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1	$T = 12 \times (0.6 - 0.4) / 0.4$ $6 = 0.1v^2 / 0.6$ $v = 6 \text{ ms}^{-1}$	M1 M1 A1	[3]	Uses $T = \lambda x / L$, (=6) N2L 1 force and RA	3
2 (i)	$0.5v \frac{dv}{dx} = 0.5g - 0.015x^2$ $v \frac{dv}{dx} = 10 - 0.03x^2$ AG	M1 A1	[2]	N2L 2 forces	
(ii)	18.3 m	B1	[1]	$\sqrt{(10/0.03)} = 18.257..$	
(iii)	$\int v \, dv = \int (10 - 0.03x^2) \, dx$ $v^2 / 2 = 10x - 0.03x^3 / 3 (+c)$ $v^2 / 2 = 10 \times 18.3 - 0.03 \times 18.3^3 / 3$ $v = 15.6 \text{ ms}^{-1}$	M1 A1 M1 A1	[4]	Attempts to integrate Accept omission of c Uses ans (ii) in formula for v^2	7
3	$R \cos \theta = 0.5 \text{ g} (=5)$ $R \sin \theta = 0.5 \times 5^2 \times 0.4 (=5)$ $\tan \theta = (0.5 \times 5^2 \times 0.4) / (0.5 \text{ g})$ $\theta = 45^\circ$ AG $R = 0.5 \text{ g} / \cos 45$ $R = 7.07 \text{ N}$	B1 M1 M1 A1 M1 A1	[6]	Resolving vertically Use of N2L horizontally with $\text{acc}^n = w^2 r$ Eliminating R $R^2 = (0.5 \times 5^2 \times 0.4)^2 + (0.5 \text{ g})^2$ 7.071..	6
4 (i)	$0.2a = 0.024t - 0.2 \text{ g} \times 0.3$ $a = 0.12t - 3$ $\int dv = \int (0.12t - 3) \, dt,$ $v = 0.12t^2 / 2 - 3t + c, t = 0, v = 0.9$ hence $c = 0.9$ $v = 0.06(t^2 - 50t + 15)$ AG	M1 A1 M1 A1	[4]	Uses N2L Integrates and finds c	
(ii)	$t^2 - 50t + 15 = 0$ $t = 0.302$	M1 A1	[2]	Solves 3 term quadratic Smaller +ve root only	

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(iii)	$0.024t = 0.3 \times 0.2 g$ $t = 25$	M1 A1	[2] Equates tractive force and friction force 8
5 (i)	$v_v^2 = (15\sin 30)^2 + 2g \times 20$ $V^2 = (15\cos 30)^2 + (15\sin 30)^2 + 2g \times 20$ $V = 25 \text{ ms}^{-1}$ $\theta (= \tan^{-1} 21.36/(15\cos 30)) = 58.7^\circ$	M1 M1 A1 A1	[4] $v_v = 21.3600..$ V or θ from components, V by energy 58.69..
(ii)	$-20 = (15\sin 30)t - gt^2/2$ $2t^2 - 3t - 8 = 0 \Rightarrow t (= 2.866..) = 2.89$ OR $t = (15\sin 30)/10 + (25\sin 58.7)/10$ $t = 2.89$ $OP^2 = 20^2 + (15\cos 30 \times 2.886)^2$ $OP = 42.5 \text{ m}$	M1 A1 M1 A1 M1 A1	[4] M1 maybe gained in (i) A1 maybe gained in (i) Separating rise and fall times 42.491.. 8
6 (i)	$0.4 g = 50e/0.8$ Moves down = 0.044 m $0.4 \times 1.5^2/2 + 0.4 g \times 0.044 + 50(0.82 - 0.8)^2/(2 \times 0.8)$ $= 0.4v^2/2 + 50 \times 0.064^2/(2 \times 0.8)$ $v = 1.6(0) \text{ ms}^{-1}$	M1 A1 M1 A1 A1	[5] Uses $T = \lambda \times /L$ ($e = 0.064$) ($0.8 + 0.064 - 0.82$) Sets up 2EE/2KE/PE equation
(ii)	PE gain to reach O = $0.4 g \times 0.82$ $KE + EE = 0.4 \times 1.5^2/2 + 50(0.82 - 0.8)^2/(2 \times 0.8)$ Shows by evaluation that insufficient energy	B1 M1 A1	[3] From initial position, (3.28J) At initial position, (0.4625J) 8

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7	(i)	$\pi \times 0.5^2 \times 0.4 \times 0.2 + \pi \times 0.5^2 \times 0.4 \times 0.5/3$ $= (\pi \times 0.5^2 \times 0.4 + \pi \times 0.5^2 \times 0.4/3) \text{OG AG}$ $d = 0.275 \text{ m}$	M1 A1 A1	[3]	Uses table of moments idea	
	(ii)	$(0.4 + 0.4)F = 0.5 \times 60$ $F = 37.5$	M1 A1	[2]	Takes moments	
	(iii)	$\mu (= 37.5/60) = 0.625$	B1 ft	[1]	cv(F)/60	
	(iv)	$F/R = (60 \sin 30) / (60 \cos 30) (= 0.577..)$ $0.577 < 0.625 \text{ (or } \mu \text{), no sliding AG}$ $\tan \theta = (0.4 - 0.275) / 0.5$ $\theta = 14^\circ \quad \text{AG}$	M1 A1 M1 A1	[4]	Or quotes $\tan 30 < 0.625$ Or $0.5 \tan 30 = 0.288..$ $0.4 - 0.29 < 0.275$, topples	10