of a fraction Attempt at $P(\text{not } 5)$ sum of 2 two-factor terms seen anywhere Correct $P(\bar{5})$ as numerator or denominator in fraction Correct answer</p>								
<p>(iv)</p> <table border="1" data-bbox="245 1458 632 1532"> <tr> <td>x</td> <td>0</td> <td>1</td> <td>2</td> </tr> <tr> <td>$P(X=x)$</td> <td>5/12</td> <td>1/2</td> <td>1/12</td> </tr> </table> <p>$P(0) = P(\bar{5}, \bar{5}) = \frac{6}{9} \times \frac{5}{8} = 30/72 (5/12)$ (0.4166) $P(1) = 0.5$ from part (ii) $P(2) = 6/72 (1/12) (0.0833)$ from part (i)</p>	x	0	1	2	$P(X=x)$	5/12	1/2	1/12	<p>B1 B1 B1ft 3</p>	<p>Values 0, 1, 2 seen in table with at least 1 prob Correct $P(0)$ unsimplified If $x=0,1,2(,3)$ ft $\Sigma p = 1$, no -ve values, all probabilities <1</p>
x	0	1	2							
$P(X=x)$	5/12	1/2	1/12							