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- 1 Either State or imply non-modular inequality  $(x+1)^2 < (3x+5)^2$ , or corresponding equation or pair of linear equations M1  
 Make reasonable solution attempt at a 3-term quadratic, or solve two linear equations M1  
 Obtain critical values  $-2$  and  $-\frac{3}{2}$  A1  
 State correct answer  $x < -2$  or  $x > -\frac{3}{2}$  A1
- Or Obtain one critical value, e.g.  $x = -2$ , by solving a linear equation (or inequality) or from a graphical method or by inspection B1  
 Obtain the other critical value similarly B2  
 State correct answer  $x < -2$  or  $x > -\frac{3}{2}$  B1 [4]
- 2 (i) Consider sign of  $x^4 + 2x - 9$  at  $x = 1.5$  and  $x = 1.6$  M1  
 Complete the argument correctly with appropriate calculations A1 [2]  
 ( $f(1.5) = -0.9375, f(1.6) = 0.7536$ )
- (ii) Rearrange  $x^4 + 2x - 9 = 0$  to given equation or *vice versa* B1 [1]
- (iii) Use the iterative formula correctly at least once M1  
 Obtain final answer 1.56 A1  
 Show sufficient iterations to justify its accuracy to 2 d.p. B1 [3]

$x_0 = 1.5$	$x_0 = 1.55$	$x_0 = 1.6$
1.5874	1.5614	1.5362
1.5424	1.5556	1.5685
1.5653		1.5520
1.5536		1.5604
1.5595		1.5561
1.5565		

or show there is a sign change in the interval (1.555, 1.565)

- 3 Obtain derivative  $e^{2x} - 5e^x + 4$  B1  
 Equate derivative to zero and carry out recognisable solution method for a quadratic in  $e^x$  M1  
 Obtain  $e^x = 1$  or  $e^x = 4$  A1  
 Obtain  $x = 0$  and  $x = \ln 4$  A1  
 Use an appropriate method for determining nature of at least one stationary point M1  
 $\left( \frac{d^2y}{dx^2} = 2e^{2x} - 5e^x, \text{ when } x = 0, \frac{d^2y}{dx^2} = -(3), x = \ln 4, \frac{d^2y}{dx^2} = +(12) \right)$   
 Conclude maximum at  $x = 0$  and minimum at  $x = \ln 4$  (no errors seen) A1 [6]
- 4 (i) Substitute  $x = 3$  and equate to 14  $(9a + 3b + 35 = 14)$  M1  
 Substitute  $x = -2$  and equate to 24  $(4a - 2b = 24)$  M1  
 Obtain a correct equation in any form A1  
 Solve a relevant pair of equations for  $a$  or for  $b$  M1  
 Obtain  $a = 1$  and  $b = -10$  A1 [5]

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- (ii) Attempt division by  $x^2 + 2x - 8$  and reach a partial quotient of  $x - k$  M1  
 Obtain quotient  $x - 1$  with no errors seen (can be done by observation) A1  
 Correct solution method for quadratic e.g. factorisation M1  
 All solutions  $x = 1, x = 2$  and  $x = -4$  given and no others CWO A1 [4]
- 5 (i) State  $\frac{dx}{d\theta} = -2 \sin 2\theta + \sin \theta$  or  $\frac{dy}{d\theta} = 8 \sin \theta \cos \theta$  B1  
 Use  $\frac{dy}{dx} = \frac{dy}{d\theta} \div \frac{dx}{d\theta}$  M1  
 Use  $\sin 2\theta = 2 \sin \theta \cos \theta$  M1  
 Obtain given answer correctly A1 [4]
- (ii) Equate derivative to  $-4$  and solve for  $\cos \theta$  M1  
 Obtain  $\cos \theta = \frac{1}{2}$  A1  
 Obtain  $x = -1$  A1  
 Obtain  $y = 3$  A1 [4]
- 6 (a) (i) Attempt to divide by  $e^{2x}$  and attempt to integrate 2 terms M1  
 Integrate a term of form  $ke^{-2x}$  correctly A1<sup>ft</sup>  
 Fully correct integral  $x - 3e^{-2x} (+c)$  A1 [3]
- (ii) State correct expression  $\frac{1}{2} \cos 2x + \frac{1}{2}$  or equivalent B1  
 Integrate an expression of the form  $a + b \cos 2x$ , where  $ab \neq 0$ , correctly M1  
 State correct integral  $\frac{3 \sin 2x}{4} + \frac{3x}{2} (+c)$  A1 [3]
- (b) State or imply correct ordinates 5.46143..., 4.78941..., 4.32808... B1  
 Use correct formula, or equivalent, correctly with  $h = 0.5$  and three ordinates M1  
 Obtain answer 4.84 with no errors seen A1 [3]
- 7 (i) State  $R = \sqrt{10}$  B1  
 Use trig formula to find  $\alpha$  M1  
 Obtain  $\alpha = 18.43^\circ$  with no errors seen A1 [3]
- (ii) Carry out evaluation of  $\cos^{-1}\left(\frac{2}{R}\right) (\approx 50.77^\circ)$  M1  
 Carry out correct method for one correct answer M1  
 Obtain one correct answer e.g.  $34.6^\circ$  A1  
 Carry out correct method for a further answer M1  
 Obtain remaining 3 answers  $163.8^\circ, 214.6^\circ, 343.8^\circ$  and no others in the range A1 [5]