

Page 4	Mark Scheme	Syllabus	Paper
	GCE AS LEVEL – October/November 2013	9709	23

- 1 Either State or imply non-modular inequality $(x+1)^2 < (3x+5)^2$, or corresponding equation or pair of linear equations M1
 Make reasonable solution attempt at a 3-term quadratic, or solve two linear equations M1
 Obtain critical values -2 and $-\frac{3}{2}$ A1
 State correct answer $x < -2$ or $x > -\frac{3}{2}$ A1
- Or Obtain one critical value, e.g. $x = -2$, by solving a linear equation (or inequality) or from a graphical method or by inspection B1
 Obtain the other critical value similarly B2
 State correct answer $x < -2$ or $x > -\frac{3}{2}$ B1 [4]
- 2 (i) Consider sign of $x^4 + 2x - 9$ at $x = 1.5$ and $x = 1.6$ M1
 Complete the argument correctly with appropriate calculations A1 [2]
 ($f(1.5) = -0.9375, f(1.6) = 0.7536$)
- (ii) Rearrange $x^4 + 2x - 9 = 0$ to given equation or *vice versa* B1 [1]
- (iii) Use the iterative formula correctly at least once M1
 Obtain final answer 1.56 A1
 Show sufficient iterations to justify its accuracy to 2 d.p. B1 [3]

$x_0 = 1.5$	$x_0 = 1.55$	$x_0 = 1.6$
1.5874	1.5614	1.5362
1.5424	1.5556	1.5685
1.5653		1.5520
1.5536		1.5604
1.5595		1.5561
1.5565		

or show there is a sign change in the interval (1.555, 1.565)

- 3 Obtain derivative $e^{2x} - 5e^x + 4$ B1
 Equate derivative to zero and carry out recognisable solution method for a quadratic in e^x M1
 Obtain $e^x = 1$ or $e^x = 4$ A1
 Obtain $x = 0$ and $x = \ln 4$ A1
 Use an appropriate method for determining nature of at least one stationary point M1
 $\left(\frac{d^2y}{dx^2} = 2e^{2x} - 5e^x, \text{ when } x = 0, \frac{d^2y}{dx^2} = -(3), x = \ln 4, \frac{d^2y}{dx^2} = +(12) \right)$
 Conclude maximum at $x = 0$ and minimum at $x = \ln 4$ (no errors seen) A1 [6]
- 4 (i) Substitute $x = 3$ and equate to 14 ($9a + 3b + 35 = 14$) M1
 Substitute $x = -2$ and equate to 24 ($4a - 2b = 24$) M1
 Obtain a correct equation in any form A1
 Solve a relevant pair of equations for a or for b M1
 Obtain $a = 1$ and $b = -10$ A1 [5]

Page 5	Mark Scheme	Syllabus	Paper
	GCE AS LEVEL – October/November 2013	9709	23

- (ii) Attempt division by $x^2 + 2x - 8$ and reach a partial quotient of $x - k$ M1
 Obtain quotient $x - 1$ with no errors seen (can be done by observation) A1
 Correct solution method for quadratic e.g. factorisation M1
 All solutions $x = 1, x = 2$ and $x = -4$ given and no others CWO A1 [4]
- 5 (i) State $\frac{dx}{d\theta} = -2 \sin 2\theta + \sin \theta$ or $\frac{dy}{d\theta} = 8 \sin \theta \cos \theta$ B1
 Use $\frac{dy}{dx} = \frac{dy}{d\theta} \div \frac{dx}{d\theta}$ M1
 Use $\sin 2\theta = 2 \sin \theta \cos \theta$ M1
 Obtain given answer correctly A1 [4]
- (ii) Equate derivative to -4 and solve for $\cos \theta$ M1
 Obtain $\cos \theta = \frac{1}{2}$ A1
 Obtain $x = -1$ A1
 Obtain $y = 3$ A1 [4]
- 6 (a) (i) Attempt to divide by e^{2x} and attempt to integrate 2 terms M1
 Integrate a term of form ke^{-2x} correctly A1^{ft}
 Fully correct integral $x - 3e^{-2x} (+c)$ A1 [3]
- (ii) State correct expression $\frac{1}{2} \cos 2x + \frac{1}{2}$ or equivalent B1
 Integrate an expression of the form $a + b \cos 2x$, where $ab \neq 0$, correctly M1
 State correct integral $\frac{3 \sin 2x}{4} + \frac{3x}{2} (+c)$ A1 [3]
- (b) State or imply correct ordinates 5.46143..., 4.78941..., 4.32808... B1
 Use correct formula, or equivalent, correctly with $h = 0.5$ and three ordinates M1
 Obtain answer 4.84 with no errors seen A1 [3]
- 7 (i) State $R = \sqrt{10}$ B1
 Use trig formula to find α M1
 Obtain $\alpha = 18.43^\circ$ with no errors seen A1 [3]
- (ii) Carry out evaluation of $\cos^{-1}\left(\frac{2}{R}\right) (\approx 50.77^\circ)$ M1
 Carry out correct method for one correct answer M1
 Obtain one correct answer e.g. 34.6° A1
 Carry out correct method for a further answer M1
 Obtain remaining 3 answers $163.8^\circ, 214.6^\circ, 343.8^\circ$ and no others in the range A1 [5]