

Page 4	Mark Scheme	Syllabus	Paper
	GCE AS/A LEVEL – October/November 2013	9709	42

1	Applying	M1	3	For resolving forces parallel to the line of greatest slope $T (24/25) = 5.1 (8/17)$ or $T \cos 16.26 = 5.1 \sin 28.07$
	$T \cos \beta = W \sin \alpha$	A1		
	Tension is 2.5 N	A1		

First Alternative Marking Scheme

	Applying	M1	3	For resolving forces vertically or horizontally $R \cos 28.07 + T \sin 44.33 = 5.1$ and $R \sin 28.07 = T \cos 44.33$
	$R \cos \alpha + T \sin (\alpha + \beta) = W$ and $R \sin \alpha = T \cos (\alpha + \beta)$	A1		
	Tension is 2.5 N	A1		

Second Alternative Marking Scheme

	Applying	M1	3	Using Triangle of forces $T / \sin 28.07 = 5.1 / \sin 106.26$
	$T / \sin \alpha = 5.1 / \sin (90 + \beta)$	A1		
	Tension is 2.5 N	A1		

2	Gain in KE = $\frac{1}{2} 25 \times 3^2$	M1	5	For using $KE = \frac{1}{2} m v^2$ or $WD = F d \cos \alpha$ For using WD by pulling force = KE gain + WD against resistance
	or WD by pulling force = $220 \times 15 \cos \alpha$	A1		
	WD by pulling force = $220 \times 15 \cos \alpha$	B1		
	or Gain in KE = $\frac{1}{2} 25 \times 3^2$	M1		
	[$3300 \cos \alpha = 112.5 + 3000$]	A1		
$\alpha = 19.4$				

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3	(i)		M1		For using $F = P/v$ and Newton's 2 nd law with $a = 0$
		$100/4 - 4k = 0 \rightarrow k = 6.25$	A1	2	AG
	(ii)		M1		For using Newton's 2 nd law with $a = 0$ uphill \rightarrow 3 term equation
		$100/v - 70g \times 0.05 - 6.25v = 0$	A1		
		$[6.25v^2 + 35v - 100 = 0]$ or $[v^2 + 5.6v - 16 = 0]$	M1		For solving a 3-term quadratic for v
		Maximum speed is 2.08 ms^{-1}	A1	4	

4			M1		For resolving three forces parallel to the plane
	$0.6g \sin \alpha = F + P \cos \alpha$		A1		Value of α used or values of $\sin \alpha$ and $\cos \alpha$ used
			M1		For resolving three forces perpendicular to the plane
	$R = 0.6g \cos \alpha + P \sin \alpha$		A1		Value of α used or values of $\sin \alpha$ and $\cos \alpha$ used
	$0.6g \sin \alpha - P \cos \alpha =$ $0.4 (0.6g \cos \alpha + P \sin \alpha)$		A1		For using $F = \mu R$
	$6(12/13) - P(5/13) =$ $2.4(5/13) + 0.4P(12/13)$		M1		Value of α used or values of $\sin \alpha$ and $\cos \alpha$ used
	$P = 6.12$		A1	8	For solving the resultant equation for P

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Alternative Marking Scheme

	$W = R \cos \alpha + F \sin \alpha$	M1		For resolving three forces vertically
		A1		Value of α used or values of $\sin \alpha$ and $\cos \alpha$ used
	$P = R \sin \alpha - F \cos \alpha$	M1		For resolving three forces horizontally
		A1		Value of α used or values of $\sin \alpha$ and $\cos \alpha$ used
	$0.6g = R(5/13) + 0.4R(12/13)$ and $P = R(12/13) - 0.4R(5/13)$	M1		For using $F = \mu R$ in both equations
		A1		Value of α used or values of $\sin \alpha$ and $\cos \alpha$ used
	$78 = R(5 + 4.8)$ and $13P = R(12 - 2)$ $\rightarrow 13P = (78 \div 9.8) \times 10$	M1		For finding R and substituting into an expression for P
	$P = 6.12$	A1	8	

5	(i)	$[s = t^2/2 - 0.1t^3/3]$	M1*		For integrating to find s for $0 \leq t \leq 5$
		$[s_1 = 25/2 - 0.1 \times 125/3]$			For obtaining s_1 by using limits 0 to 5 or having zero for constant of integration (can be implied) and substituting $t = 5$
		$s_1 = 8.33$	DM1*		
			A1	3	
	(ii)	$s_2 = 2.5 \times 40$	A1	M1	For using $s = v(5) \times (45 - 5)$ for $5 \leq t \leq 45$
		$[s = 9t^2/2 - 0.1t^3/3 - 200t$ for $45 \leq t \leq 50]$			For integrating to find s for $45 \leq t \leq 50$ and implying the use of limits 45 and 50 or equivalent via constant of integration
		$s_3 = [9(50)^2/2 - 0.1(50)^3/3 - 200(50)]$ $- [9(45)^2/2 - 0.1(45)^3/3 - 200(45)]$	M1		
		$[= 8.33]$	A1		For applying the limits at 45 and 50 correctly or equivalent via constant of integration

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Alternative mark scheme for previous 2 marks

	Recognising the symmetry of the velocity distribution due to the correspondence of the points (0,0) → (50,0) and (5,2.5) → (45,2.5)	(M1)		
	Complete the idea of symmetry with one further property and hence State $s_3 = s_1 = 8.33$	(A1)		Property is any one of $a(0) = -a(50)$ $a(5) = a(45)$ $v(2.5) = v(47.5)$ oe
	Distance from O to A is 117m	A1		
	Average speed is 2.33 ms^{-1}	B1ft	6	ft answer for total distance

6	(i)				For applying Newton's 2 nd law to A or B
		$T - 0.4g = 0.4a$ or $1.6g - T = 1.6a$	M1		
		$1.6g - T = 1.6a$ or $T - 0.4g = 0.4a$ or $1.6g - 0.4g = (1.6 + 0.4)a$	A1		
		$T = 6.4$	B1		
		Work done by tension is 7.68 J	A1		
			B1ft	5	

Alternative mark scheme for 6 (i)

					For applying Newton's 2 nd law to A or B
		$T - 0.4g = 0.4a$ or $1.6g - T = 1.6a$	M1		
		$1.6g - T = 1.6a$ or $T - 0.4g = 0.4a$ or $1.6g - 0.4g = (1.6 + 0.4)a$	A1		
		WD by T = initial PE – final KE $= 1.6 \times g \times 1.2 - \frac{1}{2} \times 1.6 \times 14.4$	B1		
		WD by T = $19.2 - 11.52 = 7.68$	M1		For finding v^2 and applying Work/Energy equation to B
			A1	5	

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6 (ii)	$[1.6 \times 10 \times 1.2 = \frac{1}{2} 1.6 v^2 + 7.68]$	M1	4	For using PE loss = KE gain + WD by T to find v^2
	$v^2 = 14.4$	A1		For using PCE for A's motion after B reaches the ground or $0 = u^2 - 2gh$ and $H = 2 \times 1.2 + h$
	$14.4 = 2 \times 10 \times h$ $h = 0.72$ $H = 2 \times 1.2 + h$	M1		
	Greatest height is 3.12 m	A1		

First Alternative Marking Scheme for 6 (ii)

	$[v^2 = 2 \times 6 \times 1.2]$	M1	4	For using $v^2 = 2as$ to find v^2
	$v^2 = 14.4$	A1		For using PCE for A's motion after B reaches the ground or $0 = u^2 - 2gh$ and $H = 2 \times 1.2 + h$
	$14.4 = 2 \times 10 \times h$ $h = 0.72$ $H = 2 \times 1.2 + h$	M1		
	Greatest height is 3.12 m	A1		

Second Alternative Marking Scheme for 6 (ii)

	WD by T = Increase in PE $7.68 = 0.4 \times g \times s$	M1	4	For applying WD by T to particle A's complete motion
	$s = 1.92$	A1		For adding 1.2 to s
	$H = 1.2 + s$	M1		
	$H = 1.2 + 1.92 = 3.12$ Height = 3.12 m	A1		

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7	(i)	$[s = \frac{1}{2} 5 \times 0.4 + 19 \times 0.4 + \frac{1}{2} 4 \times 0.4]$ Distance = 9.4	M1 A1	2	For using the area property for distance
	(ii)	Acceleration is 0.08 ms^{-2} Deceleration is 0.1 ms^{-2}	B1 B1	2	
	(iii)	$[T - (800 + 100)g = (800 + 100)a]$ $T - 900g = 900a$ $T = 9072 \text{ N}$ in 1 st stage $T = 9000 \text{ N}$ in 2 nd stage $T = 8910 \text{ N}$ in 3 rd stage	M1 A1 A1	3	For applying Newton's 2 nd law to the <u>elevator and box</u>
	(iv)	$[R - 100g = 100a]$ $R = 1008 \text{ N}$ $R = 990 \text{ N}$	M1 A1 A1	3	For applying Newton's 2 nd law to the <u>box</u> For obtaining the greatest value of the force on the box For obtaining the least value of the force on the box